

# HEAT TRANSFER ENHANCEMENT AND PRESSURE DROP FROM TUBE BANK WITH SPLITTER PLATES IN CROSS FLOW EMPLOYING RANS AND LES TURBULENCE MODELS

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*Heat transfer enhancement from tube bank in cross flow with air can be achieved for energy saving by enhancing the flow turbulence nature. Adding splitter plates (SPs) to the tubes' trailing edges, besides, increasing the heat transfer surface's roughness are proposed options to enhance the flow turbulence. However, few literatures are available to discuss this, moreover, almost all available Computational Fluid Dynamics (CFD) models employ Reynolds-Averaged Navier-Stokes (RANS) turbulence models and away from using Large Eddy Simulation (LES). Accordingly, this work was presented to compare the employing of RANS and LES turbulence models for such problems at low Reynolds numbers. Toward this objective, a complete 3D CFD model consisting of seven rows of tubes in flow direction is developed without using any symmetrical boundary conditions. The present study includes the impact of the Remax range (500 to 4500), for three surface relative roughnesses: ks/D of 0, 0.01, and 0.02. The local turbulence and heat transfer characteristics are discussed. The findings confirmed that the two proposed options for heat transfer enhancement succeeded in doubling it. LES is superior to RANS models in resolving a wide spectrum scale of flow eddies. The results are useful in designing more efficient heat exchangers, especially at low Reynolds number.*

*Keywords: Heat transfer; Tube bank; Reynolds-Averaged Navier-Stokes; Large Eddy Simulation; Pressure drop*

## 1. Introduction

The design of energy-efficient systems is essentially required for the energy-saving goals [1-4]. In engineering practice, cross flow over tube banks is frequently encountered in heat transfer apparatus such as steam generation in a furnace, condensers, and evaporators in refrigerators, power plants, air conditioners, and heat recovery systems. The flow of cross flow over a tube bank is characterized to be turbulent. As the pressure drops, the heat transfer coefficient ( $h$ ) for the tubes in the following rows rises because the first-row tubes act as a turbulence grid. However, the heat transmission coefficient stabilizes after the fourth or fifth row [5-6]. Its uneven distribution results in changing turbulent movements which can carry momentum, heat, and mass. These movements have a noteworthy impact on flow field velocity, temperature, and pressure distribution. The turbulent movements profile is three-dimensional (3D), unstable, and unsuitable medium, in which they are different from enormous Eddy sizes, which correspond to low-frequency fluctuations. Trivial eddies where dissipation occurs, correspond to high-frequency oscillations, the turbulent movements characterized by eddies of various sizes.

Therefore, two crucial aspects for researching turbulence are choosing the turbulence technique rather than the model, and the fact that 3D simulation is still the best way to explain such complicated flows. The turbulence technique should provide models "whose predictions are close to those of the equations" but are computationally easier than the Navier-Stokes equations. The first method statistically averages the Navier-Stokes equations which are known as Reynolds-Averaged Navier-Stokes (RANS). Large-eddy simulation (LES) is the second method. For the Navier-Stokes equations, LES uses a spatial averaging filter to recover large-scale velocity, pressure, and temperature structures and reduce their small-scale features. After modeling tiny-scale effects on enormous sizes only big-scale random motion is resolved. The third method, Direct Numerical Simulation (DNS), solves Navier-Stokes equations without turbulence. The complete spectrum of turbulence's spatial and temporal scales, from the lowest dissipative scales (Kolmogorov scales) to the integral scale, which is associated with the movements that contain most of the kinetic energy must be resolved. DNS is necessary for investigating complicated flow phenomena that need a lot of computer resources, but not for engineering calculations. LES outperforms RANS when large-scale features dominate flow behavior and unstable phenomena such as vortex shedding occur, particularly at lower Reynolds numbers. Though cheaper than DNS, LES calculations are expensive [7].

Many research efforts are devoted to enhancing the turbulence within cross-flow over tube banks while keeping an eye on the pressure drop. Splitter plates (SPs) may be positioned at the dragging edge of the tubes of a cross-flow heat exchanger to improve heat transmission. Due to their role as enlarged heat transfer surfaces and their ability to minimize pressure drop in cross-flow heat exchangers via the suppression of vortex shedding, the inclusion of such SPs significantly improves heat transfer [8]. Apelt et al., [9], pointed out that adding SPs to circular cylinders reduces drag independent of the Reynolds number. A Computational Fluid Dynamics (CFD) analysis was presented by Kwon and Choi, [10] to examine the effect of SP length on vortex shedding. Furthermore, the SP critical length required to completely stop the shedding was identified. The square cylinder was the subject of another CFD investigation by Park, [11], and the findings showed that the shorter SP was responsible for controlling the cylinder's downstream wake. The impact of putting SPs in a staggered tube bank in cross-flow with air, which consists of five rows of tubes in the flow direction, was exposed to experimental and CFD studies by Mangrulkar et al., [12]. They employed the RANS

technique and suggested utilizing the RNG  $k-\varepsilon$  turbulence model with such flow issues for SPs with a tube length-to-tube diameter ratio of one; the examined range of  $Re_{max}$  was 5,500-14,500. The findings demonstrated that the SP facility boosted the fluid flow's Nusselt number ( $Nu$ ) while decreasing pressure drop. Later, Mangrulkar et al., [13], published further research utilizing six rows of tubes arranged in the flow direction to examine various SP geometries. It was discovered that for the majority of patterns, the SPs with the geometrical parameters,  $L/D = 1.0$  and  $t/D = 0.20$  improved the  $Nu$  and decreased the overall pressure drop. The work of Mangrulkar et al., [12], was quantitatively enlarged by Elmekawy et al., [14], to add to the optimization of the SP thickness. The RANS RNG  $k-\varepsilon$  turbulence model was also used. According to their findings, the SPs should be thin to maintain the best heat exchanger performance.

Another proposed option for heat transfer augmentation is by roughing the associated surfaces, as this will increase turbulence. The surface roughness can be expressed as either the surface relative roughness,  $k_s/D$ , or the surface roughness height,  $k_s$ .  $D$  is the outer diameter of the tube, and  $k_s$  is the comparable roughness height of sand particles in millimeters [15]. The roughness conditions determine both the crucial Reynolds number ( $Re$ ) and the drag coefficient. The literature introduces numerous surface roughening techniques. Various approaches such as sandpaper [16-18], sand grain [19], arrays of rods [20-21], and regular configurations of pyramids [22-25] have been widely used. Different work such as that presented in [16, 20, 21, 22, 23, 25, 15] and computer-based studies [26-30] have looked at how roughness affects the thermal boundary layer and, the value of heat transfer coefficient  $h$  which represents the airflow around a cylinder in a circle. However, researchers use existing computational studies to explore the impact of roughness on a single cylinder in cross-flow to air. You may find further studies on the impact of roughness on pressure drops, velocity vectors, and lift and drag coefficients in Taylor et al. [31]. Here are detailed summaries of related work. Achenbach [16], Achenbach [22], and Achenbach and Heinecke [23] carried out numerous experiments to ascertain the impact of surface roughness on  $h$  and flow topology surrounding a circular cylinder. Achenbach [16] reported using the two-roughness approach, which involves warping sandpaper around the cylinder. Achenbach [22], and Achenbach and Heinecke [23], used regular pyramid layouts. The relative roughness ( $k_s/D$ ) ranged between  $1.1 \times 10^{-3}$  and  $9.0 \times 10^{-3}$ . Tetsu et al. [25] analyzed the local  $h$  and boundary layer temperature trends to determine how roughness affects natural convection for water flow through a vertical cylinder. Their results suggested that the roughness of the water's surface enhanced the rate of local heat transmission. The impact of  $k_s/D$  on the parameter  $h$  is the subject of studies [20, 24]. Kolár [24], claimed that rising tube roughness lowered the mean velocity, improved the friction factor, and decreased the value of  $h$ .

Al-Rubaiy [15], reviewed the literature to determine the unique and typical influences of the ratio, ( $k_s/D$ ). This ratio was modified from 0 to 0.00725 and the turbulence intensity varied from 2.2% to 9.7%. Results established that surface roughness was necessary to improve the thermal performance. Arenales et al., [18], investigated how surface roughness affected copper tubes in boiling water between 0.032 and 0.544 m. The discoveries showed that rough tubes increase the value of  $h$  by 1.5 times more than smooth ones. The incompressible flow through a rounded cylinder with ( $k_s/D = 0.5\%$ ) was quantitatively examined by Kawamura and Takami, [26]. No turbulence model was used; the Reynolds values varied from 1,000 to 100,000. At around  $Re = 20,000$ , the drag coefficient significantly decreased. This demonstrated that the crucial Reynolds number had been captured within their computational bounds. Our research team in Karali et al., [32] presented a CFD analysis on the

influence of surface roughness on heat transfer and pressure decrease in a staggered tube bank in cross-flow using air. This study benefits from a complete 3D CFD model without symmetrical boundary conditions. The tube bank has five rows of tubes facing airflow. The enlarged analysis includes  $Re_{max}$  changes between 5,000 and 100,000.  $k_s/D = 0$  (smooth), 0.01 (rough), and 0.02 (rough). As suggested by earlier studies: using the RANS RNG  $k-\varepsilon$  turbulence model [12-13]. The conclusions displayed that heat transfer surface roughness promotes heat transfer, and pressure drop increases somewhat. Improving surface roughness and including SPs doubled the heat transfer rate.

Regarding the use of LES turbulence models, there are limited CFD works from the literature that employ LES models for cross-flow over a single cylinder, rather than for cross-flow over virtually non-existent tube banks [33-39]. The following are some of these researches; Breuer, [33], numerically studied the turbulent flow past a circular cylinder at  $Re = 3900$  using (LES). The objective was to investigate numerical and modeling factors that affect the LES solution quality. Investigations were done into five separate schemes. No-slip boundary circumstances were utilized at solid walls due to the study's being limited to low Reynolds numbers. There are two separate subgrid-scale models are employed. LES calculations without subgrid-scale modeling were also done to illustrate the models' efficiency. The obtained results were compared to the experimental data for verification purposes. Rodi [34] presented using direct numerical simulations (DNS). The large-scale Eddy flow (LES) was flowing in a low-pressure turbine cascade with wakes routinely traveling down the cascade channel. The studied flow was through a surface-mounted rounded cylinder with a 2.5 height-to-diameter ratio. The results showed that DNS and LES can reliably predict engineering-relevant turbulent flows despite their high cost. In situations of unsteadiness, such as shedding, and large-scale structures, DNS is better than RANS techniques, and DNS has become a significant instrument for transition process study. LES was used by Sarkar [35] to study flow through a cylinder near a wall. To understand flow physics' insights into boundary layer-wake exchanges for three gap-to-diameter ratios. The current LES shows the shear layer's instability and the growth of small-scale eddies. CFD analysis was utilized by Afgan et al., [36] to study cross-flow over two heated infinite cylinders in an in-line arrangement. Using the dynamic Smagorinsky's non-isothermal LES model dependent on the cylinder diameter and free stream velocity, at a Reynolds number of 3,000. Two distinct Prandtl number ( $Pr$ ) values,  $Pr = 0.1$  and  $1.0$  were examined with a cylinder gap ratio of  $1.0 < L/D < 5.0$ . The upstream cylinder's average Nusselt number was discovered to be greater than the downstream one, which is their key discovery. Additionally, it was discovered that the maximal  $Nu$  is independent of the spacing ratio and is situated at the separation angle.

From the preceding discussions, it can be concluded that only a limited number of CFD models from the literature address the combined effects of surface roughness in tube banks in cross flow with air and the addition of SPs on heat transfer and pressure drop at low Reynolds numbers. Additionally, implementing full 3D simulations without applying symmetrical boundary conditions provides greater detail and aligns the simulation results more closely with experimental findings by modeling the problem as it occurs in practice. In the long run, this approach reduces the need for challenging experimental work. Moreover, almost no work has been found in the literature to discuss the same topic using LES turbulence models due to the highly intensive computational resources needed.

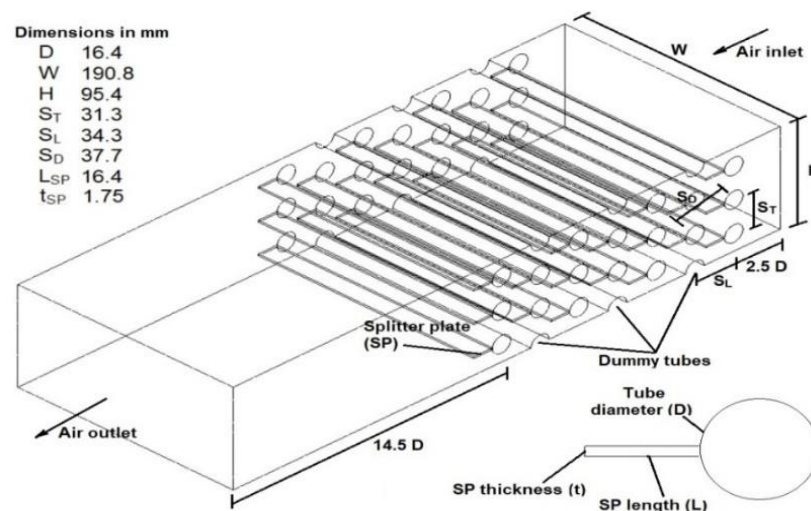
This paper aims to compare the performance of RANS and LES turbulence models in addressing challenges associated with low  $Re$  applications. The study seeks to provide deeper insights into the turbulent behavior of such problems. Another major focus of the study is to examine the local

turbulence and heat transfer characteristics in detail. To achieve this, the number of stream-wise tubes increased to seven. These critical considerations underscore the significance of the present study, which contributes to the design of more efficient heat exchangers, particularly for low Reynolds number conditions.

## 2. Numerical simulations

### 2.1. Geometric configuration

The numerical simulation for a staggered tube bank in cross-flow using air will be employed for this investigation. It comprises six half-dummy tubes to maintain the flow characteristics inside the arrangement, along with 18 thermally heated tubes. The transverse columns are three in a staggered layout, with seven rows in the streamwise direction. The used dimensions are found in Incropera et al., 2006 [5], which may be used with numerous devices,  $D = 16.4$  mm, 34.3 mm is the longitudinal pitch, 31.3 mm is the transverse pitch, and 37.7 mm is the diagonal pitch. The duct height ( $H = 95.4$  mm) is based on the previously mentioned measurements. The spanwise tube length is assumed to be 190.8 mm ( $W/H = 2$ ), and  $W$  is duct width. 18 rectangular splitter plates (SPs) are secured to each tube's trailing edge in the case of splitter plates; the SPs' length is ( $L_{SP} = D$ ) and their thickness is assumed to be 1.75 mm. The initial tube row is  $2D$  away, and the final tube row is assumed to be  $14D$  away from the end of the CFD domain. Ansys Design Modeler R18.0's numerical simulation for the case of SPs is shown in Figure 1 with all geometrical parameters.

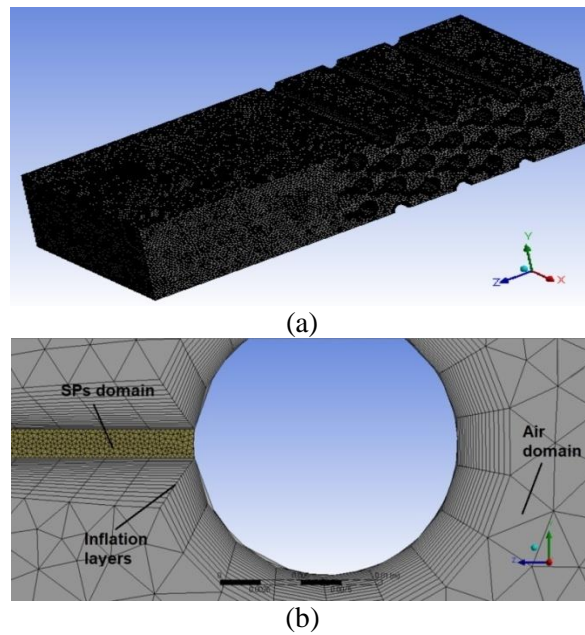


**Figure 1. Geometrical configuration for the case of SPs, showing the seven tube rows in a streamwise direction**

### 2.2. Meshing properties

ANSYS-ICEM Mesh R18.0 meshes the discretized solution domain with a fine mesh adjacent to all solid surfaces in the boundary layer regions and areas with significant gradients of the dependent variables. This method inflates such areas using 18 layers with a 1<sup>st</sup> layer of 0.08 mm thickness including 1.1 inflation rate. This guaranteed lower  $Y^+$  values for all situations examined. In the case of SPs, Figure 2 depicts the produced mesh in (a) an overall view and (b) a zoomed-in sight to highlight the inflating layers for both air and splitter plate domains. Another concern for creating the mesh

sometimes referred to as "mesh independence" is whether there are enough nodes and if the iterative solution procedure has workable convergence criteria. In the smooth case with SPs at  $Re_{max} = 2500$ , several meshes were used to demonstrate mesh independence. Additionally, the matching average Nusselt values were compared (to be explained later). The respective meshes carry different cell sizes for the air domain and the SP domain with 3.06 (5, 0.4 mm), 4.5 (4, 0.35mm), 6.4 (5, 0.3mm), 6.6 (4, 0.3 mm), 7.3 (3, 0.3 mm), 8.9 (2, 0.3 mm) million counted for the total number of nodes. It was determined that any number of nodes more than one of 6.6 million will provide very little marginal difference in  $Nu$ . The mesh with 7.3 million nodes was chosen throughout the whole study to provide a better understanding of the intricate structure of turbulence.



**Figure 2. Mesh properties (Ansys-ICEM R18.0): (a) overall view showing seven tube rows and (b) zoom-in view**

### 2.3. Methodology

The RANS and LES methodologies were employed in this study, using the ANSYS CFX R18.0 numerical tool. The discretization of limited volumes underlies this piece of software. Two domains may be distinguished in the case of tubes containing SPs: air-based fluid domain, and aluminum-based solid domain. The hot tube surface is described as no-slip walls with defined roughness which varies from:  $k_s/D = 0$  (smooth), to  $k_s/D = 0.02$  [15, 18, 26 and 32], and at a fixed surface temperature of 363 K. The SPs bases are also kept at 363 K and have the same surface roughness as the tube walls. While adiabatic wall boundary conditions refer to all other walls. The moving fluid intake velocity is calculated based on  $Re_{max}$  values of 500, 1500, 2500, 3500, and 4500 [32 and 36]. The air inlet temperature is 288 K. For all studied cases the RNG  $k-\epsilon$  turbulence model is applied as it was recommended by other investigators [12, 14, 32, 40, 41, 42, 43, and 44] to be the best RANS model that describes the current problem. While the LES turbulence model is tested for six cases namely: without SP and  $k_s/D = 0.01$  for  $Re_{max}$  of 2500 and 4500, without SP and  $k_s/D = 0.02$  for  $Re_{max}$  of 500 and 4500, and with SP and  $k_s/D = 0.01$  for  $Re_{max}$  of 3500, and rough ( $k_s/D = 0.02$ ) for  $Re_{max}$  of 4500. However, an initial test was conducted to check the flow type for the lowest  $Re_{max} = 500$ . Therefore, the laminar model was checked beside the RNG  $k-\epsilon$ , and results from the two models were compared

particularly based on the average  $Nu$  number, where the same methodology was used by Gorman et al. [44]. It was noted that there is a deviation of about 15 % between the results from the two models, which indicates that the turbulent flow type is prevailing even for the lowest  $Re_{max} = 500$ ; this can be attributed to the flow nature of such problem configuration with a staggered tube bank.

A residual mean square of  $10^{-6}$  and below was chosen as the primary solution convergence criteria for both techniques, RANS and LES. For the LES model, convergent statistics are ensured by simulating the instances for a significant time. The best convergence was evaluated during the first transient period. Statistics were typically gathered during intervals of roughly  $100 D/V_\infty$  time units. With a Courant number setting between 0.5 and 1, the number of loop iterations every shedding cycle is maintained at 10. The solution was operated on an Intel (R) Xeon (R) CPU E5-26700@ 2.6 x 2 GHZ 16 cores 32 GB RAM system in parallel local MPI.

For incompressible, single-phase, fully developed flow, the RANS RNG  $k-\varepsilon$  turbulence model, which incorporates the fundamental mass, momentum, and energy transfer equations, is presented in detail in; Wilcox, [7]; Stefanidis et al., [46]; and Karali et al., [32].

The mass and momentum equations of the LES for incompressible flow are expressed as [7, 35, and 36]:

$$\frac{\partial \bar{u}_i}{\partial x_i} = 0 \quad (1)$$

$$\frac{\partial \bar{u}_i}{\partial t} + \frac{\partial}{\partial x_j} (\bar{u}_i \bar{u}_j) = -\frac{1}{\rho} \frac{\partial p}{\partial x_i} + \frac{1}{Re} \nabla^2 \bar{u}_i - \frac{\partial \tau_{ij}}{\partial x_j} \quad (2)$$

where,  $\bar{u}_i$  denotes the velocity field and  $\tau_{ij} = \overline{u_i u_j} - \bar{u}_i \bar{u}_j$  is the residual stress tensor that is identified also as the subgrid-scale stress (SGS). The inducement of subgrid movements is included in the resolved LES using the model developed by Germano et al., [47] and altered by Lilly, [48].

## 2.4. Governing equations

The maximum fluid velocity across the tube bank is shown in Eq. 3 [42-43],

$$V_{max} = \left( \frac{S_T}{S_T - D} \right) V_\infty \text{ at } S_D > \frac{S_T + D}{2} \quad (3)$$

$D$  corresponds to the tube diameter,  $S_T$  and  $S_D$  are the tube bank's transversal pitch and diagonal pitch, respectively.

Eq. 4 allows for the computation of the  $Re_{max}$  based on  $V_{max}$ .

$$Re_{max} = \frac{\rho V_{max} D}{\mu} \quad (4)$$

$\rho$ , and  $\mu$  are corresponds to fluid density and dynamic viscosity coefficient, respectively.

Using Eq. 5, it is likely to determine the air side total heat transfer rate ( $Q_a$ ).

$$Q_a = \dot{m}_a c_p (T_{a,o} - T_{a,i}) \quad (5)$$

$\dot{m}_a$  is the air mass flow rate (computed after Eq. 6),  $C_p$  is the air-specific heat,  $T_{a,o}$  is outlet air temperature (evaluated from CFD findings), and  $T_{a,i}$  is inlet air temperature (288 K).

$$\dot{m}_a = \rho H W V_\infty \quad (6)$$

Where  $H$  and  $W$  are air duct height and width. Thus, the ( $h_{avg}$ ) is described in Eq. 7,

$$h_{avg} = \frac{Q_a}{A_s LMTD} \quad (7)$$

where,  $A_s$  is the total heat transfer surface area, and  $LMTD$  is computed from Eq. 8,

$$LMTD = \frac{(T_s - T_{a,i}) - (T_s - T_{a,o})}{\ln \left[ \frac{(T_s - T_{a,i})}{(T_s - T_{a,o})} \right]} \quad (8)$$

Where  $T_s$  is the hot surface temperature (363 K). And  $Nu_{avg}$  is attained from Eq. 9,

$$Nu_{avg} = \frac{h_{avg} D}{K} \quad (9)$$

where  $K$  corresponds to the air thermal conductivity.

One main point of interest to discuss here is obtaining the fluid properties, as it essentially influences the calculated results. The air properties are obtained using the CFX library at an air entry of 288 K. And then it was fed to the calculation equations under the assumption that the effects of changes in air temperature throughout the tube bank on air characteristics are insignificant [51-52].

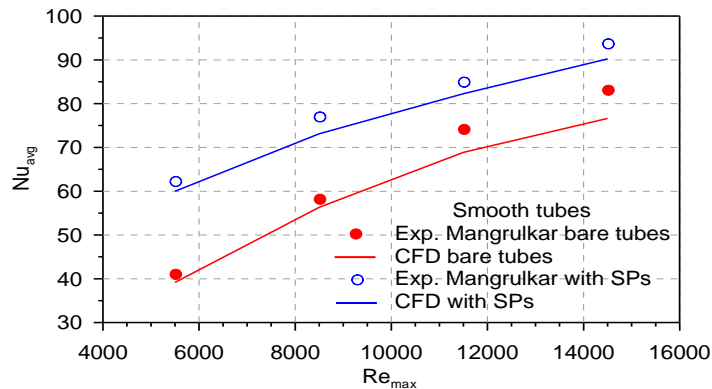
The total air pressure drop might be established from Eq. 10,

$$\Delta p = p_{a,i} - p_{a,o} \quad (10)$$

Where  $p_{a,i}$  and  $p_{a,o}$  are the air static pressures at the inlet and outflow, respectively.

## 2.5. Model validation with experimental work

As previously highlighted, the literature contains a limited number of experimental studies related to the current research issue. It is also restricted to discussing the feasibility of incorporating splitter plates at the trailing margins of a tube bank in cross-flow using airflow. Mangrulkar et al. [12] conducted experimental research in an open-channel wind tunnel. Their test rig facility has a rectangular air duct measuring 600 mm in length and 175 x 150 mm<sup>2</sup> in cross-section. The test portion consists of 13 examination tubes and 4 half-blank tubes organized in five rows with a staggered arrangement. A comparable test section is available for circular cylinders fitted with splitter plates. The provided working fluid, air, is introduced at 300 K. The longitudinal and transverse pitch ratios are consistently maintained at 1.75 and 2.0, respectively, for both arrangements. The range of  $Re$  chosen spans from 5500 to 14,500. A splitter plate length ( $L_{SP} = D$ ) is used. Consequently, the existing numerical model delineated in this research for smooth tubes is corroborated by the experimental findings of Mangrulkar et al. [12], with the results shown in Figure 3. As noticed in Figure 3, the validation performed throughout the whole range of investigated  $Re_{max}$  is reliable with the increasing pattern seen in the experimental findings.



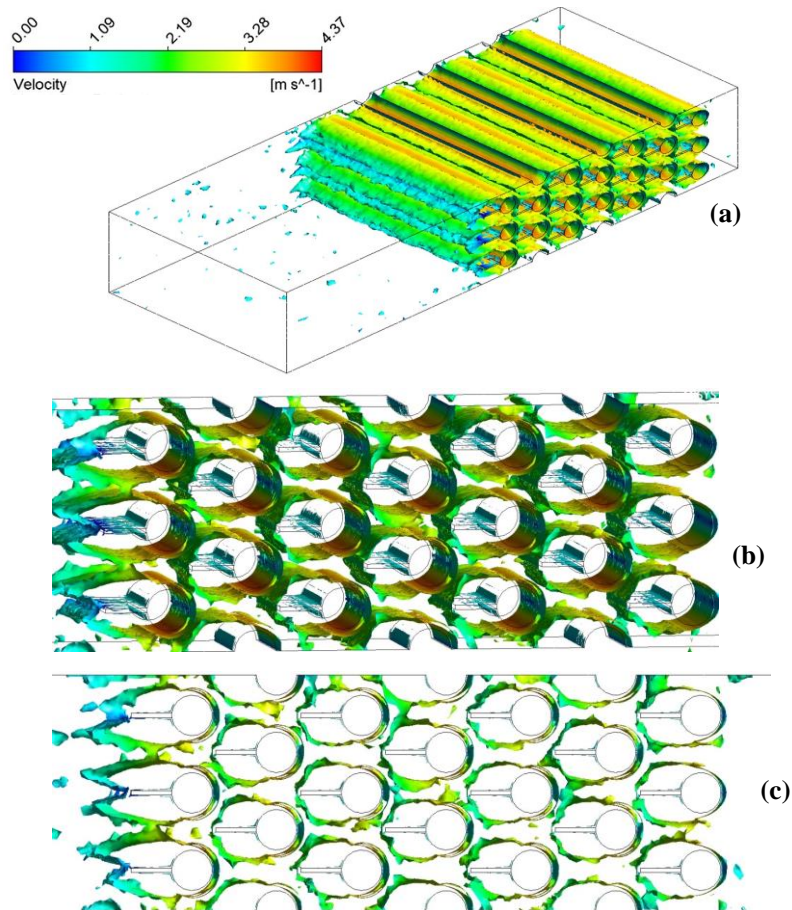
**Figure 3. CFD validation with experimental work for the baseline case (smooth tubes)**



### 3. Results

#### 3.1. Comparison between RANS and LES models

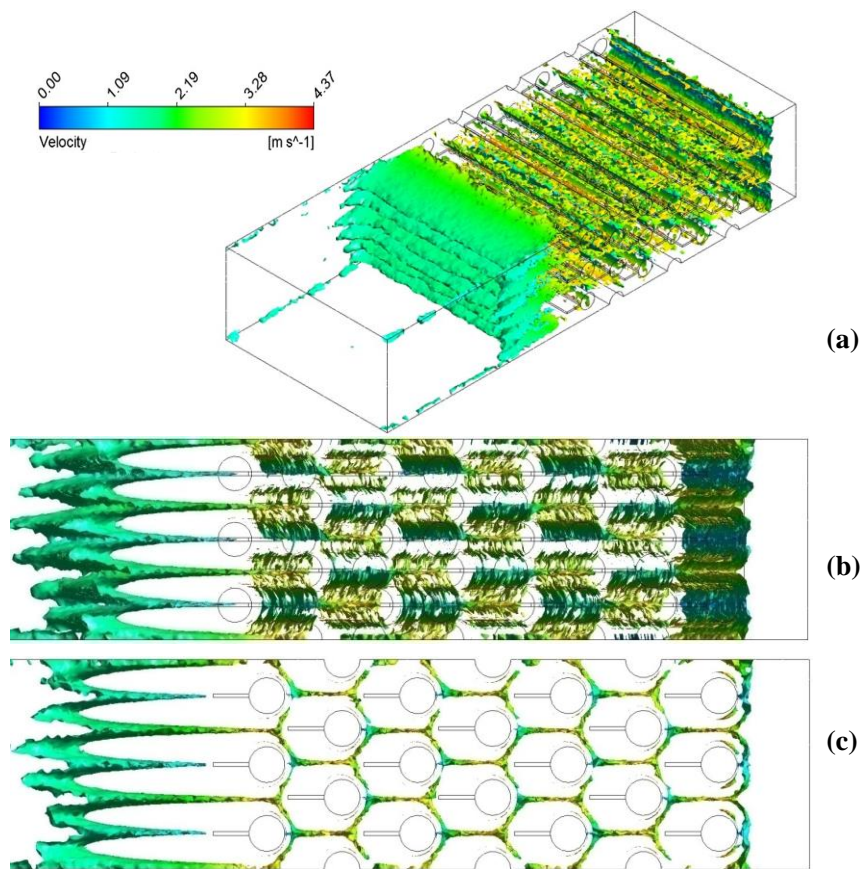
The main finding from this research is comparing the employing of the LES turbulence model with the RANS turbulence model within cross flow over a staggered tube bank problem. Comparison based on the iso-surfaces of immediate streamwise vorticity colored by the velocity magnitude for the case of with SPs and  $k_r/D = 0.01$  at  $Re_{max} = 3500$  is conducted between using LES (as shown in Figure 4), and RANS (as shown in Figure 5). For the two figures, three sub-images are drawn; (a) spanwise view (b) zoom-in view (c) streamwise view. The comparison between Figure 4 (a) and Figure 5 (a) shows the effectiveness of the LES model in resolving a broad spectrum of eddies over the RANS model. This can be confirmed by the excessively detailed flow vortices found in Figure 4 rather than that found in Figure 5 at the same vorticity level ( $\pm 0.01$ ). However, the high computational resources needed are the main obstacles to using such an LES model in real-world applications.



**Figure 4. Iso-surfaces of instantaneous streamwise vorticity ( $\pm 0.01$ ) highlighted by velocity magnitude for the case of with SPs rough 0.01 LES  $Re_{max} = 3500$  (a) spanwise view (b) zoom in view (c) streamwise view (total wall clock time = 20 days, computational time 1.25 days for 170 shedding cycles)**

In the prescribed issue with SPs, the flow topology is characterized by stagnation patterns in front of the tubes due to the upstream flow striking with the first row of tubes (Figs. 4 and 5). The flow then approaches the tube walls. Due to the curvature of the tube circumference, the separation then

becomes pronounced, and a vortex region forms behind the tubes. In contrast, installing SPs precludes vortex interference from the upper and lower tube sides in the downstream region compared to the absence of SPs. The two flow reattaching the SPs surfaces from the sides of adjacent tubes to one another. Compared to tubes without SPs, stratified flow with weaker vortex strength is produced by tubes with SPs. This would reduce the total pressure decline and energy losses in the tube bank. Such flow topologies for different cases; with and without installing SPs are similar to limited works from the literature [12, 14, 32, 34, 35, 36, and 53]. While the focus difference observed when comparing Figure 4 (c) to Figure 5 (c), is the flow wake nature after the last row (7<sup>th</sup> row). The flow wakes vortex region for the LES is shorter in length than found by the one using the RANS model and closer to the tubes trailing edges of the last row. Indeed the shorter vortex length can be appropriate for the physical predictions of such problems. However, a comparison based on the resulting actual amounts of heat transfer would be useful for more clarification of using the two models (see coming sections).

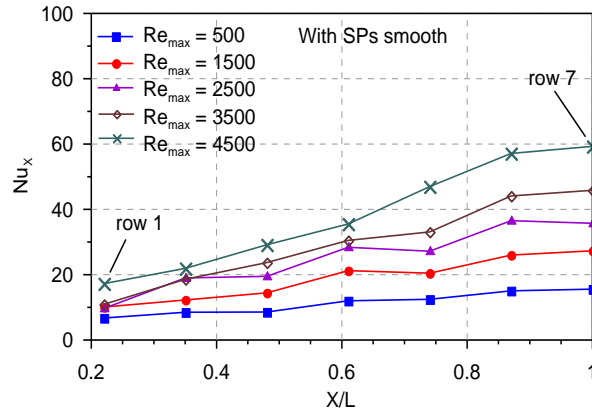


**Figure 5. Isosurfaces of instantaneous streamwise vorticity ( $\pm 0.01$ ) colored by velocity magnitude for the case of with SP srough 0.01 RANS  $Re_{max} = 3500$  (a) spanwise view (b) streamwise view (b) zoom in view (c) streamwise view (total wall clock time = 1.8 days, total computational time 2.75 hrs for 150 iterations)**

### 3.2. Local Nusselt number

At the beginning of results discussions from the present work, an interesting point to discuss is the change of the local  $Nu$  in a streamwise direction. The designed CFD model enables such a study with the favor of considering seven tube rows in the streamwise direction. The average  $Nu$  number is calculated from Eq. 8 but locally ( $Nu_x$ ) based on the intermediate temperatures between rows. This is

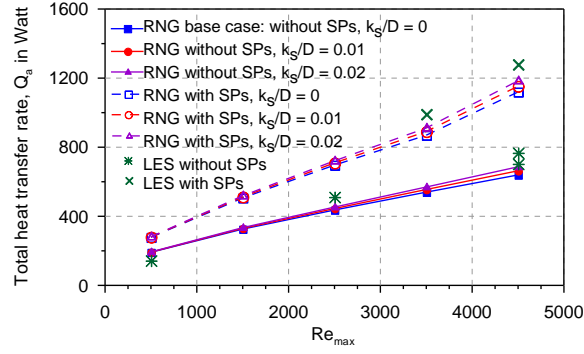
shown in Figure 6 based on all RANS results, where it is confirmed by the aforementioned knowledge that the  $(h)$  stabilizes with little change beyond the fourth or fifth row [4-6]. As shown in Figure 6, at any value of  $Re_{max}$  the average  $Nu$  value is improved by increasing the turbulence along with the streamwise direction till the fourth or fifth rows. Thereafter, no significant improvement is observed. As an example, at  $Re_{max} = 4500$ , the  $Nu$  improves by about 183 % from the 1<sup>st</sup> row to the 5<sup>th</sup> row, after that the  $Nu$  is slightly changed by 20 % till beyond the seventh row. This significant conclusion enhances the credibility of the model utilized in the present study.



**Figure 6. Local Nusselt number for the case of SPs smooth**

### 3.3 Heat transfer rate

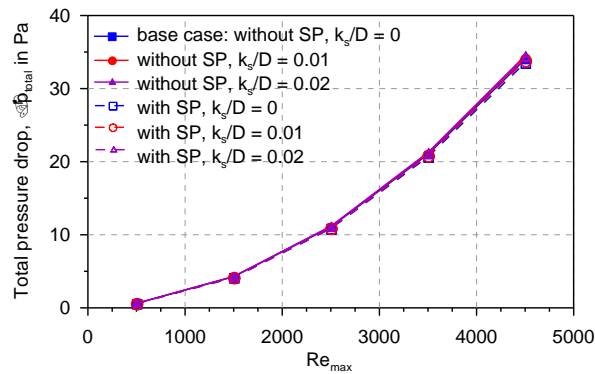
The quantity of heat carried beyond the tube bank under specified circumstances is more essential to researchers than the recommended boosting strategy. Figure 7 shows the overall heat transfer rate ( $Q_a$ ) versus  $Re_{max}$ . The talks use all RANS findings except the six LES points. In Figure 7, the total heat transmitted rises with  $Re_{max}$  in all circumstances. The air mass flow rate decreased the output air temperature. For a shift in  $Re_{max}$  from 500 to 4500, the basal case without SPs and homogeneous surfaces improves air heat transmission by 264%. Figure 7 shows that placing SPs as extended surfaces enhances heat transfer by 60% throughout the  $Re_{max}$  range compared to the basic scenario. Figure 7 shows that increasing heat transfer surface roughness promotes heat transmission. In the baseline scenario (without SPs), raising the heat transfer surface irregularity from  $k_s/D = 0$  to rugged ( $k_s/D = 0.01$ ) raises the overall heat transfer rate by 15%. However, increasing roughness from 0.01 to 0.02 has minimal effect. In addition to adding SPs, increasing the surface roughness ( $k_s/D$ ) irregularity from 0 to 0.02 raises the overall heat transfer rate by 80% across the examined parameter range. Thus, one important finding from the present study showed that the use of roughened surfaces alongside adding splitter plates increases the overall heat transmission rate throughout the  $Re_{max}$ 's spectrum. This emphasizes their potential to reduce the energy consumption of industrial heat exchangers and improve their efficiency. LES data supports these conclusions, while, RANS and LES findings are varied by about 15%.



**Figure 7. Changing heat transfer rate versus  $Re_{max}$  for all analyzed situations**

### 3.3. Pressure drop

Equation 10 illustrates tube bank pressure decrease. Figure 8 illustrates pressure decline versus  $Re_{max}$  for all scenarios examined. Figure 8 shows that increasing  $\dot{m}_a$  is the main parameter for improving total tube bank pressure drop, which is reliable with physical explanations and requires greater pumping power. The default pressure drops increase by 349% when the  $Re_{max}$  is adjusted from 500 to 4500 without SPs or smooth surfaces. While adding splitter plates as widened surfaces to the trailing ends of tubes reduced the overall pressure drop of such a heat exchanger by a small amount, adding SPs to the basic case reduces it by roughly 2% over the measured  $Re_{max}$  range. When different roughness levels are used, comparable results are obtained. This shows that increased irregularity may be used without fear of increased pressure loss, while heat transmission is improved.



**Figure 8. Total pressure drop changes along with  $Re_{max}$  for all studied situations**

### 3.4. Streamlines, velocity vectors, and turbulent kinetic energy

Figure 9 shows two instances of streamlines and velocity vectors at  $Re_{max} = 4500$ : (a) Smooth without SPs (base case) and rough with SPs ( $k_g/D = 0.02$ ). Case (a) Flow Topology: Upstream flow interacting with the 1<sup>st</sup> row of tubes causes stagnation patterns. Streamlines in the flow are forced up against the walls of the tube. Because the circumference of the tubes is curved, the separation becomes apparent, and a vortex zone emerges behind them. Streamlines at the conduit's apex and base combine to form a low-speed wake recirculation zone. Prolonging the wake zones to the last row produces expanded velocity zones for the subsequent tube rows. Figure 9 (b) shows the flow topology after adding SPs to tubes. Pipelines with SPs have equivalent upstream flow characteristics. SPs change the downstream flow topology. The SPs also reduce vortex interference from the top and lower tube walls.

The flow streamlines rejoin the SPs surfaces from neighboring tubes' borders. Stratified flow with lower vortex amplitude occurs in tubes having SPs. The overall tube bank pressure drops and energy losses decrease. This study's comprehensive 3D simulation without symmetrical borders is similar to previous researchers' flow topology [12 and 14].

The impact of flow topology on the enhancement of surface roughness can be attributed to the analysis of turbulent kinetic energy (TKE). TKE is frequently defined as the measurement of turbulence intensity in fluid flow [7]. The TKE spreading in the flow field is shown in Figure 10 for two chosen examples at  $Re_{max} = 4500$ : (a) without SPs and smooth, and (b) with SPs and rugged ( $k_s/D = 0.02$ ). In general, Figure 10 shows that the TKE intensity rises in the streamwise direction and attains its maximum downstream after the last row for all studied situations. Although this rise in TKE for the basic case (a) smooth without SPs is only visible in the last rows, it is considerable. From the second to the final row, the TKE for scenario (b) with SPs and ( $k_s/D = 0.02$ ) grows and is spread equally over the whole configuration. This is partly due to SPs' ability to prevent vortices from the top and lower tube sides from interacting, resulting in more stratified flow with minor eddies and vortex intensification. As a result, the employment of SPs and higher roughens becomes a feasible alternative for enhancing total turbulence inside the tube bank and, as a result, the heat transmitted.

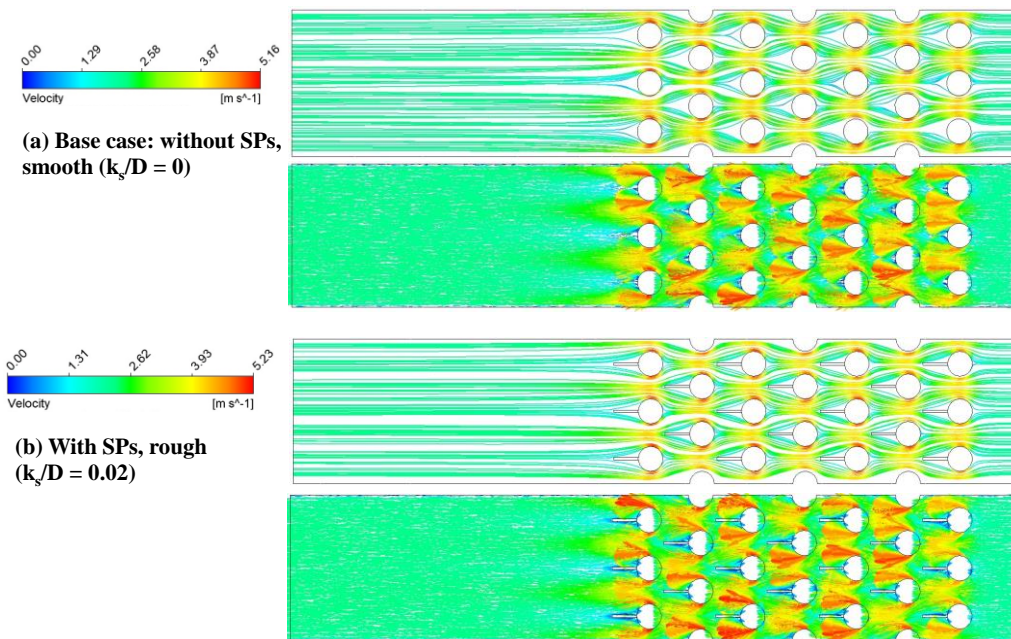


Figure 9. Streamlines and velocity vectors for selected two cases at  $Re_{max} = 4500$

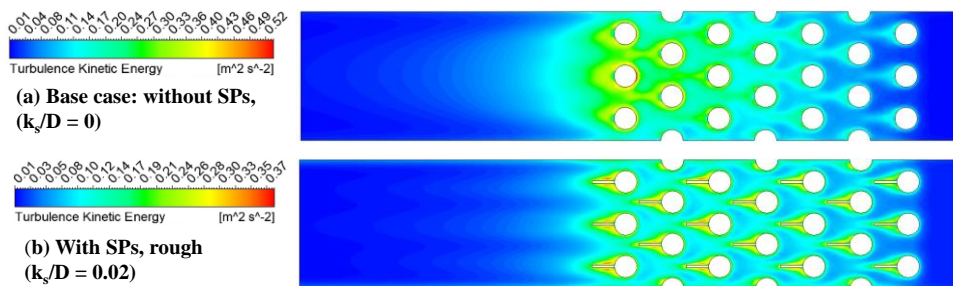
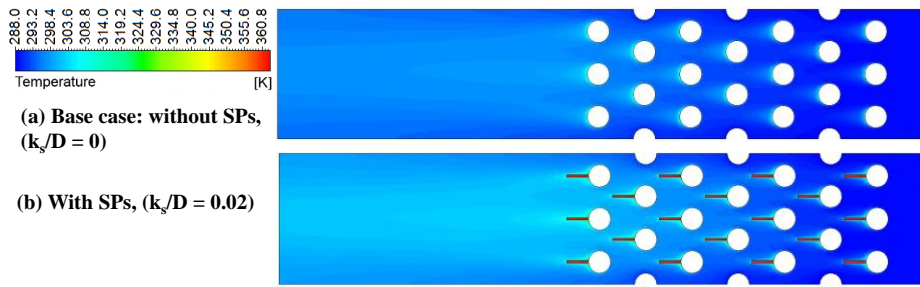


Figure 10. Turbulent kinetic energy for chosen two cases at  $Re_{max} = 4500$

### 3.5. Temperature contours

The importance of exhibiting temperature contours from the current CFD study originates from the fact that temperature variations according to the analyzed scenario resulted in a parameter that determines the improvement of heat transfer rate at a certain air mass flow rate, or  $Re_{max}$  (Eq. 5). Figure 11 shows temperature contours for two examples with  $Re_{max} = 4500$ ; the images are created with 100 contours to improve image resolution. The pictures show downstream air temperature rising steadily from the smooth case (a) to the rough example (d) ( $k_s/D = 0.02$ ). Unlike instance (a), example (b) bright blue tint is intense, indicating a consistent rise in downstream air temperature. The overall heat transfer enhancement comes from this downstream air temperature gain, which instantly boosts the temperature difference in Eq. (5).



**Figure 11. Temperature contours for selected cases at  $Re_{max} = 4500$**

### 4. Conclusions

Simulations utilizing comprehensive 3D RANS and LES methodologies, without the imposition of symmetrical boundary conditions, were conducted to analyze heat transfer and total pressure drop in a staggered tube bank configuration in cross-flow with air. Providing the option to increase the irregularity of the heat transfer surfaces in addition to integrating splitter plates (SPs) to the trailing margins of the tubing. The tube bank of 18 tubes with diameters of 16.4 mm, and longitudinal, transverse, and diagonal pitches of 34.3, 31.3, and 37.7 mm, respectively is investigated. The SP's length equals the tube's diameter ( $L_{SP}/D = 1$ ), and the thickness was assumed to be 1.75 mm. Six half-dummy tubes were inserted into the model to maintain the flow characteristics of the staggered configuration. The study's scope was expanded to examine the influence of  $Re_{max}$  modifications from 500 to 4500. While investigating the relative roughness of three surfaces ( $k_s/D = 0$  to 0.02) for the two cases with and without SPs. All cases were evaluated using the RANS model, but only six examples were designated for the LES model.

A comparative analysis based on the isosurfaces of instantaneous streamwise vorticity, colored by velocity magnitude, was performed to evaluate the performance of LES and RANS models. The findings from the present study highlight the superiority of LES in capturing a broader spectrum of eddies compared to RANS models. However, this advantage comes with the significant drawback of substantially higher computational resource requirements for LES.

Another key observation from the results is that the average local Nusselt number ( $Nu_x$ ) stabilizes with minimal variation beyond the fourth or fifth row. Furthermore, several additional conclusions can be drawn from the analysis: the total heat transfer rises as  $Re_{max}$  rises across all examined scenarios. Additionally, the exit air temperature decreased as the air mass flow rate rose.

The overall heat transfer rate contributed to the air augmented by roughly 264% for a change in  $Re_{max}$  from 500 to 4500 for the case without SPs and uniform surfaces (the basal scenario).

Installing SPs as extended surfaces significantly enhances the heat transfer rate by roughly 60% across the tested  $Re_{max}$  range compared to the base scenario. Additionally, it has been demonstrated that roughening the surfaces of heat transmission enhances the total heat transfer rate. When the effects of surface roughening and the addition of SPs are combined, the total heat transfer rate experiences a substantial improvement, highlighting the synergistic effect of these modifications in optimizing thermal performance.

The augmentation in heat transfer surface roughness, coupled with the incorporation of SPs, resulted in an impressive nearly 80% enhancement in the total heat transfer rate across the entire spectrum of measured parameters. Notably, increasing surface roughness, as opposed to using splitter plates, was found to further enhance the total heat transfer rate across the examined range of  $Re_{max}$  spectrum.

The findings from the LES research are likely to yield similar conclusions, with a notable 15% disparity observed between the results of the RANS and LES models. This discrepancy highlights the potential for further investigation into the underlying causes of turbulence dynamics. Future studies should focus on exploring additional turbulence-enhancing mechanisms to improve model accuracy and further bridge the gap between these two approaches.

The results from the current research, in addition to those available in existing literature, offer valuable insights into designing more efficient heat exchangers. These results contribute to enhancing performance and minimizing operational costs in industrial applications, particularly in systems operating at low Reynolds numbers. This improvement has the potential to optimize energy use, increase heat transfer efficiency, and reduce maintenance costs, making it highly relevant for industries seeking cost-effective and sustainable solutions.

## Nomenclature

### Symbols

$A$	area, [m <sup>2</sup> ]	$p$	static pressure, [Pa]
$D$	tube outer diameter, [m]	$Q$	fluid heat transfer rate, [W]
$H$	height of fluid duct, [m]	$S$	pitch, [m]
$h$	coefficient of convection heat transfer, [Wm <sup>-2</sup> K <sup>-1</sup> ]	$t$	thickness of splitter plate, [m]
$k$	turbulent kinetic energy, [J/kg]	$t$	time, [s]
$K$	thermal conductivity, [Wm <sup>-1</sup> K <sup>-1</sup> ]	$T$	temperature, [K]
$k_s$	height of surface roughness, [m]	$X$	axial advance in the streamwise direction, [m]
$k_s/D$	relative roughness, dimensionless	$u$	velocity vector, [m/s]
$L$	length of splitter plate, [m]	$\bar{u}_i$	filtered velocity field, [m/s]
$LMTD$	logarithmic mean temperature difference, [K]	$v$	velocity, [m/s]
$\dot{m}_a$	total air mass flow rate, [kg/s]	$W$	width of fluid duct, [m]
$N$	tubes count	$y^+$	mesh specification near the wall

### Dimensionless numbers

$Nu$  average Nusselt number

### Greek letters

$\rho$  density, [kg/m<sup>3</sup>]

$Pr$	Prandtl number	$\mu$	dynamic viscosity, [Pa.s]
$Re$	Reynolds number	$\varepsilon$	dissipation rate, [m <sup>2</sup> /s <sup>3</sup> ]
		$\Delta$	difference
		$\tau_{ij}$	residual stress tensor
<i>Abbreviations</i>			
$avg$	average	$max$	maximum
$CFD$	computational fluid dynamics	$RANS$	Reynolds average Navier-Stokes
$DNS$	direct numerical simulations	$SGS$	Subgrid-scale stress
$LES$	large eddy simulations	$TKE$	turbulent kinetic energy

#### *Subscripts*

$a$	air	$o$	outlet
$avg$	average	$s$	surface
$D$	diagonal	$SP$	splitter plate
$i$	inlet	$T$	transversal
$L$	longitudinal	$\infty$	upstream fluid
$max$	maximum		

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