# FIRST-PRINCIPLES STUDY ON THE MECHANICAL PROPERTIES OF Al<sub>1-x</sub>TM<sub>x</sub>P

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Using first-principles calculations, the mechanical properties of orthorhombic phase  $Al_{1-x}TM_xP$  (x = 0.0625, 0.125, 0.25; TM = Sc, Ti, V, Cr, Mn, Fe, Co, Ni, Cu, and Zn) crystals were studied. By analyzing the mechanical stability, it was found that  $Al_{0.75}Zn_{0.25}P$  is mechanical unstable, and the rest all mechanical stable. The mechanical properties of  $Al_{1-x}TM_xP$  were studied, including Bulk modulus, shear modulus, Young's modulus, Poisson's ration, ductility, Vickers hardness, and elastic anisotropy. It was found that  $Al_{0.75}Ni_{0.25}P$  has the largest Bulk modulus, the largest Poisson's ratio.  $Al_{0.75}Ni_{0.25}P$  has the smallest shear modulus, the smallest Young's modulus and the smallest Vickers hardness. The  $Al_{0.75}Ni_{0.25}P$ has the best ductility.  $Al_{0.75}Ni_{0.25}P$  and  $Al_{0.75}Cu_{0.25}P$  show strong elastic anisotropy, and the  $Al_{0.75}Cu_{0.25}P$  has the largest elastic anisotropy. Through the study of the mechanical properties of  $Al_{1-x}TM_xP$ , it was found that doping Ni into AlP is an effective means to tune its mechanical properties.

Key words: first-principles, mechanical stability, elastic modulus, Vickers hardness

# Introduction

Aluminum Phosphide (AIP) is an important III-V compound semiconductor material, which has been widely applied to functional materials [1, 2]. Doping transition metals into AIP is an effective method to improve its mechanical, magnetic, and optical properties [3-8]. Especially, 2-D AIP materials have more excellent and novel mechanical, magnetic and optical properties [9, 10]. After doping Mn or Cr into AIP,  $Al_{1-x}Mn_xP$  and  $Al_{1-x}Cr_xP$  have good magnetic properties with Curie temperature of above 300 K [11, 12]. After doping Mn into AIP, the shear modulus and Young's modulus of  $Al_{0.75}Mn_{0.25}P$  are less than those of AIP, but the Poisson's ratio and ductility are higher than those of AIP [13]. After doping Mn into AIP,  $Al_{0.875}Mn_{0.125}P$  has an absorption peak in the visible light range, and the characteristics of the absorption peak can be controlled by strain [11]. There are many studies on the magnetic and optical properties of semiconductor  $Al_{1-x}TM_xP$  (herby TM presents transition metal, rare earth, or non-metal), but few studies on its mechanical properties. In this work, the mechanical properties of  $Al_{1-x}TM_xP$  were systematically studied by doping transition metals into AIP, and the effects of transition metal element types and doping concentrations on the mechanical properties of  $Al_{1-x}TM_xP$  were studied.

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### **Computational methods**

In this work, the first-principles calculation [14-16] is used to study the properties of  $Al_{1-x}TM_xP$  (TM = Sc, Ti, V, Cr, Mn, Fe, Co, Ni, Cu, Zn; x = 0.0625, 0.125, 0.25) through the density functional theory (DFT) [17] using a plane-wave pseudopotential method as implemented in the Cambridge Sequential Total Energy Package (CASTEP) code [18, 19]. The Generalized Gradient Approximation (GGA) [20] within the Perdew, Burke, and Ernzerhof (PBE) scheme [21] is used to obtain the exchange-correlation potential. To ensure calculation precision, we employ the plane-wave energy cutoff of 400 eV, and the Brillouin-zone sampling mesh parameters for the *k*-point set of  $2 \times 2 \times 5$ . The other parameters use the default settings of ultra-fine accuracy.

The zinc blende (*zb*) AlP with space group *F*-43*m* has an experimental lattice constant of 0.5421 nm, the Al an P atom in which are located at positions (0,0,0) and (0.25,0.25,0.25), respectively. In this work,  $Al_{0.9375}TM_{0.0625}P$  compound were obtained by substituting one Al atom with one TM atom in a  $1\times1\times1$  Al<sub>3</sub>TM<sub>1</sub>P<sub>4</sub> supercell models as shown in fig. 1(a). The Al<sub>0.875</sub>TM<sub>0.125</sub>P compound were obtained by substituting one Al atom with one TM atom in a  $2\times1\times1$  Al<sub>7</sub>TM<sub>1</sub>P<sub>8</sub> supercell models as shown in fig. 1(b). The Al<sub>0.75</sub>TM<sub>0.25</sub>P compound were obtained by substituting one Al atom with one TM atom in a  $1\times1\times1$  Al<sub>3</sub>TM<sub>1</sub>P<sub>16</sub> supercell models as shown in fig. 1(c).



Figure 1. (a) The supercell models of  $Al_{0.9375}TM_{0.0625}P$ , (b) the supercell models of  $Al_{0.75}TM_{0.125}P$ , and (c) the supercell models of  $Al_{0.75}TM_{0.25}P$ 

### **Results and discussion**

### Elastic constants and mechanical stability

Elastic constants of crystals provide a link between mechanical and dynamical behaviors, they are also important information concerning the elastic response of a crystal to an external pressure. Elastic constants are important parameters to describe mechanical properties of solids. This elastic matrix has size  $6\times 6$  and it is symmetric. The elastic constants,  $C_{ij}$ , for orthorhombic  $Al_{1-x}TM_xP$  supercell predicated by GGA method. According to the elastic constants, it is found that  $Al_{1-x}TM_xP$  belongs to orthorhombic crystal. The mechanical stabilities of crystal structure under isotropic pressure can be determined by the criteria of independent elastic constants,  $C_{ij}$ . For an orthorhombic crystal, there independent components as shown in the following equation [22, 23]:

#### 2278

$$C_{ii} > 0$$

$$C_{11} + C_{22} - 2C_{12} > 0$$

$$C_{11} + C_{33} - 2C_{13} > 0$$

$$C_{22} + C_{33} - 2C_{23} > 0$$

$$C_{11} + C_{22} + C_{33} + 2(C_{12} + C_{13} + C_{23}) > 0$$
(1)

According to the criteria, except for  $Al_{0.75}Zn_{0.25}P$ , all  $Al_{1-x}TM_xP$  is mechanically stable at ambient pressure. Therefore,  $Al_{0.75}Zn_{0.25}P$  will not be studied when studying the mechanical properties of  $Al_{1-x}TM_xP$ .

# Elastic modulus

The elastic modulus of polycrystalline is interconnected to the elastic constants of single crystals. Generally speaking, elastic properties of polycrystalline have greater practical significance than single crystal. Polycrystalline elastic properties are properties by bulk modulus, *B*, shear modulus, *G*, Young's modulus, *E*, and Poisson's ration,  $\mu$ . There are two models to evaluate the modulus: the Voigt method and Reuss method, which provide the upper and lower bounds of the polycrystalline elastic modulus, respectively. For different crystalline systems, the bulk modulus and shear modulus according to Voigt can be expressed [24, 25]:

$$B_{\rm v} = \frac{C_{11} + C_{22} + C_{33} + 2(C_{12} + C_{13} + C_{23})}{9} \tag{2}$$

$$G_{\rm v} = \frac{C_{11} + C_{22} + C_{33} - C_{12} - C_{13} - C_{23}}{15} + \frac{C_{44} + C_{55} + C_{66}}{5} \tag{3}$$

and by Reuss that:

$$B_{\rm R} = \frac{1}{S_{11} + S_{22} + S_{33} + 2(S_{12} + S_{13} + S_{23})} \tag{4}$$

$$G_{\rm R} = \frac{15}{4(S_{11} + S_{22} + S_{33}) + 3(S_{44} + S_{55} + S_{66}) - 4(S_{12} + S_{13} + S_{23})}$$
(5)

The bulk modulus and shear modulus can be obtained by the Voigt-Reuss-Hill method. The arithmetic average of Voigt and Reuss bounds is known as the Voigt-Reuss-Hill average, which is regarded as the best estimate for the theoretical value of polycrystalline elastic modulus:

$$B = \frac{B_{\rm V} + B_{\rm R}}{2} \tag{6}$$

$$G = \frac{G_{\rm V} + G_{\rm R}}{2} \tag{7}$$

The Young's modulus and Poisson's ratio can be computed based on the above values by:

$$E = \frac{9BG}{3B+G} \tag{8}$$

$$\mu = \frac{3B - 2G}{6B + 2G} \tag{9}$$

where B, G, E, and  $\mu$  of Al<sub>1-x</sub>TM<sub>x</sub>P are calculated according to eqs. (2)-(9). The calculation results are shown in fig. 2.



Figure 2. (a) The bulk modulus of  $Al_{1-x}TM_xP$ , (b) the shear modulus of  $Al_{1-x}TM_xP$ , (c) the Young's modulus of  $Al_{1-x}TM_xP$ , and (d) the Poisson's ration of  $Al_{1-x}TM_xP$ 

The bulk modulus *B* of Al<sub>1-x</sub>TM<sub>x</sub>Pis shown in fig. 2(a). The dash line denotes the bulk modulus *B* of the pure AlP. After doping TM into AlP, except Al<sub>0.75</sub>Ni<sub>0.25</sub>P, the bulk modulus *B* of Al<sub>1-x</sub>TM<sub>x</sub> is decreased. The bulk modulus of Al<sub>0.75</sub>Ni<sub>0.25</sub>P is the largest (85.94 GPa) and the bulk modulus of Al<sub>0.75</sub>Mn<sub>0.25</sub>P is the smallest (66.33 GPa).

The *G* of  $Al_{1-x}TM_xP$  is shown in fig. 2(b). The dash line denotes the *G* of the pure AlP. After doping TM into AlP, the shear modulus *G* of  $Al_{1-x}TM_x$  is decreased. The shear modulus of  $Al_{0.9375}Mn_{0.0625}P$  is the largest (45.14 GPa) and the shear modulus of  $Al_{0.75}Ni_{0.25}P$  is the smallest (21.34 GPa).

The Young's modulus *E* of  $Al_{1-x}TM_xP$  is shown in fig. 2(c). The dash line denotes the Young's modulus *E* of the pure AlP. After doping TM into AlP, the Young's modulus of all  $Al_{1-x}TM_xP$  is decreased. The Young's modulus of  $Al_{0.9375}Mn_{0.0625}P$  is the largest (113.52 GPa) and the Young's modulus of  $Al_{0.75}Ni_{0.25}P$  is the smallest (59.13 GPa).

The Poisson's ratio  $\mu$  of Al<sub>1-x</sub>TM<sub>x</sub>P is shown in fig. 2(d). The dash line denotes the Poisson's ratio  $\mu$  of the pure AlP. After doping TM into AlP, the Poisson's ratio of all Al<sub>1-x</sub>TM<sub>x</sub>P is decrease. The Poisson's ratio of Al<sub>0.75</sub>Ni<sub>0.25</sub>P is the largest (0.39) and the Poisson's ratio of Al<sub>0.875</sub>Mn<sub>0.125</sub>P is the smallest (0.25).

### Vickers hardness and ductility

The hardness of a material is the intrinsic resistance to deformation when a force is applied. Currently, a formal theoretical definition of hardness is still a challenge for material scientists. The hardness of a material is related to the elastic and plastic properties, there have been some semi-empirical model developed to predict the hardness of materials. Chen *et al.* [26] proposed a model to predict the hardness of polycrystalline materials and bulk metallic glassed based on the Pugh's modulus ration (k = G/B) and the shear modulus:

$$H_{\rm V} = 1.887k^{1.171}G^{0.591} \tag{10}$$

where  $H_V$  denotes the Vickers hardness.

The ration of B/G can be used to estimate the ductility or brittleness of materials [27], since a high (low) value is associated with ductility(brittleness), and the critical value is about 1.75.

$$D = \frac{B}{G} \tag{11}$$

The  $H_V$  and B/G of Al<sub>1-x</sub>TM<sub>x</sub>P are calculated according to eqs. (10) and (11). The calculation results are shown in fig. 3.



Figure 3. (a) The H<sub>V</sub> of Al<sub>1-x</sub>TM<sub>x</sub>P and (b) the B/G of Al<sub>1-x</sub>TM<sub>x</sub>P

The Vickers hardness  $H_V$  of Al<sub>1-x</sub>TM<sub>x</sub>P is shown in fig. 3(a). The dash line denotes the Vickers hardness  $H_V$  of the pure AlP. After doping TM into AlP, the Vickers hardness of all Al<sub>1-x</sub>TM<sub>x</sub>P are decreases. The Vickers hardness of Al<sub>0.9375</sub>Mn<sub>0.0625</sub>P is the largest (9.45 GPa) and the Vickers hardness of Al<sub>0.75</sub>Ni<sub>0.25</sub>P is the smallest (2.25 GPa).

The B/G of  $Al_{1-x}TM_xP$  is shown in fig. 3(b). The dash line denotes the B/G of the pure AIP. After doping TM into AIP, the ductility of all  $Al_{1-x}TM_xP$  are creases. The ductility of  $Al_{0.75}Ni_{0.25}P$  is the largest (4.03) and the ductility of  $Al_{0.875}Mn_{0.125}P$  is the smallest (1.70).

### Elastic anisotropy

Several methods have been developed [27] to estimate he elastic anisotropy of compound. The bulk modulus anisotropy,  $A_B$ , shear modulus anisotropy,  $A_G$ , Young's modulus anisotropy,  $A_{\rm E}$ , universal elastic anisotropy index,  $A_{\rm U}$ , and for a crystal with orthorhombic symmetry can be determined:

$$A_{\rm B} = \frac{B_{\rm V} - B_{\rm R}}{B_{\rm V} + B_{\rm R}}$$

$$A_{\rm G} = \frac{G_{\rm V} - G_{\rm R}}{G_{\rm V} + G_{\rm R}}$$

$$A_{\rm E} = \frac{E_{\rm V} - E_{\rm R}}{E_{\rm V} + E_{\rm R}}$$

$$A_{\rm U} = 5\frac{G_{\rm V}}{G_{\rm R}} + \frac{B_{\rm V}}{B_{\rm R}} - 6$$
(12)

Similar to the definitions of  $B_V$ ,  $B_R$ ,  $G_V$ , and  $G_R$ ,  $E_V$  and  $E_R$  are the lower and upper bounds of Young's modulus in the in the Voigt and Reuss approximations, respectively.  $E_V$ and  $E_R$  are different from  $B_V$ ,  $B_R$ ,  $G_V$ , and  $G_R$ . they have no analytical solution and can only obtain numerical solution. The 3-D surface constructions of Young's modulus, E, for orthorhombic system is calculated by [27]:

$$\frac{1}{E} = S_{11}l_1^4 + S_{22}l_2^4 + S_{33}l_3^4 + (2S_{12} + S_{66})l_1^2l_2^2 + (2S_{13} + S_{55})l_1^2l_3^2 + (2S_{23} + S_{44})l_2^2l_3^2$$
(13)

According to eq. (13), the value of Young's modulus, E, along any direction in 3-D space can be obtained, and its maximum value,  $E_V$ , and minimum values,  $E_R$ , can be further obtained.

The zero value of anisotropic index ( $A_B$ ,  $A_G$ ,  $A_E$ ,  $A_U$ ) indicates that the crystal is isotropic. A high value of anisotropic index ( $A_B$ ,  $A_G$ ,  $A_E$ ,  $A_U$ ) means that the crystal structure has highly anisotropic elastic properties. The  $A_B$ ,  $A_G$ ,  $A_E$  and  $A_U$  of  $A_{1-x}TM_xP$  are calculated according to eqs. (12) and (13). The calculation results are shown in fig. 4.

The bulk modulus anisotropy  $A_B$  of  $Al_{1-x}TM_xP$  is shown in fig. 4(a). The dash line denotes the  $A_B$  of the pure AlP. After doping TM into AlP, the bulk modulus anisotropy of  $Al_{1-x}TM_xP$  are increased slightly. The bulk modulus anisotropy of  $Al_{1-x}TM_xP$  is very small, almost approach zero. The bulk modulus anisotropy of  $Al_{0.75}Cu_{0.25}P$  is the largest (2.39%).

The  $A_G$  of  $Al_{1-x}TM_xP$  is shown in fig. 4(b). The dash line denotes the  $A_G$  of the pure AlP. After doping TM into AlP, the shear modulus anisotropy of  $Al_{1-x}TM_xP$  are decreases except for  $Al_{0.75}Ni_{0.25}P$  and  $Al_{0.75}Cu_{0.25}P$ . The shear modulus anisotropy of  $Al_{0.75}Cu_{0.25}P$  is the largest (31.33%) and the shear modulus anisotropy of  $Al_{0.75}Sc_{0.25}P$  is the smallest (2.29%).

The  $A_E$  of  $Al_{1-x}TM_xP$  is shown in fig. 4(c). The dash line denotes the  $A_E$  of the pure AlP. After doping TM into AlP, the Young's modulus anisotropy of most  $Al_{1-x}TM_xP$  are creases. The Young's modulus anisotropy of  $Al_{0.75}Cu_{0.25}P$  is the largest (69.94%) and the Young's modulus anisotropy of  $Al_{0.75}Sc_{0.25}P$  is the smallest (22.15%).

The  $A_U$  of  $Al_{1-x}TM_xP$  is shown in fig. 4(d). The dash line denotes the  $A_U$  of the pure AlP. After doping TM into AlP, the universal elastic anisotropy index of most  $Al_{1-x}TM_xP$  are creases. The universal elastic anisotropy of  $Al_{0.75}Cu_{0.25}P$  is the largest (4.61) and the universal elastic anisotropy of  $Al_{0.75}Sc_{0.25}P$  is the smallest (0.24).



Figure 4. (a) The bulk modulus anisotropy factors of  $Al_{1-x}TM_xP$ , (b) the shear modulus anisotropy factors of  $Al_{1-x}TM_xP$ , and (c) the universal elastic anisotropy factors of  $Al_{1-x}TM_xP$ 

Based on the comprehensive analysis of four elastic anisotropy factors,  $Al_{0.75}Cu_{0.25}P$  has the largest elastic anisotropy value. Except  $Al_{0.75}Ni_{0.25}P$  and  $Al_{0.75}Cu_{0.25}P$ , the elastic anisotropy of  $Al_{1-x}TM_xP$  is insensitive to dope concentration.

# Conclusion

In this work, based on the first-principles calculations, mechanical properties of  $Al_{1-x}TM_xP$  (x = 0.0625, 0.125, 0.25; TM = Sc, Ti, V, Cr, Mn, Fe, Co, Ni, Cu, and Zn) crystal have studied in the orthorhombic phase. By analyzing the mechanical stability, it is found that  $Al_{0.75}Zn_{0.25}P$  is mechanically unstable, and the rest all mechanically stable. It is found that  $Al_{0.75}Ni_{0.25}P$  has the largest bulk modulus, the largest Poisson's ratio.  $Al_{0.75}Ni_{0.25}P$  has the smallest shear modulus, the smallest Young's modulus and the smallest Vickers hardness. The  $Al_{0.75}Ni_{0.25}P$  has the best ductility.  $Al_{0.75}Ni_{0.25}P$  and  $Al_{0.75}Cu_{0.25}P$  show strong elastic anisotropy, and the  $Al_{0.75}Cu_{0.25}P$  has the largest elastic anisotropy. Through the study of the mechanical properties of  $Al_{1-x}TM_xP$ , it is found that doping Ni in AlP is an effective means to tune its mechanical properties. The present method can be extended to study the TM-doped nanofiber properties [28, 29] by the electrospinning technology or the bubble electrospinning [30-35].

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