

## INVESTIGATION OF THE MILLER CYCLE ON THE PERFORMANCE AND EMISSION IN A NATURAL GAS-DIESEL DUAL-FUEL MARINE ENGINE BY USING TWO ZONE COMBUSTION MODEL

by

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*Compared to the standard cycle, the Miller cycle decreases the cylinder maximum combustion temperature which can effectively reduce  $NO_x$  emissions. In this paper, a 0-D two-zone combustion model is used to establish the simulation model of a marine dual-fuel engine, which is calibrated according to the test report under different loads. Due to the high emissions under part load, the Miller cycle (early intake valve closing method) is used for optimization. By analyzing the cylinder pressure, temperature, heat release rate, and  $NO_x$  emissions under different cases, it can be found that the effective working volume and thermal efficiency decrease with the advance of intake valve closing and improve with the increase of the geometric compression ratio. In all optimization cases, the  $NO_x$  emissions and fuel consumption are reduced by 72% and 0.1%, respectively, by increasing the geometric compression ratio to 14 and the intake valve closing timing to 510 °CA (the reference top dead center is 360 °CA). The simulation results show that the early intake valve closing Miller cycle can effectively reduce the  $NO_x$  emissions and cylinder peak pressure.*

**Key words:** Miller cycle, dual-fuel engine, 0-D two-zone combustion model, reduce  $NO_x$  emission, geometric compression ratio

### Introduction

With the implementation of IMO Tier III emission requirements, more stringent requirements are imposed on the marine engines  $NO_x$  emissions [1]. Current technologies for reducing  $NO_x$  emissions mainly include exhaust gas re-circulation (EGR) [2], exhaust gas selective catalytic reduction [3], electronically controlled fuel injection technology [4], Miller cycle [5] and so on. In addition, natural gas-diesel dual-fuel engines are considered to be a more attractive solution due to higher natural gas reserves and lower emissions [6-8]. Combined with the Miller cycle,  $NO_x$  emission in dual-fuel engine can be further reduced [9, 10]. The Miller cycle reduces the effective working volume of the cylinder by changing the intake valve closing timing such that the effective compression ratio is less than the expansion ratio. The Miller cycle reduces the maximum cylinder combustion temperature and thus reduces emissions [11]. Wang *et al.* [12] used the late intake valve closing to achieve the Miller cycle in reducing gasoline engine emissions. The characteristics of the Otto cycle and the Miller cycle were compared. The results show that the Miller cycle reduces  $NO_x$  emissions by reducing the in-cylinder combustion temperature. Mikalsen *et al.* [13] studied the feasibility of a small

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natural gas engine for cogeneration applications, and the Miller cycle can improve fuel efficiency [13]. Gonca and Sahin [14] used the Miller cycle and intake humidification method on a supercharged Diesel engine. The experimental results show that the Miller cycle combined with intake humidification can effectively reduce  $\text{NO}_x$  emissions and it is better than use the Miller cycle alone. Tavakoli *et al.* [15] applied the Miller cycle to a lean-burn natural gas engine and analyzed the performance and emission characteristics of a four-stroke supercharged gas engine using a finite volume method. The results show that the late intake valve closing improves engine performance, but the peak pressure and temperature variation in the cylinder is not significant. Yan *et al.* [16] studied Miller's optimization of the combustion and performance of a stoichiometric natural gas engine. Through thermodynamic analysis, as the geometric compression ratio increases, the potential for higher thermal efficiency increases. Kayadelen *et al.* [17] and Gonca *et al.* [18] used a two-zone combustion model to apply the Miller cycle to a Diesel engine and compared it to a conventional Diesel engine. The 0-D two-zone combustion has the advantages of simple model modeling and fast calculation speed. It is not inferior to the quasi-dimensional or 3-D model in the optimization and improvement of the internal combustion engine [19]. Since there is no variable valve timing system in the original engine, the purpose of this paper is to discuss the feasibility of Miller cycle application in marine low-speed engines. The model is built by a 0-D two-zone combustion model, and the Miller cycle is achieved by the early intake valve closing method. The optimal operating point for engine emissions and performance at low loads was investigated by Miller cycle and varying geometric compression ratios. This paper explores the feasibility of applying the Miller cycle for the dual-fuel engine and provides a reasonable solution for the marine medium-speed engine to reduce emissions at part load and meet the Tier III standard.

## Miller cycle principle and modeling theory

### Miller cycle principle

The effective compression ratio of the Miller cycle intake stroke is less than the expansion ratio of the exhaust stroke compared to the standard cycle. There are three ways to achieve the Miller cycle: Install a rotary valve between the intake manifold and the intake valve to control the amount of intake air. This is the so-called intake control rotary valve

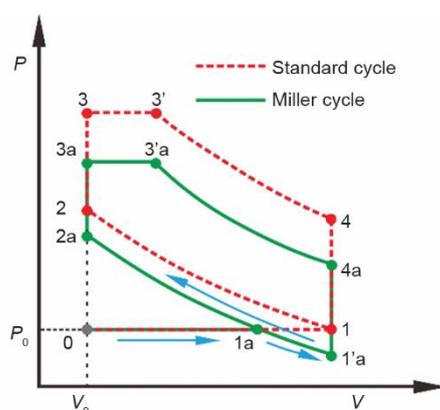


Figure 1. Comparison of standard and Miller cycles

(ICRV) [20]; The intake valve is closed before the end of the intake stroke, *i. e.* the early intake valve closing (EIVC) [21] and; Keep the intake valve open during a portion of the compression stroke to exclude some of the gas and reduce the effective compression ratio, *i. e.* the late intake valve closing (LIVC) [16, 22].

Figure 1 shows a comparison of the EIVC Miller cycle and the standard cycle [23]. The diesel engine standard cycle curve is 0-1-2-3-3'-4-1-0. The workflow is: 1 – the intake stroke is 0-1, and when the piston moves to BDC, the intake valve closes. 2 – Compression stroke is 1-2. 3 – Combustion and expansion stroke is 2-3-3'-4. 4 – exhaust stroke is 4-1-0. The Miller cycle curve is 0-1a-1'a-2a-3a-3'a-4a-1-0. The workflow is: 1 – the intake

stroke is 0-1a, and when the piston moves to 1a, the intake valve closes and the piston still moves down from 1a to 1'a. Since the intake valve is closed, the air in the cylinder is lowered due to expansion, and the temperature is lower than the standard cycle. 2 – Compression stroke is 1'a-2a. The cylinder pressure at the end of compression is lower than the standard cycle, and the air temperature in the cylinder is also lower than the standard cycle. 3 – Combustion and expansion stroke is 2a-3a-3'a-4a. Its highest cylinder pressure is lower than the standard cycle, and the maximum combustion temperature in the cylinder is also lower than the standard cycle. 4 – Exhaust stroke is 4a-1-0. Compared with the standard cycle, the Miller cycle reduces the maximum combustion temperature in the cylinder, so that the NO<sub>x</sub> generation region is avoided during the combustion process to achieve the purpose of reducing NO<sub>x</sub>.

### Modeling theory

In this paper, the 0-D two-zone combustion model is used to calculate emissions and performance [19]. The cylinder is divided into a burned zone and an unburned zone at the start of injection. The fuel in the unburned zone reacts with the air to become part of the burned zone. The energy conservation equation in the cylinder can be expressed:

$$\frac{dU}{d\phi} = \frac{d(mu)}{d\phi} = \frac{dQ_f}{d\phi} + h_s \frac{dm_s}{d\phi} - h_e \frac{dm_e}{d\phi} - \frac{dQ_w}{d\phi} - p \frac{dV}{d\phi} \quad (1)$$

where  $u$  is specific internal energy and the temperature changes in the cylinder is:

$$\frac{dT}{d\phi} = \frac{1}{mc_v} \left( \frac{dQ_f}{d\phi} + h_s \frac{dm_s}{d\phi} - h_e \frac{dm_e}{d\phi} - \frac{dQ_w}{d\phi} - p \frac{dV_b}{d\phi} - u \frac{dm}{d\phi} \right) \quad (2)$$

Ignore valve leakage and by-pass flow, assuming the total mass in the cylinder is constant, the total mass of the burned zone and the unburned zone is:

$$m = m_u + m_b \quad (3)$$

The total volume of the burned zone and the unburned zone is equal to the total volume of the cylinder:

$$V = V_u + V_b \quad (4)$$

The research engine's piston pin in this paper has no offset, so the total cylinder volume function is:

$$\frac{dV}{d\phi} = \frac{d\pi}{8} B^2 S \sin \phi \left[ 1 + \varepsilon \frac{\cos \phi}{\sqrt{1 - \varepsilon^2 \sin^2 \phi}} \right] \quad (5)$$

In each region, assuming the ideal gas and the same pressure, the equation of state are:

$$\begin{cases} pV_u = m_u R_u T_u \\ pV_b = m_b R_b T_b \end{cases} \quad (6)$$

where the  $R_u$  and  $R_b$  are the gas constant of unburned and burned zone.

The energy equations for each region are [24]:

$$\begin{cases} \frac{d(m_u u_u)}{d\phi} = -p \frac{dV_u}{d\phi} + \frac{dQ_{w,u}}{d\phi} - h_u \frac{dm_u}{d\phi} \\ \frac{d(m_b u_b)}{d\phi} = -p \frac{dV_b}{d\phi} + \frac{dQ_{w,b}}{d\phi} + h_u \frac{dm_u}{d\phi} \end{cases} \quad (7)$$

The Wiebe function is used to describe the heat release rate [25]:

$$\frac{dx}{d\phi} = a \frac{m+1}{\phi_b} \left( \frac{\phi - \phi_0}{\phi_b} \right)^m \exp \left[ -a \left( \frac{\phi - \phi_0}{\phi_b} \right)^{m+1} \right] \quad (8)$$

where the  $m$  is the combustion shape factor,  $a$  – the Wiebe constant, and 6.908 for complete combustion.

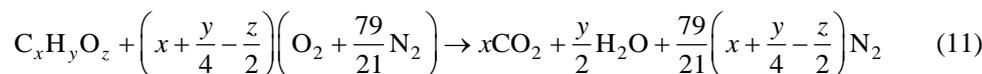
For the combustion duration and ignition delay,  $id$ , at variable working condition [26]:

$$\phi_b = \phi_{b,ref} \left( \frac{s_{ref}}{s} \right)^{2/3} \left( \frac{n}{n_{ref}} \frac{f_{ref}}{f} \right)^{1/3} \quad (9)$$

$$id = id_{ref} \left( \frac{s_{ref}}{s} \frac{f}{f_{ref}} \right)^{2/3} \left( \frac{n}{n_{ref}} \right)^{1/3} \quad (10)$$

where  $s$ ,  $id$ , and  $f$  mean laminar flame speed, ignition delay, and piston to head distance at ignition timing, respectively. The laminar flame velocity is a function of in-cylinder conditions, air-fuel ratio, and residual gas mole fraction and it is obtained by looking up the table [27].

The natural gas is mixed with air at the intake port and the diesel directly injected into the cylinder. It is assumed that the diesel fuel is instantaneously atomized and uniformly mixed in the cylinder, and the formed mixture is evenly distributed in the cylinder. The injected diesel fuel evaporates immediately and there is no liquid fuel zone in the cylinder. The chemical reaction equation is simplified to:



The heat release of diesel accounts for less than 2% of the total heat release, so the mass-flow of diesel is converted to natural gas mass according to the heat release of diesel.

For the species thermodynamic parameters, the working gas in the cylinder is assumed to be ideal gas and the single gas parameters is [28]:

$$c_p = a_1 + a_2 \theta + a_3 \theta^2 + \dots + a_k \theta^{k-1} \dots + a_m \theta^m \quad (12)$$

$$\theta = \frac{(T - T_{shift})}{T_{norm}}$$

where  $a_i$  and  $\theta$  are the fitting coefficient of constant pressure specific heat and normalized temperature, respectively. The typical values of  $T_{shift}$  and  $T_{norm}$  are 0 K and 1000 K, respectively [29].

Heat transfer is ongoing at all stages of the engine. It is generally believed that the combustion phase is dominated by intense radiation, while the other phases are dominated by convection and heat conduction. The Newton formula is used to describe the heat transfer model in the 0-D model [30]:

$$\frac{dQ_w}{d\phi} = \sum_{i=1}^3 \alpha_w A_i (T_z - T_{wi}) \quad (13)$$

The Woschni [31] heat transfer model converts complex heat dissipation calculations into heat transfer coefficient calculations:

$$\alpha_w = C_0 D^{-0.2} p^{0.8} T^{-0.53} \left[ C_1 C_m + C_2 \cdot \frac{V_D T_1}{P_1 V_1} (p - p_{mot}) \right]^{0.8} \quad (14)$$

For the part load:

$$\begin{cases} \alpha_w = C_0 D^{-0.2} p^{0.8} T^{-0.53} (C_1 C_m + I)^{0.8} \\ I = \max \left[ C_2 \frac{V_D T_1}{P_1 V_1} (p - p_{mot}), 2C_1 C_m \left( \frac{V_C}{V} \right)^2 \text{IMEP}^{-0.2} \right] \end{cases} \quad (15)$$

Table 1 shows the coefficient  $C_1$  and  $C_2$  [24].

When the turbocharger works in a stable condition, the compressor power consumption is theoretically equal to the available output power of the turbine. To simplify the model, the total mechanical losses are borne by the exhaust turbine. The exhaust turbine output power is:

$$\dot{W}_t = \dot{m}_t c_p T_e \eta_t (1 - w_t^\gamma) \quad (16)$$

The input power of the compressor is:

$$\dot{W}_c = \dot{m}_c c_p T_a \frac{1}{\eta_c} (w_c^\gamma - 1) \quad (17)$$

The compressor outlet temperature is:

$$T_c = T_a \left[ 1 + \frac{1}{\eta_c} (w_c^\gamma - 1) \right] \quad (18)$$

The turbocharger outlet temperature is very high and requires an intercooler for cooling. The intercooler can be simplified to the throttling process, the intercooler outlet temperature is:

$$T_i = T_c - \eta_s (T_c - T_{wi}) \quad (19)$$

**Table 1. Coefficients  $C_1$  and  $C_2$  for Woschni's correlation**

Phase	$C_1$ [-]	$C_2$ [ $\text{ms}^{-1}\text{K}$ ]
Intake-exhaust	6.18	0
Compression	2.28	0
Combustion-expansion	2.28	$3.24 \times 10^{-3}$

In general, NO in Diesel engine emissions is derived from the reaction of nitrogen and oxygen at high temperature. According to the extended Zeldovich mechanism [32], the three-step NO formation reaction is as follows, and the reaction constants are shown in tab. 2.

$$k = A_A T^{B_A} e^{\frac{E_A}{T}} \quad (20)$$

**Table 2. Reactions of NO formation**

No. reaction		Forward/backward		
		$A_A$ [ $\text{cm}^3 \text{mol}^{-1}\text{s}^{-1}$ ]	$B_A$	$E_A$ [ $\text{kcal mol}^{-1}\text{K}^{-1}$ ]
1	$\text{N}_2 + \text{O} \leftrightarrow \text{NO} + \text{N}$	$7.6 \times 10^{13} / 1.6 \times 10^{13}$	0/0	-38000/0
2	$\text{O}_2 + \text{N} \leftrightarrow \text{NO} + \text{O}$	$6.4 \times 10^9 / 1.5 \times 10^9$	0/0	-3150/-19500
3	$\text{OH} + \text{N} \leftrightarrow \text{NO} + \text{H}$	$4.1 \times 10^{13} / 2 \times 10^{14}$	0/0	0/-23650

The NO generation rate is [33]:

$$\left\{ \begin{array}{l} \frac{d[\text{NO}]}{dt} = \frac{2R_1(1-\alpha^2)}{1+\alpha R_1} \\ \alpha = \frac{[\text{NO}]}{[\text{NO}]_e} \end{array} \right. \quad (21)$$

The  $[\ ]_e$  represents the concentration at equilibrium. The other constants in the equation are expressed as:

$$\left\{ \begin{array}{l} R_1 = k_{+1}[\text{N}_2]_e[\text{O}]_e = k_{-1}[\text{NO}]_e[\text{N}]_e \\ R_2 = k_{+2}[\text{O}_2]_e[\text{N}]_e = k_{-2}[\text{NO}]_e[\text{O}]_e \\ R_3 = k_{+3}[\text{OH}]_e[\text{N}]_e = k_{-3}[\text{NO}]_e[\text{H}]_e \end{array} \right. \quad (22)$$

## Model verification and Miller cycle cases

### Model verification

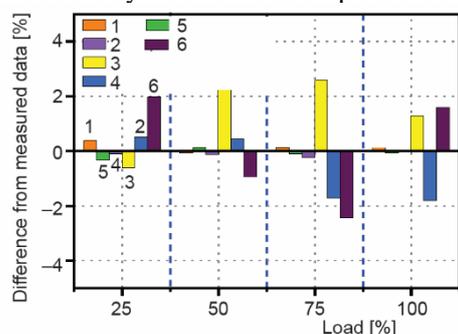
All measurements of this engine are from the official workshop test report certified by CCS (China Classification Society) and LR (Lloyd's Register of Shipping). The basic parameters of the engine are shown in tab. 3.

Figure 2 shows the comparison between the calculated and the measured error under different loads. It can be seen that the error of all the main parameters is within 3%, and the fuel consumption and power error are within 1%, which indicate that the simulation model can meet the calculation requirements. Figure 3

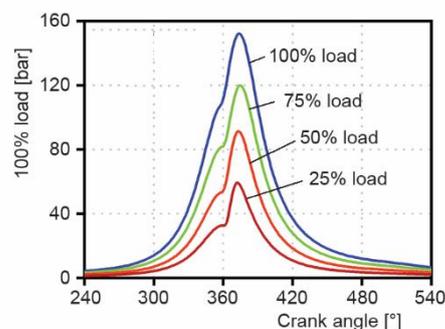
**Table 3. Specification of dual-fuel engine (100% load)**

Engine parameters	Specifications
Cylinder number [-]	8
Cylinder diameter [mm]	510
Stroke [mm]	600
Compression ratio [-]	13.3
Power [kW]	8000
Speed [rpm]	514
Fire order [-]	1-4-7-6-8-5-2-3

shows the cylinder simulation pressure under different loads.



**Figure 2. Comparison of model and measurement;**  
 1 – power, 2 – intake manifold pressure, 3 – exhaust manifold pressure, 4 – peak pressure, 5 – BSFC, 6 – NO<sub>x</sub>



**Figure 3. Comparison of cylinder pressure simulation**

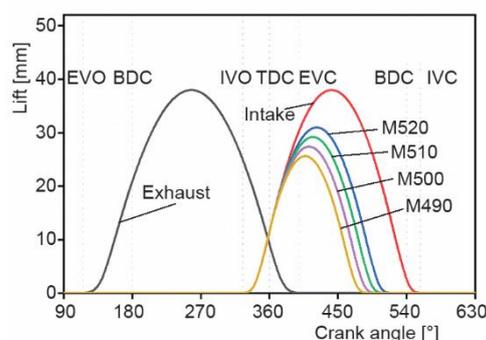
Considering the maximum NO<sub>x</sub> emission flow rate at 50% load, therefore, the Miller cycle is used to optimize the 50% load condition. Table 4 shows the error between the simulation and measure values at 50% load.

**Table 4. Comparison of experimental main parameters with calculated one at 50% load**

Main Parameters	Measured	Calculated	Error
Power [kW]	4004	4000	-0.10%
BSFC converted [gk <sup>-1</sup> W <sup>-1</sup> h <sup>-1</sup> ]	172.1	172.4	0.17%
Intake manifold temperature [K]	321	321.2	0.06%
Intake manifold pressure [bar]	111	112.6	1.44%
Intake manifold mass flow [kgs <sup>-1</sup> ]	6.91	6.92	0.14%
Exhaust manifold temperature [K]	789	789.7	0.09%
Exhaust manifold pressure [bar]	1.526	1.56	2.23%
NO <sub>x</sub> flow [kgh <sup>-1</sup> ]	18.77	18.51	-1.39%
Peak pressure [bar]	91	91.3	0.33%

*Model cycle calculation cases*

Compared with the LIVC Miller cycle, the EIVC Miller cycle pumping loss is lower, so the EIVC method is chosen in this paper to achieve the Miller cycle [21]. Figure 4 shows the comparison of different Miller cycle valve timing. The original valve closing time is 558 °CA (Base), and the EIVC Miller cycle are 520 °CA (M520), 510 °CA (M510), 500 °CA (M500), and 490 °CA (M490). To maintain the approximate intake air mass and temperature, two-stage turbocharger or more efficient turbocharger and more efficient intercooler or greater



**Figure 4. Valve lift curves**

cooling water flow are needed in the actual test. However, it can directly improve the efficiency of the compressor and intercooler in the simulation research to meet the same intake mass-flow and temperature requirement, which will not affect the study of the Miller cycle.

Table 5 shows the initial conditions of the calculation. The intake air temperature remains the same due to the same load. The values in the table are the averages of the final simulation after stabilization. In all the cases, it is assumed that the temperature of the cylinder head, the cylinder wall and the piston crown are the same under different cases.

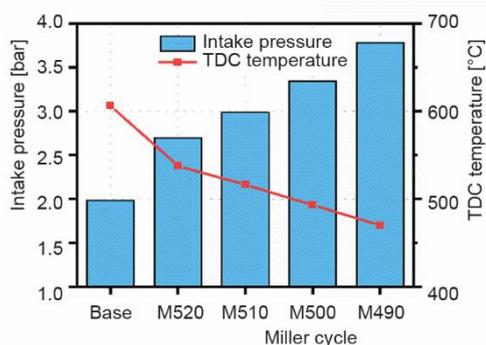
**Table 5. The initial conditions in the calculation**

50% load	Base	M520	M510	M500	M490
Intake Pressure [bar]	1.98	2.70	2.99	3.34	3.78
Intake temperature [K]	321.2	320.6	320.5	320.6	321.0
Exhaust pressure [bar]	1.56	2.05	2.26	2.51	2.83
Exhaust temperature [K]	789.7	795.3	800.3	807.1	817.9
Head temperature [K]	783				
Liner temperature [K]	723 at TDC and 623 at BDC				
Piston temperature [K]	873				

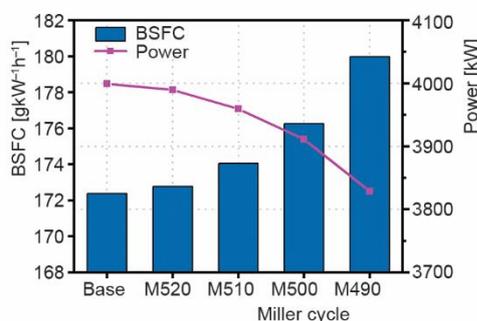
## Results and discussion

Figure 5 shows the comparison of the intake pressure and the TDC. It can be seen from the figure, with the advance of IVC angle, the intake pressure increases. Since the intake valve is closed early, the in-cylinder charge expands and cools down. The effective compression stroke is shortened and the effective compression ratio is reduced. The temperature at TDC decreases with the earlier angle of the IVC, and the M490 calculation simulation is reduced by 136 K compared with the original engine. This conclusion is consistent with previous studies [34].

Figure 6 shows the comparison of power and fuel consumption. With the advance of IVC angle, the effective compression stroke becomes shorter. The lower effective working volumes results in lower thermal efficiency, higher fuel consumption and lower power.



**Figure 5. Comparison of intake pressure and TDC temperature**



**Figure 6. Comparison of power and fuel consumption**

Figure 7 shows the comparison of NO<sub>x</sub> emissions and exhaust manifold temperature. The NO<sub>x</sub> emissions is affected by combustion temperature in cylinder. The cylinder charge

expands and cools with the advance of IVC angle which leads to the lower effective compression ratio [35]. This causes the temperature of the entire combustion process to decrease, which greatly deteriorates the  $\text{NO}_x$  generation conditions and greatly reduces the  $\text{NO}_x$  emissions. The increase in the intake pressure causes the enthalpy of the charge in the cylinder to increase, resulting in an increase in the exhaust gas temperature.

Figure 8 shows the trend of pressure and heat release rate in the cylinder. With the advance of IVC angle, the intake pressure increases, which delays the start of combustion, increases the duration of combustion and moves the heat release center back. This coincides with previous works [21]. This causes the cylinder peak pressure to shift back and the peak pressure to drop, which reduces the geometric load on the engine and helps to improve the reliability of the engine.

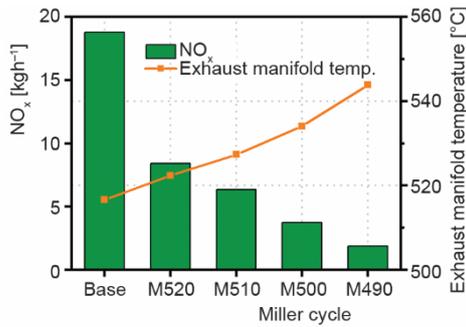


Figure 7. Comparison of  $\text{NO}_x$  emissions and exhaust manifold temperature

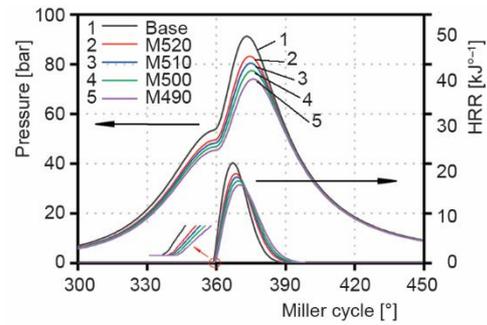


Figure 8. Comparison of cylinder pressure and heat release rate

Figure 9 shows the 3-D diagram of fuel consumption, compression ratio and  $\text{NO}_x$  emissions. With the advance of IVC angle, the effective compression ratio decreases, which leads to the lower thermal efficiency, higher fuel consumption and lower power consumption [36]. This problem can be effectively solved by increasing the geometric compression ratio. The geometric compression ratio and Miller cycle have opposite effects on engine  $\text{NO}_x$  emissions. The higher geometric compression ratio causes the higher cylinder maximum combustion temperature and increases the  $\text{NO}_x$  emissions. In all optimization cases, the fuel consumption of the M520-CR13.3, M510-CR14 and M500-CR15 cases are almost the same, but the  $\text{NO}_x$  emissions of M500-CR15 case is lower. For all the M490 calculation cases, the fuel consumption cannot be improved by increasing the geometric compression ratio, so the M490 cases is not recommended in actual conditions. Considering the affection of the geometric compression ratio on the Miller cycle, the M510-14 case is the best solution for economics and emissions.

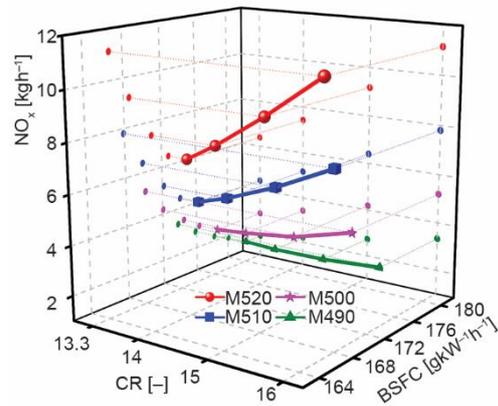


Figure 9. The 3-D plot of fuel consumption, compression ratio and  $\text{NO}_x$  emissions

## Conclusions

The previous analyses show that the Miller cycle has a greater advantage in terms of emissions than the standard cycle. Compared with the original engine, in the M520 case, the  $\text{NO}_x$  emission is reduced by 65.5%, the fuel consumption is only increased by 0.24%, and the power is reduced by 0.27%. The earlier angle of the IVC can further reduce the  $\text{NO}_x$  emissions. In the M490 case, the  $\text{NO}_x$  emissions is reduced by 89%, but the combustion efficiency is also decreased. However, the Miller cycle increases the fuel consumption and reduces the power, in the original Miller cycle, the fuel consumption and power are improved by changing the compression ratio. In order to achieve less fuel consumption and higher power, the geometric compression is increased to the Miller cycle calculation cases. Considering  $\text{NO}_x$  emissions and fuel consumption, the  $\text{NO}_x$  emissions and fuel consumption are reduced by 72% and 0.1% respectively in the M510-CR14 case. In this paper, the early intake valve closing method of the Miller cycle is used to optimize the  $\text{NO}_x$  emissions. However, the earlier angle of the IVC needs higher intake pressure and requires a better turbocharger which limits the application of the Miller cycle. This paper provides a reasonable solution for dual-fuel engines operating on partial load and an important reference for reducing emissions optimization and meeting Tier III standards.

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## Nomenclature

$A$  – heat transfer area, [ $\text{m}^2$ ]

$B$  – bore, [m]

$C_m$  – mean piston velocity, [ $\text{m s}^{-1}$ ]

$c_p$  – constant pressure specific heat, [ $\text{kJkg}^{-1}\text{K}^{-1}$ ]

$c_v$  – constant volume specific heat, [ $\text{kJkg}^{-1}\text{K}^{-1}$ ]

$h$  – specific enthalpy, [ $\text{kJkg}^{-1}$ ]

$m$  – mass, [kg]

$n$  – specific internal energy, [ $\text{kJkg}^{-1}$ ]

$p$  – pressure, [bar]

$Q$  – heat loss, [ $\text{kJkg}^{-1}$ ]

$S$  – stroke, [m]

$T$  – temperature, [K]

$U$  – internal energy, [kJ]

$V$  – volume, [ $\text{m}^3$ ]

$\dot{W}$  – work output or input, [kJ]

$w$  – pressure ratio, [–]

$x$  – burn fraction, [–]

### Greek symbols

$\varepsilon$  – ratio of half stroke to rod length, [–]

$\phi$  – crank angle, [ $^\circ$ ]

$\gamma$  – compression ratio index, [–]

$\eta$  – efficiency, [–]

### Subscripts

0 – start of combustion

1 – state at intake valve closing

a – ambient

b – burned zone

c – compressor

e – exhaust state

f – fuel (include diesel and natural gas)

i – intercooler

mot – engine motored

s – intake state

t – turbine

u – unburned zone

z – in cylinder state parameters

w – cylinder walls

### Acronyms

BSFC – brake specific fuel consumption, [ $\text{gK}^{-1}\text{W}^{-1}\text{h}^{-1}$ ]

CA – crank angle

HRR – heat release rate

IMEP – indicated mean effective pressure, [bar]

IVC – intake valve closing

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