

## AN EXERGY-RATIONAL DISTRICT ENERGY MODEL FOR 100% RENEWABLE CITIES WITH DISTANCE LIMITATIONS

by

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*While moving towards 100% renewable district energy systems at low temperatures, the exergy of the district energy may decrease below the pumping exergy requirement, which eliminates the benefits of using low-exergy renewables. Because such a possibility may not be revealed by the First Law, an exergy-based holistic model for district energy systems was developed. Four tiers, namely renewable energy resources, energy conversion and storage, main district network, and the low-exergy district are identified. Each tier is indexed to the optimum plant-to-district distance for maximum exergy-based performance with minimum CO<sub>2</sub> emissions responsibility. This model further optimizes the temperature peaking with heat pumps versus HVAC equipment oversizing and determines the optimum mix of renewables. Three alternatives of conveying and distributing exergy to the district were considered, namely: electricity only, electricity and heat with or without temperature peaking or equipment oversizing, and electricity, heat, and cold. Comparisons showed that the choice primarily depends upon the district size, district-to-plant distance, climatic conditions, local availability of RES, optimum supply temperature, and thermal condition of the buildings. Another algorithm optimizes the thermal insulation thickness in terms of equipment oversizing and temperature-peaking.*

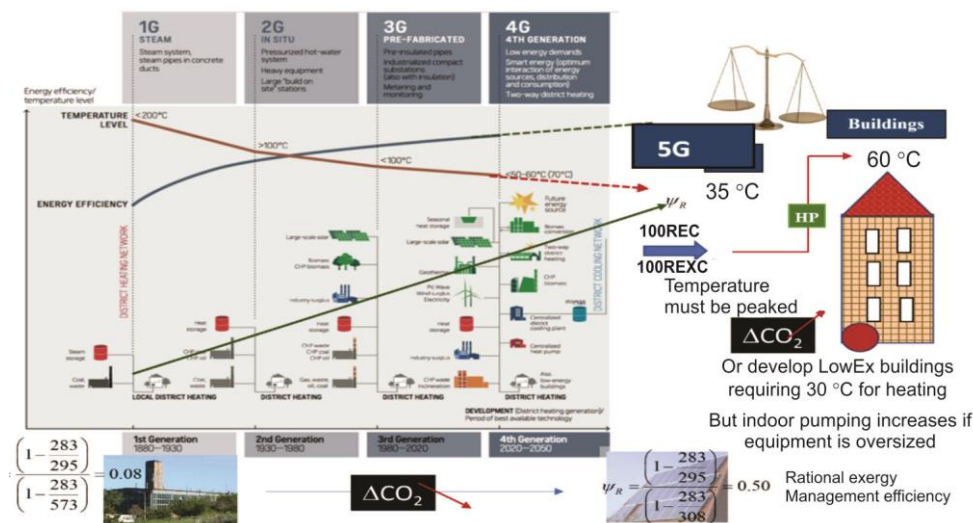
**Keywords:** *exergy, low-exergy district energy system, low-exergy building, maximum piping distance, equipment oversizing, temperature peaking*

### Introduction

This paper hypothesizes that an environmentally admissible district energy system is possible only if it is designed and operated according to the Second Law of thermodynamics and paves the way for the accomplishment of the 2030 EU climate and energy framework. This framework includes binding targets and policy objectives of reducing GHG emissions by at least 40% from 1990 levels, to increase the share of renewables by at least 32% of final energy consumption, and to improve energy efficiency by at least 32.5% [1]. Among these targets, low temperature district energy systems are becoming a focal point for potential solutions. This paper is expected to contribute by expanding this concept into a dynamic design and control tool for maximum exergy rationality for nearly-zero emissions. For increasing the share of renewables for 100% renewable cities (100REC), it is necessary to tap in widely abundant but unexploited low-exergy renewables. Figure 1 shows the historical trend with

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steam heating with  $>200^\circ\text{C}$ , named 1G (first-generation) leading to poor energy (First law) efficiency,  $\eta_I$ , and exergy rationality,  $\psi_R$  (Second Law). The system got better and diverse in terms of renewables with lower supply temperatures for higher efficiency, better exergy rationality, and temperatures decreased below  $60^\circ\text{C}$ , which is named 4G [2-4].



Note: The Original Figure Expanded, Extrapolated, and Modified from [2, 3, 4]

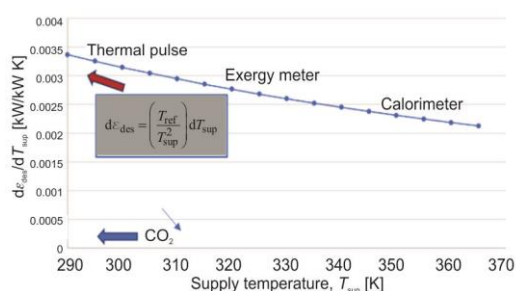
**Figure 1. Historical evolution of district energy systems and the handicap with existing building stock**

Today, district heating systems with  $35^\circ\text{C}$  supply temperatures are considered (5G), potentially leading to  $5G^+$  systems, which shall involve even lower supply temperatures. For example, the EU project RELaTED in Denmark involves an ultra-low temperature district heating demonstration project at a temperature range of  $45\text{--}30^\circ\text{C}$  [5]. Dealing with low-exergy sources, the essence of exergy balance between supply and demand became more recognizable such that equipment oversizing and/or temperature peaking in buildings renders the advantages pointless in terms of economy, environment, energy, and exergy. For example, an electrically driven heat pump seems to be energy efficient. Yet the large difference between unit exergy of electricity ( $0.95\text{ W/W}$ ) and the low temperature heat (below  $0.10\text{ kW/kW}$ ) requires a COP of 9 or above to be exergy-even. Otherwise, destroyed exergy leads to avoidable  $\text{CO}_2$  emissions,  $\Delta\text{CO}_2$ . At low supply temperatures, the difference between the supply and return temperatures both in the building and the district network must also be small. This leads to high power demand by pumps and fans unless the pipe and duct diameters are selected larger, which in turn will be responsible for additional embodiments of cost,  $\text{CO}_2$ , exergy, energy, and material. Temperature-peaking generates more GHG and ozone-depleting emissions, compounded by additional material, energy,  $\text{CO}_2$ , and exergy embodiments and more pump power for fluid circulation in the oversized equipment. Two definitions follow [4, 6]:

- The 100REC is a city with defined municipal/administrative boundaries, which on an annual basis, satisfies at least 75% of its power, heat, and cold demand from renewables in its boundaries, with proper thermal and electrical energy storage mediums and if the remaining 25% is imported from external renewables.
- The 100REXC is a city with defined municipal/administrative boundaries, which on an annual basis satisfies at least 75% of the total power, heat, and cold exergy demands from

renewables, with sufficient thermal and electrical energy storage mediums and if the remaining 25% is satisfied by outside renewables and the annually-averaged city-wide rational exergy management efficiency,  $\eta_R$  is not less than 0.50.

Energy watch group [7] outlined a 1.5 °C scenario for global warming emergency with a cost-effective, cross-sectoral, technology-rich global 100% renewable energy system. Their model simulates a total global energy transition in the electricity, heat, transport, and desalination sectors by 2050 to prove that the transition to 100% renewable energy is economically competitive with fossil and nuclear-based systems leading to zero emissions even before 2050. Another technical barrier to 5G systems is the increased sensitivity of exergy destructions by lower supply temperatures, which is shown in fig. 2. This makes the precise control of heat supply in response to dynamically changing loads more difficult. When this difficulty is coupled with the fact that the difference between the supply and return temperatures,  $\Delta T$ , decrease, there is also a need for more accurate and sensitive heat measuring devices like thermal pulse meters. The minimization of exergy destructions requires a good exergy balance between the low-exergy district and low-exergy buildings [8]. In this respect, the district of Ostra Sala Backe in Uppsala Municipality in Sweden planned a near-zero energy district for 20000 residents, including combined heat and power, heat pumps, which are driven on renewable energy, smart home automation, efficient lighting, and bioelectricity-driven public transport. The annual exergy that is produced in the district is optimized by REMM, through eight measures, supplying thermal exergy of 49.7 GWh, where the annual exergy consumed is 54.3 GWh. This corresponds to an exergy match with 84% [8]. On the other hand, through its various projects and publications, the IEA EBC Annex 64-LowEx Communities demonstrates the potentials of low exergy thinking on a community level as energy and cost-efficient solutions towards 100% renewable and GHG-free systems. Central challenges are the identification of promising and efficient technical solutions for practical implementation [9].



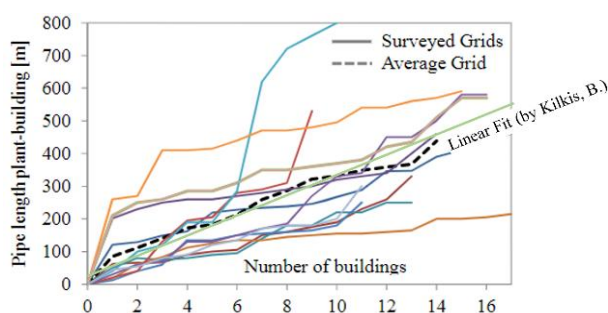
**Figure 2. Variation of destroyed exergy with supply temperature [4]**

or more energy sources into a single system to overcome the limitations of individual technologies. According to Gong and Werner [11], another consequence of the current level of distribution temperatures if fossil fuels are used is that two-thirds of the exergy content fed into the hydronic distribution networks are lost in the heat distribution chain before fulfilling the final customer temperature demands. In this case implementation of LowEx buildings does not make much sense due to large unit exergy difference between the fossil fuel and unit exergy of the building. This is one of the reasons for 100% renewable cities. On the other hand, they gave the first clues about the importance of exergy rationale especially when low-exergy renewables used by mapping energy and exergy flows in Sweden. Harvey claimed that it will be necessary

In line with 100% renewable heating and cooling for a sustainable, low-exergy future, EU RHC is emphasizing on district energy systems for better and concerted utilization of renewables, establishing an important strategic part of the decarbonization and electrification efforts [10], while four key cross-cutting technology areas were identified. The first one is the district heating and cooling. Other key areas are thermal energy storage, heat pumps, and hybrid renewable energy systems, combining two

to replace fossil fuels in any case with hydrogen fuel in applications where renewable energy resources may not be directly utilized [12]. The pioneering work on solar-assisted district heating was carried out in Sweden during the 1970's and 1980's. By 2003, eight solar-assisted district heating systems had been constructed under the German Solarthermie-2000 program. Fischedick *et al.* [13] provided a wide review of an all-renewable energy system using hydrogen and electricity as interchangeable energy assets. A hydrogen economy district energy system was introduced recently [14] and Dincer and Rosen [15] gave a detailed analysis of hydrogen production from solar and wind systems with their embodied exergy consumption. District cooling is also possible by low-exergy cold sources like a deep lake and seawater [13]. For example, in an urban renewal project in the Italian seaport of Livorno covering 63 apartments and 37 shops rely on seawater for district cooling through two heat pump stations [16]. The authors claimed an average COP value of 4.09 in heating mode supplying hot water at 48.9 °C (322K). What misses in this article is the exergy rationality, such that at the given supply temperature and for a reference temperature of 283 K, the exergy-based COP reduces to 0.495 according to the ideal Carnot cycle. Lund [17] has introduced the concept of smart energy systems approach via the EU EnergyPLAN code (Advanced Energy System Analysis Computer Model) for 100% renewables. A smart thermal grid is a parallel term to the smart electricity grid, in such a manner that it responds to fluctuating renewable energy resources by proper controls and allocation schemes. In this code, the objective is maximum efficiency (First law) and affordable cost. However, the exergy constraints (Second law) on the objective function are not included. In the same token, the very first district energy company that coined the term Exergy in their CHP-based district energy system title is in Stockholm, Sweden [18]. The so-called Stockholm Exergi's goal is to utilize 100% renewable fuels by 2022, which is in line with the aim of the city of Stockholm to be a fossil-fuel-free city by 2040. The Brandenburg town of Hennigsdorf planned to increase the climate-neutral share of heat in its existing district heating network to 80% in five years, by integrating the waste heat at a maximum temperature of 60 °C (333K) from local steelworks and 854 m<sup>2</sup> solar thermal collectors. A large thermal storage system provides sufficient flexibility. By 2020 it is expected to have 81% CO<sub>2</sub> neutrality with the contribution of bio-natural gas, forest wood, solar thermal, waste heat, and fossil fuels [19]. The distance between the plant and the district, especially in low-exergy renewable energy district heating and cooling is very important. But the few available works of literature on this topic depend on the First law and economy only. For example, Prando *et al.* [20] have developed a numerical model for the thermal behavior of a district heating network and calculated its performance in terms of cost-optimal building refurbishment, focusing on 13 micro-networks located in South Tyrol, Italy, and investigated the optimum building refurbishment for constant heat price and provided data about a relationship between the thermal load decrease and the distribution cost for fixed piping design. Although it covers a limited number of buildings, it shows the dependence of the piping length and thermal loads as a function of the number of buildings that may have a closely-linear relationship, which is shown in fig. 3. Arguing that current designs depend on recommended values for specific pressure loss ( $R = \Delta P/L$ ) about economically feasible solutions, Wang *et al.* [21] developed an optimization model by considering the initial investment of piping and pumping costs. The resulting CO<sub>2</sub> emissions responsibility both during operation (pumps, *etc.*) and due to material embodiment and exergy difference between electricity, heat, and cold were not considered. Kavvaidas and Quoilin [22] investigated the maximum distance permitted to transport low-grade waste heat from industrial processes or thermal power plants for long distances, simply by using the First law of Thermodynamics and developed a techno-economic model. Their study involved the

supply temperature in addition to the work reported in reference [21]. They introduced an approximate equation, for  $L_{\max}$  as a function of the square-root of the thermal power,  $\dot{Q}_D$  [MW], multiplied by a constant, which depends on the supply temperature, thermal energy price, electricity price, and  $\dot{Q}_D$ . Ljubenko *et al.* [23] referred to exergy by noting that lowering the exergy more renewable and low-quality waste heat sources may be exploited.



**Figure 3. Plant to buildings distance; reproduced from [20] with an added linear fit**

They developed an exergy-based distribution-network analysis model and introduced new criteria for performance. Their model is based on the primary pipeline between the supply and demand points in the district heating system and a case study about the district heating of Saleska Valley revealed a relationship among optimal supply temperature, pipe diameters, and district capacity vs. exergetic efficiency and have shown that with

such an optimization and sensitivity analysis, a conventional design may be substantially improved. Verda *et al.* [24] made another thermo-economic analysis of a district heating system, which shows that the average exergo-economic unit cost of the district supply mainly depends on the exergy flow and mechanical power required. Sangi and Muller [25] applied the Second law to control, which also applies to district energy systems in general. They stated that for proper performance and environmental benefits, exergy-based control is necessary because district energy systems are highly dynamic. A simple relationship states that  $L_{\max}$  is proportional to  $\dot{Q}_D$ , sometimes numerically raised to a power constant [8, 26-28].

### Aim of the research work

This research aims an exergy-based holistic model, which will be instrumental in optimizing the design and operation of successful 5G districts for improving the overall  $COP_{EX}$  value by primarily focusing on the plant-to-district distance. All studies in the literature analyze the plant-to-district distance in a simple format, which is isolated from the resources, the district plant, and the buildings on the demand side. These studies were also carried in terms of the First law, without taking the embodiments into account. None of them holistically covered the four tiers of this research.

### Preliminary model

#### Start-up model

There is a simple connection between the district plant and the district, fig. 4. The electrical power demand of the circulation pump station(s) and the exergy of supply and demand sides are noted. There is a temperature-peaking heat pump, which comes with a penalty of ozone-depleting potential (ODP) and global warming potential (GWP) due to its indirect  $CO_2$  responsibilities, and refrigerant leaks. The ODP and GWP are closely related, which was recently expressed by a composite, ODI [29]. According to preliminary studies, the constants are:  $w = 0.1$ ,  $y = 0.045$ , and  $z = 0.01$ , whereby includes the water vapor released from cooling towers, which has a greenhouse effect leading to GWP:

$$ODI = \frac{wGWP^y}{(1-ODP)} \left( \frac{ALT}{1} \right)^z \quad \{ODP, < 1\} \quad (1)$$

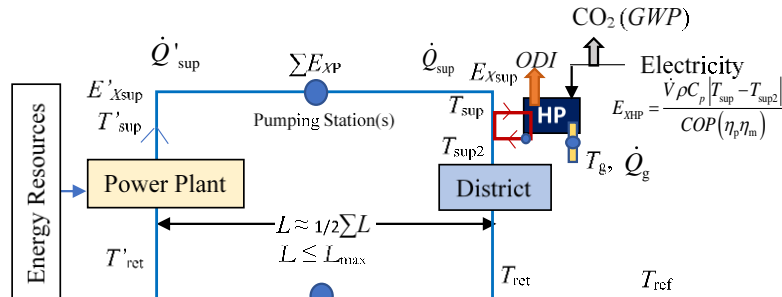


Figure 4. Start-up model for district energy system with a distant power plant

#### Recognition of the handicaps of low exergy district energy systems

By acknowledging that only low-exergy demand exists in a low-exergy district and there are low exergy renewable energy resources available, but pumping demand remains to be high-exergy, the exergy balance is getting more important than the thermal load balance. For a given district thermal power demand,  $\dot{Q}_{sup}$ , and a given reference environment temperature,  $T_{ref}$ , thermal supply power exergy, and pumping exergy are not considered:

$$E_{Xsup} = \dot{Q}_{sup} \left( 1 - \frac{T_{ret}}{T_{sup}} \right) \quad \left\{ \text{In district heating, } T_{sup} > T_{ret} \right\} \quad (2)$$

$$E_{Xsup} = \dot{Q}_{sup} \left( 1 - \frac{T_{ret}}{T_{sup}} \right) \quad \left\{ \text{In district cooling, } T_{sup} < T_{ret} \right\} \quad (3)$$

$$\sum E_{XP} = C\dot{Q}_{sup}^3 \sum L \times (0.95 \text{ kW/1 kW}) \approx C\dot{Q}_{sup}^3 \sum L \quad \left\{ \text{From Affinity law} \right\} \quad (4)$$

For a positive exergy gain, either eq. (2) or eq. (3) must be greater than eq. (4), which expresses the total exergy demand of the pumping power needed in the district network. Otherwise, the system will not be exergy-rational because more exergy will be spent than the exergy delivered to the district. In eq. (4),  $\sum E_{XP}$  is the total electrical power demand of the district pump station(s) with unit exergy of 0.95 kW/kW, (Approximately 1). In fig. 4 plant and city variables are differentiated with ( ' ) to take into account the thermal losses (gains) and fluid temperatures in the piping.

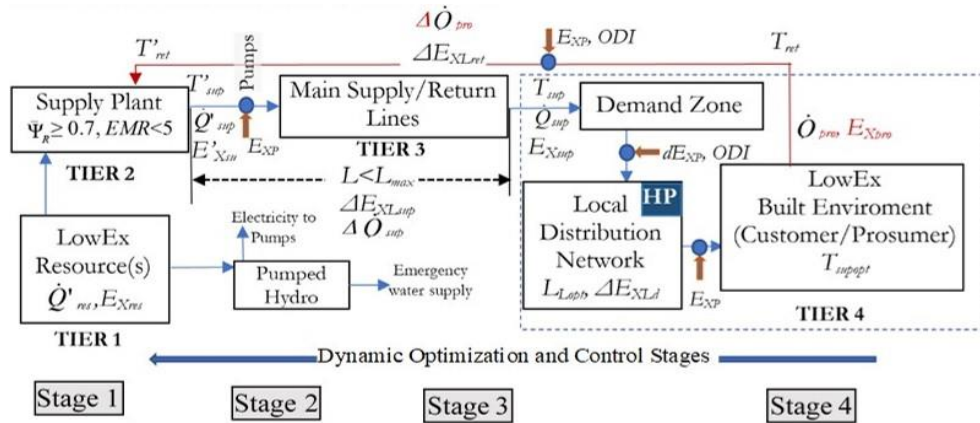
#### Possible remedies for the Low-exergy district handicap

##### Case 1: The HVAC equipment oversizing (without temperature peaking)

The exergy balance between supply and pumping determines the minimum  $T_{sup}$  and thus  $T'_{sup}$  by simultaneously solving eqs. (2) or (3) and (4), for a given  $\Delta T$  between district supply and return, with the  $NetE_{Xsup} = 0$  condition. Due to difficulties in exergy metering and helping to maintain the rated performance of the equipment is  $\Delta T$  kept quite low, as low as 5 K even lower:

$$NetE_{X\sup} = E_{X\sup} - \sum E_{XP} \quad (5)$$

$$T_{\sup} \geq \frac{\Delta T}{C\dot{Q}^2 \sum L} \quad \{\text{Without temperature peaking}\} \quad (6)$$



Note: ( ) means the plant side

Figure 5. Four tiers of the holistic district energy model

If the equipment performance is compromised while the district network is optimized for lower  $T_{\sup}$  values then an optimum mix of temperature peaking and equipment oversizing factor (OF) is necessary for the maximum use of low-exergy renewables towards 5G districts. Retrofits such as oversizing radiators may not be easy if indoor spaces are restrictive while plumbing also needs to be proportionately oversized for minimum impact on pumping exergy demand,  $P_{SR}$ . The OF is given by eq. (7) [30]:

$$OF = \frac{c(T_{f,design} - T_a)^n}{c(T_{f,5G} - T_a)^n} \approx \left[ \frac{T_{f,design} - T_a}{T_{f,5G} - T_a} \right]^n \quad \{OF \geq 1\} \quad (7)$$

$$P_{SR} = \left\{ \frac{\left( T_{\sup,design} - \frac{\Delta T_{design}}{2} - T_a \right)^{3n}}{\left( T_{\sup,f,5G} - \frac{\Delta T_{\sup,5G}}{2} - T_a \right)} \right\} \quad (8)$$

Utilization of the lowest-exergy resources with low  $\Delta T$  in the hydronic circuit, without compromising the COP of heat pumps at the minimum need for temperature peaking is possible only by LowEx buildings, which also reduce the embodied energy, exergy, cost, and CO<sub>2</sub> emissions attributable to their power demand,  $E_{XHP}$ , and minimize refrigerant leakages. The  $E_{XHP}$  depends on the COP [4]:

$$COP = q - r |T_{\sup 2} - T_{\sup}| \quad (9)$$

If the district heat is going to be utilized also in an open system, like domestic hot water supply, then  $T_{\sup}$  or  $T_{\sup 2}$  needs to satisfy the limits set for minimizing Legionella risk. This may require another set of temperature peaking limit. When all these parameters are

considered, it becomes clear that the city (Tier-4, fig. 8) needs special care and exergy-oriented optimization. In conclusion, the distance between the central plant and the district network becomes more critical when low-exergy heat or cold is circulated. For example, if instead of 90-70 °C supply and return temperature with unit exergy of 0.055 W/W, 40 °C to 30 °C is in place, only 0.032 W/W is circulated. The latter becomes less comparable with the power exergy demand of the pump stations, rendering exergy a dominant parameter in determining the maximum allowable distance [31-34].

*Case 2: Temperature peaking with heat pump (without HVAC equipment oversizing)*

The term  $\Sigma E'_{XP}$  includes the power demand of additional circulation pumps and the ground loop, where  $\dot{V}$  is the volume flow rate of the circulating fluid in the district loop with the given average thermophysical properties  $\rho$  and  $C_p$ . The  $\eta_p$  and  $\eta_m$  are respectively the pump drive, and the motor efficiencies:

$$NetE_{X\sup} = E_{X\sup} - \Sigma E'_{XP} - E_{X\sup} \quad (10)$$

$$T_{\sup} \geq \frac{T_{\text{ref}}}{\left(1 - C\dot{Q}_D \sum L - \frac{\dot{V} \rho C_p |T_{\sup} - T_{\sup 2}|}{COP(\eta_p \eta_m)}\right)} \quad \{\text{With temperature peaking}\} \quad (11)$$

*Case 3: The optimum mix of temperature peaking and equipment oversizing*

The objective is to pair low-temperature renewables with low-temperature districts with little or no need for temperature peaking to satisfy the recent 5G<sup>+</sup> trend.

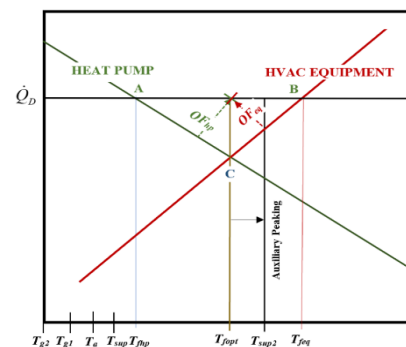
STEP 1 – Economic optimization

Equation (12) determines the  $T_{f,\text{opt}}$  (point C in fig. 6) for minimum life-cycle cost regarding heat pump vs. equipment oversizing. Here,  $C_{\text{eq}}$  and  $C_{\text{hp}}$  are the life-cycle cost factors [€/Wh] for the equipment and the heat pump at their rated operating temperatures, respectively. If the supply temperature  $T_{\sup}$  needs to be peaked ( $T_{\sup} < T_{f,\text{HP}} < T_{f,\text{eq}} < T_{\sup 2}$ ), temperature deficits namely  $C_2 = (T_{f,\text{eq}} - T_a)$  and  $C_1 = (T_{f,\text{p}} - T_g)$ , respectively need to be compensated to maintain the original thermal performance by partially oversizing the heat pump ( $OF_{\text{HP}}$ ) and the equipment ( $OF_{\text{eq}}$ ) by using eq. (12). The  $T_{f,\text{opt}}$  is the optimum operating temperature,  $T_{f,\text{eq}}$  and  $T_{f,\text{HP}}$  are the rated operating temperatures of the equipment at an indoor temperature  $T_a$ , and the heat pump ground heat at a temperature  $T_g$ , respectively:

$$T_{f,\text{opt}} = \sqrt{\frac{C_{\text{eq}} C_2}{C_{\text{HP}} C_1}} + T_a \quad (12)$$

STEP 2 – Tandem Heat Pumps

Figure 7 shows one large temperature lift-heat pump and a multitude of tandem heat pumps with smaller temperature lifts. In this strategy,  $\Delta T_i$  is kept constant along the tempera-



**Figure 6. The linearized performance conflict between heat pump and HVAC equipment [35]**

ture peaking path for each heat pump ( $i$ ). According to previous studies, only two heat pumps in tandem gives the best result [36]:

$$\Delta T_o = T_{\text{sup}2} - T_{\text{sup}} \quad (13)$$

$$\Delta T_i = \left( \frac{\Delta T_o}{N_{\text{HP}}} \right) = \text{constant} \quad (14)$$

$$COP_i = q - (r\Delta T_i) = q - r \left( \frac{\Delta T_o}{N_{\text{HP}}} \right) \{N_{\text{HP}} = 2\} \quad (15)$$

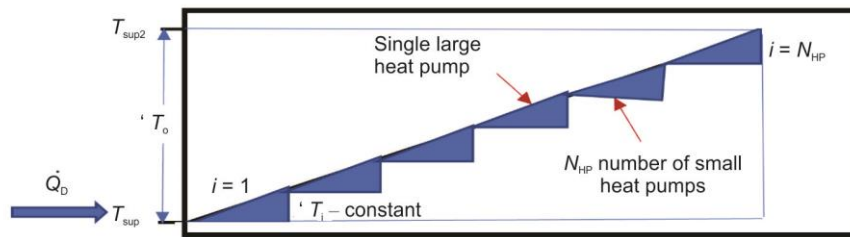


Figure 7. Temperature peaking with a multitude of  $N$  number of smaller heat pumps in tandem

### The need for an exergy-based model

Low-Exergy, “High-Efficiency” renewable/waste energy systems and equipment which are not generally collocated, often fail in terms of the Second law of thermodynamics at the absence of an exergy-based model. Consider a ground-source heat pump that delivers hot water to a building at a  $T_{\text{sup}2}$  temperature of 55 °C (328 K). The ground-source temperature  $T_g$  is 283 K. If the electric power input to the heat pump is 1 kW, then the thermal power delivered will be  $COP$  kW, assuming that the ambient exergy input and parasitic exergy destructions (pumps, *etc.*) are ignored. The corresponding exergy of the thermal power delivered to the building according to the ideal Carnot cycle is  $COP \times (1 - 283 \text{ K}/328 \text{ K})$ , which is only  $(0.137 \times COP)$  kW. Therefore, the minimum  $COP$  must be 7.3 (1 kW/0.137 kW) for the exergy break-even condition. A  $COP_{\text{EX}}$  term for a simple heat pump case was defined. For example, from eqs. (9) and (16), the optimum supply temperature,  $T_{\text{sup}2,\text{opt}}$  for maximum  $COP_{\text{EX}}$ , which represents the optimally maximum exergy gain may be determined. The  $COP_{\text{EX}}$  and the unit exergy destruction,  $\varepsilon_{\text{des}}$  are inversely proportional and,  $\varepsilon_{\text{des}}$  is related to the avoidable  $\text{CO}_2$  emissions,  $\Delta\text{CO}_2$  by referencing it to a natural-gas non-condensing boiler, 0.87 kW/kW of unit exergy, 0.2 kg  $\text{CO}_2/\text{kWh}$ , thermal efficiency 85% in eqs. (19) to (23). Such derivations are not possible by the  $COP$  definition given in eq. (9), which only shows that  $T_{\text{sup}2}$  should be close to  $T_g$ . Therefore the First law must always be accompanied by the Second law for environmentally responsible designs. A simple heat pump is a piece of stand-alone equipment with one energy source input port and one energy supply port:

$$COP_{\text{EX}} = COP \left( 1 - \frac{T_g}{T_{\text{sup}2}} \right) \{ \text{Simple heat pump only} \} \quad (16)$$

$$T_{\text{sup}2,\text{max}} = \sqrt{T_g \left( \frac{q}{r} \right) + rT_g} \{ \text{For maximum } COP_{\text{EX}} \} \quad (17)$$

## Development of the holistic district energy model

### New rules of exergy and emissions

In pursuing the aim of this work, the following rules were compiled. For a sustainable and exergy-rational district energy system the minimum REMM efficiency,  $\psi_R$  is set by the following green district condition [4, 33]:

$$\psi_{Ri} \geq 0.70 \quad (18)$$

If major exergy destruction takes place upstream on a branch ( $i$ ) of exergy flow:

$$\psi_{Ri} = \left( \frac{\varepsilon_{\text{dem}}}{\varepsilon_{\text{sup}}} \right)_i \quad (19)$$

or takes place downstream:

$$\psi_{Ri} = 1 - \left( \frac{\varepsilon_{\text{des}}}{\varepsilon_{\text{sup}}} \right)_i \quad (20)$$

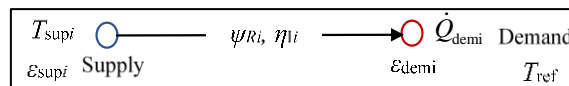


Figure 8. Supply-demand exergy flow in a single path ( $i$ ) of a complex system

$$\bar{\psi}_R = \frac{\sum_{i=1}^j \psi_{Ri} \dot{Q}_{\text{demi}} / \eta_{li} \left( 1 - \frac{T_{\text{ref}}}{T_{\text{sup } i}} \right)}{\sum_{i=1}^j \dot{Q}_{\text{demi}} / \eta_{li} \left( 1 - \frac{T_{\text{ref}}}{T_{\text{sup } i}} \right)} \quad (21)$$

$$\eta_{\text{II}} = \text{COP}_{\text{EX}} = \bar{\psi}_R \eta_{\text{I}} \quad (22)$$

$$\varepsilon_{\text{des}} = 1 - \text{COP}_{\text{EX}} = 1 - \eta_{\text{II}} = 1 - (\eta_{\text{I}} \bar{\psi}_R) \quad (23)$$

If both  $\eta_{\text{I}}$  and  $\psi_R$  are one then  $\varepsilon_{\text{des}}$  is zero. If both  $\eta_{\text{I}}$  and  $\psi_R$  are zero then  $\varepsilon_{\text{des}}$  is one: all exergy is destroyed.

On a single exergy flow path in a complex system after using eq. (20):

$$\varepsilon_{\text{des}} = \varepsilon_{\text{sup}} (1 - \psi_R) = \varepsilon_{\text{sup}} \left( 1 - \frac{\eta_{\text{II}}}{\eta_{\text{I}}} \right), \quad (24)$$

from eq. (23):

$$\text{COP}_{\text{EX}} = 1 - \varepsilon_{\text{des}} = 1 - \varepsilon_{\text{sup}} (1 - \psi_R) \quad (25)$$

$$\Delta \text{CO}_2 = 0.27 \varepsilon_{\text{des}} \text{ kg CO}_2/\text{kWh of heat} \quad (26)$$

$$\sum \text{CO}_2 = \left( \frac{c}{\eta_{\text{T}}} \right) + 0.27 \varepsilon_{\text{des}} \{ \text{per unit heat, } Q \} \quad (27)$$

After neglecting transmission losses or temperature is peaked by an on-site boiler, such that if  $\eta_T \sim \eta_I$ .

$$\begin{aligned}\sum \text{CO}_2 &\approx \left( \frac{c}{\eta_I} \right) + 0.27 \varepsilon_{\text{des}} \approx c \left( \frac{\text{COP}_{\text{EX}}}{\bar{\psi}_R} \right)^{-1} + 0.27 \varepsilon_{\text{des}} \\ &= \left( \frac{c \bar{\psi}_R}{\text{COP}_{\text{EX}}} \right) + 0.27 (1 - \text{COP}_{\text{EX}})\end{aligned}\quad (28a)$$

$$\begin{aligned}\sum \text{CO}_2 &\approx \left( \frac{c \bar{\psi}_R}{1 - \varepsilon_{\text{sup}} (1 - \bar{\psi}_R)} \right) + 0.27 [1 - 1 + \varepsilon_{\text{sup}} (1 - \bar{\psi}_R)] \\ &\approx \left( \frac{c \bar{\psi}_R}{1 - \varepsilon_{\text{sup}} (1 - \bar{\psi}_R)} \right) + 0.27 [\varepsilon_{\text{sup}} (1 - \bar{\psi}_R)]\end{aligned}\quad (28b)$$

$$\sum \text{CO}_2 \approx \left( \frac{\frac{c \bar{\psi}_R}{\varepsilon_{\text{sup}}}}{\frac{1}{\varepsilon_{\text{sup}}} - (1 - \bar{\psi}_R)} \right) + 0.27 [(1 - \bar{\psi}_R)] \quad \{\bar{\psi}_R > 0.70\} \quad (29)$$

$$d\varepsilon_{\text{des}} = \left( \frac{T_{\text{ref}}}{T_{\text{sup}}^2} \right) dT_{\text{sup}} \quad \{\text{see fig. 2}\} \quad (30)$$

$$\varepsilon_{\text{des}}(T_{\text{sup}}) = \frac{1}{2} \left( 1 - \frac{T_{\text{ref}}}{T_{\text{sup}}} \right) \quad \{T_{\text{sup}} \geq T_{\text{ref}}\} \quad \{\text{must be minimized}\} \quad (31)$$

### **Tiers of the holistic model**

There are four tiers, which establish the steps of dynamic optimization and control algorithm: TIER-1 – Renewable energy resource(s), TIER-2 – District energy supply plant, TIER-3 – Exergy transport between the plant and the district (city), and TIER-4 – Demand (customer) zone of the district energy system, including prosumer supply.

$$\dot{Q}_{\text{sup}} = \eta_I \dot{Q}_{\text{res}} + \dot{Q}_{\text{pro}} - \Delta \dot{Q}_{\text{pro}} - \Delta \dot{Q}_{\text{sup}} \quad (32)$$

$$E_{X \text{ sup}} = \eta_{II} E_{X \text{ res}} + E_{X \text{ pro}} - \Delta E_{X \text{ sup}} - \Delta E_{X \text{ pro}} \quad (33)$$

where  $\eta_I \dot{Q}_{\text{res}}$  is the thermal power supply at the exit of the plant,  $\dot{Q}'_{\text{sup}}$ . The  $\eta_I$  is the overall First law efficiency. The last two terms in eqs. (32) and (33) represent the exergy losses between plant and the district and  $\eta_{II}$  is the exergy efficiency. Thermal loss (gain) coefficients are assumed to be the same for heating and cooling pipes. The TIER-1 covers the energy sources available for the district. The TIER-2 covers energy conversion and storage systems. The TIER-3 covers the main piping system that connects the district plant and the built environment on both supply and return sides. The TIER-4 covers the built environment (City). The TIER at the same time correspond to four stages of the dynamic optimization and control algorithm, which is planned for the next step of this study. The algorithm starts backward from TIER-4 to TIER-1.

$$\Delta E_{XLsup} = x_1 L \left| 1 - \frac{T'_{sup}}{T_{sup}} \right| \Delta \dot{Q}_{sup} \quad (34)$$

$$\Delta E_{XLret} = x_2 L \left| 1 - \frac{T'_{ret}}{T_{ret}} \right| \Delta \dot{Q}_{pros} \quad (35)$$

Here,  $x_1$  and  $x_2$  are the heat loss coefficients per meter of pipe. This rule holds for TIER-4 piping:

$$\Delta T_{sup} = T'_{sup} - T_{sup} = x_3 L \Delta \dot{Q}_{sup} \quad (36)$$

$$\Delta T_{ret} = T_{ret} - T'_{ret} = x_4 L \Delta \dot{Q}'_{pro} \quad (37)$$

#### The TIER-1: Resources

This tier is a hybridization of different renewable and waste energy sources available for the district plant area (TIER-2). Each energy conversion system ( $i$ ) like solar PVT or a

**Table 1. Sample list of wind turbine and solar PV embodiments [15]**

RES	Embodied exergy	Unit
Wind turbine (6 MW electricity)	1.21	MJ/s of lifetime
Solar PV (157.2 m <sup>2</sup> PV block)	716	GJ/block
Solar PVT (160 m <sup>2</sup> block)	1200*	GJ/block

\* Estimated value

wind turbine is defined in terms of their resource energy harvesting design capacity,  $\dot{Q}_R(i)$  [kW], unit exergy,  $\varepsilon(i)$  [kW/kW] supply temperatures (if applicable), chemical exergy (*i. e.* biogas from the district waste), energy conversion efficiency,  $\eta_1(i)$ , embodied exergy  $E_{X,m}(i)$  [kWh/kW], embodied CO<sub>2</sub> [kWh/kW equivalent] and embodied cost for unit  $\dot{Q}_R(i)$  [kW]. Embodied exergy and CO<sub>2</sub> costs must be returned by increased exergy rationality during operation. Sample exergy embodiments are given in tab. 1. The equivalent solar source temperature,  $T_{f,solar}$ , and unit exergy,  $\varepsilon_{solar}$  for a given normal solar insolation,  $I_n$  is given by eq. (38). Equation (39) is the Carnot Cycle-Equivalent  $T_f$  for wind [8]:

$$\frac{I_n}{1366 \text{ W/m}^2} = \frac{\varepsilon_{solar}}{\varepsilon_e} = \frac{\left(1 - \frac{T_{ref}}{T_{f,solar}}\right)}{1 \text{ kW/kW}} \{ \text{solar energy} \} \quad (38)$$

$$T_{f,wind} = \frac{T_{ref}}{(1 - 0.95\eta_{lwt})} \approx \frac{T_{ref}}{(1 - \eta_{lwt})} \{ \text{wind turbine} \} \quad (39)$$

#### The TIER-2: The central plant

All sustainable power and heat generating and energy conversion systems of ( $i$ ) different types using renewables and waste heat are collocated and bundled. Prosumers are excluded. A new exergy benefit-to-embodied cost metric, which at the same time indexed to exergy destructions during annual operation, namely *EXBC* has been developed, using simulated hourly design data for the given location and sustainable systems to be involved:

$$EXCB = \left( \frac{1}{k} \right) \sum_{i=1}^k \frac{\int_{t=0}^{8760} \left[ \dot{Q}_{Ri}(t) \eta_{li}(t) \left( \frac{\varepsilon_i(t)}{\varepsilon_{desi}(t)} \right) \right] dt}{\left[ E_{Xmi} + E_{mi} + \left( \frac{\bar{\eta}_T}{\bar{c}_f} \right) \text{CO}_{2mi} + \frac{1}{\bar{p}} C_{mi} \right]} \{ \text{maximize} \} \quad (40a)$$

Here the denominator includes embodiments of exergy, energy, CO<sub>2</sub>, and renewable system cost,  $C$ , respectively. Another constraint is the exergy-payback ratio of the total embodied exergy of the sustainable systems installed in the plant,  $\Sigma E_{X,m}$  vs.  $E'_{X,sup,i}$ , namely EMR for (i) different systems in the bundle. The goal is to keep EMR below 5 years, which is indexed to an annual capacity factor,  $CF_i$  of each renewable source (i) in TIER-1. Minimization is iterative with varying supply mix of renewables:

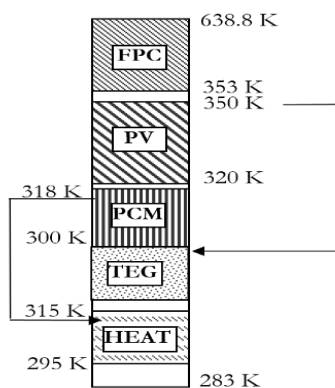
$$EMR = \frac{\sum E_{Xmi}}{8760 \sum CF_i E'_{Xsupi}} < 5 \quad \{\text{constraint}\} \quad (40b)$$

$$\psi_R = 1 - \frac{\sum \varepsilon_{des}}{\varepsilon_s} = 1 - \frac{\left(1 - \frac{350 \text{ K}}{353 \text{ K}}\right) + \left(1 - \frac{318 \text{ K}}{320 \text{ K}}\right) + \left(1 - \frac{315 \text{ K}}{318 \text{ K}}\right) + \left(1 - \frac{283 \text{ K}}{295 \text{ K}}\right)}{\left(1 - \frac{283 \text{ K}}{638.8 \text{ K}}\right)} = 0.88 \quad \{\text{see fig. 9}\}$$

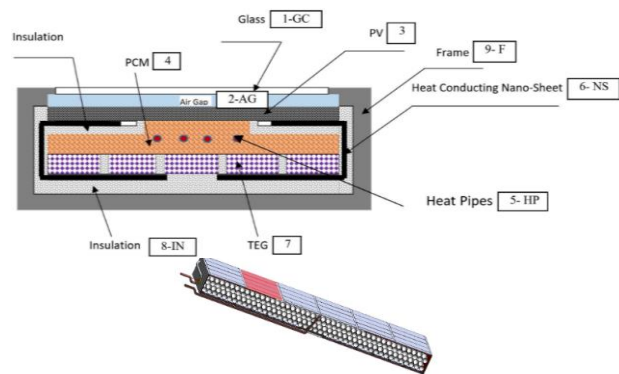
According to tab. 2 PVT3 (fig. 10) has the highest  $\psi_R$ .

**Table 2. Comparison of solar power, heat and power, and heat systems**

FEATURE		SYSTEM			
		CSP	PV	PVT	PVT3
Efficiency $\eta_i$	Power	0.40	0.17	0.20	0.25
	Heat	0.35	—	0.55	0.65
$\psi_R$		0.726	0.64	0.79	0.88
$\varepsilon_{des}$		0.344	0.198	0.094	0.055
$\Delta\text{CO}_2$		0.093	0.053	0.025	0.015
Occupied area per MW <sub>e</sub>		7.6 acres	4.4 acres	4.1 acres	3.4 acres



**Figure 9. Exergy flow bar for PVT3**



**Figure 10. Solar PVT3 cassette (TPI patent: 2017/10622)**

### The TIER-3 exergy transport between the plant and the city

Among many alternatives to supply exergy transport, the following three scenarios were selected:

- *Scenario 1, Electricity only:* Heating and cooling by local heat pumps (EU goal for total electrification for decarbonization). Yet additional electrical infrastructure and upgrading of power lines must be considered. An optimum on-site heat pump sizing, building insulation, and HVAC equipment oversizing may be required in TIER-4 to compensate for the performance loss of the equipment.
- *Scenario 2, Electricity and heat:* There is one main thermal network (piping) delivering heat only to the city. Cooling is achieved in the buildings by utilizing the heat supply in on-site ABS and ADS units. If there is a thermal power plant: temperature peaking at the plant with steam supply reduces power generation capacity. Otherwise, temperature peaking by heat pumps or building equipment oversizing or both at the city level. A dedicated and comprehensive model is presented, because in many cases this scenario is the most infrastructure, exergy, and carbon footprint-heavy.
- *Scenario 3, Electricity, heat, and cold:* Two district heating and district cooling networks. If the heating degree-hours value is dominant, then the cooling network may not be feasible and *Scenario 2* may be preferred. If there is a thermal power plant, then temperature peaking maybe with steam supply at an expense of reduced power. The exergy flow and pumping exergy balance per meter of pipe with known properties and the district course, gives a simple relationship:

$$dE_{XP} = \frac{\Delta E_{XP}}{\Delta L} \quad (41)$$

$$L_{\max} < \frac{\dot{Q}_{\text{sup}} \left( 1 - \frac{T'_{\text{ret}}}{T'_{\text{sup}}} \right)}{2dE_{XP}} \quad \{\text{one-way distance}\} \quad (42)$$

The term  $dE_{XPS}$  in the denominator is the exergy demand of the pumping station(s) per unit distance. The new equation considers the average design flow velocity in the main district loop (One may replace 5 m/s by another input design value). From Affinity Laws [37]:

$$\frac{P_{XEL}}{L} = c \frac{\dot{V}^3}{D^5} \left( \frac{1}{\eta_p} \right) \left( \frac{1 \text{ kW}}{1 \text{ kW}} \right) \leq \dot{Q}_D \left( 1 - \frac{T_{DS}}{T_{DR}} \right) \quad (43)$$

where:

$$c = f \left( \frac{\rho}{g_c} \right) \left( \frac{4}{\pi^2} \right) \quad (44)$$

Then solving for the maximum permissible distance from the plant to the district on average which can be assumed to be the half distance of the complete main district loop length,  $L$ :

$$L_{\max} \leq \frac{\left( 1 - \frac{T_{DR}}{T_{DS}} \right) \eta_p}{c \dot{Q}_D} \left( \rho C_p \Delta T_D \right)^2 D^5 \quad (45)$$

here:

$$\Delta T_D = T_{DS} - T_{DR} \quad (46)$$

The pipe diameter,  $D$ , is governed by practical flow velocity, *i. e.* 5 m/s:

$$L_{\max} \leq \frac{\left(1 - \frac{T_{DR}}{T_{DS}}\right) \eta_P}{c \dot{Q}_D} (\rho C_p \Delta T_D)^2 \left( \frac{4 \dot{Q}_D}{5 \pi \rho C_p \Delta T_D} \right)^{5/2} = \frac{\left(1 - \frac{T_{DR}}{T_{DS}}\right) \eta_P}{c} \dot{Q}_D^{1.5} \frac{32}{\sqrt{5 \pi \rho C_p \Delta T_D}} \quad (47)$$

– *Scenario 4, Central Temperature Peaking*: Large heat pumps peak the temperature at the plant. Although larger heat pumps are cheaper per unit capacity, district heating piping diameter is smaller with larger  $\Delta T$ , and equipment oversizing is reduced, larger TES systems are required at the plant and if district cooling is required, different heat and cold distribution regimes necessitate a separate cooling network.

#### Comparison of the scenarios

A new metric has been developed, *TVAR*, which stands for total value-adding potential ratio per unit electric power generated at the renewable energy plant of the district. The *TVAR* compares this unit power with the final total added value supplied to the district in terms of the sum of power and thermal exergy:

$$\begin{aligned} TVAR &= \frac{\text{Total exergy supplied to the district}}{\text{Unit electric exergy originally generated}} \\ &= \frac{x \eta_H \left(1 - \frac{T_{ret}}{T_{sup}}\right) + (1-x) \times 0.95 \eta_T}{1 \times 0.95} \quad \{1 \geq x \geq 0\} \end{aligned} \quad (48)$$

The split between the thermal and the electrical supply to the grid,  $x$  represents the aforementioned scenarios. The condition  $x = 0$  is *Scenario 1* (Only electricity is delivered to the district).  $x = 1$  represents *Scenario 2* (Only heat is delivered to the district). Equation (49), shows that  $L_{\max}$  is an implicit function of *TVAR*, which establishes another upper limit for  $L_{\max}$ . Table 3 summarizes typical results for four scenarios:

**Table 3. Typical *TVAR* values of the Scenarios for the same  $L_{\max}$**

Scenario	<i>TVAR</i>
1	0.95
2	0.92
3	0.89
4	0.85

$$TVAR = \frac{0.1x \left\{ \left[ \left( \frac{c}{\eta_P} \right) L_{\max} \right]^{2/3} \left( 5 \pi \rho C_p \Delta T_D \right)^{1/3} \right\} + (1-x) \times 0.95 [\eta_T f(L_{\max})]}{1 \times 0.95} \quad (49)$$

#### The TIER-4, The city

While the conglomeration of on-site heat pumps may be costlier, district infrastructure costs are saved. [33-35]. Therefore, the solution starts from LowEx buildings such that thicker the building insulation,  $t$  is, lower the heating or cooling loads are. This means less thermal power,  $\dot{Q}_0$ , low exergy demand,  $\varepsilon_{dem}$ , better *COP*, temperature peaking demand, leading to a decrease in other investment and operating costs, and embodiments. Equation (50) is the first solution:

$$T_{\text{sup}2} = \sqrt[n]{\frac{(\dot{Q}_o - bt)}{c}} + T_a \quad (50)$$

If  $T_{\text{sup}2}$  exceeds the value permitted in eq. (6) then this equation shall be used. Radiant panel heating and cooling systems offer two advantages: First, they are more responsive to very moderate supply temperatures. Second,  $n$  is close to one, which makes the control more linear [33]. A trivial solution is  $t_{\text{opt}} = \dot{Q}_o/b$ , and  $T_{\text{sup}2} \rightarrow (T_a - T_g)$ . For maximizing  $\psi_R$ , the next step with the ground reinjection temperature,  $T_g$  as the reference and electricity supplied by a natural gas power plant, is an exergy flow diagram, fig. 11.

$$\psi_R = \frac{\left(1 - \frac{T_g}{T_{\text{sup}}}\right) \text{COP}}{\left(1 - \frac{T_g}{2235}\right)} = \frac{\left(1 - \frac{T_g}{T_{\text{sup}}}\right)}{\left(1 - \frac{T_g}{2235}\right)} \left[ q - r(T_{\text{sup}} - T_g) \right] = \frac{\left(1 - \frac{T_g}{\sqrt[n]{\frac{(\dot{Q}_o - bt)}{c}}}\right)}{\left(1 - \frac{T_g}{2235}\right)} \left[ q - r \left( \sqrt[n]{\frac{(\dot{Q}_o - bt)}{c}} - T_g \right) \right] \quad (51)$$

$$t_{\text{opt}} = \left( \frac{\dot{Q}_o - c|T_{\text{sup}} - T_a|^n}{b} \right) \left\{ \text{with } \frac{d\psi_R}{dt} = 0 \right\} \quad (52)$$

$$\text{COP}_{\text{EX}} = \frac{(\dot{Q}_o - bt) \left| 1 - \frac{T_{\text{ref}}}{T_a} \right|}{\frac{(\dot{Q}_o - bt)}{(q - r|T_{\text{sup}2} - T_g|)} \times 0.95 + \sum E_{\text{XP}} \times 0.95 + (\dot{Q}_o - bt) \left| 1 - \frac{T_{\text{ref}}}{T_g} \right|} \left\{ \text{maximize} \right\} \quad (53)$$

Increasing COP leads to environmental and cost benefits while a smaller heat pump has less investment cost,  $\Delta I_{\text{HP}}$ , and longer operating hours close to peak efficiency. A payback period,  $T_{\text{pb}}$  is determined by comparing the additional net investment cost  $\Delta I = (\Delta I_{\text{ins}} - \Delta I_{\text{HP}})$ , and the net operational savings,  $S(t)$ , fig. 12:

$$S(t) = \bar{p} \left( \frac{\dot{Q}_o}{\Delta \text{COP}} \right) t \quad (54)$$

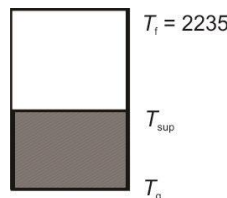


Figure 11. Exergy flow bar for electric-driven heat pump, electricity is from NG thermal plant

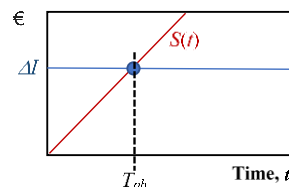


Figure 12. Additional net investment cost vs. net operational savings of a heat pump

## Holistic model

The holistic model is an expanded version of the  $COP_{EX}$  equation for TIER-4:

$$COP_{EX} = \frac{E_{Xsup} + E'_{Xpro}}{\left( \frac{\dot{Q}_o - bt}{(q - r|T_{sup} - T_g|)} \times 0.95 + \sum E_{XP} \times 0.95 + E_{Xres} + E_{Xpro} \right)} \quad \{\text{maximize}\} \quad (55)$$

The  $COP_{EX}$  may be maximized iteratively by changing variables.  $E'_{Xpro}$  is the part of the prosumer exergy generation,  $E_{Xpro}$  supplied to the district. Figure 13 gives a sample dependence of  $COP_{EX}$  on  $T_{sup}$  for different insulation thicknesses,  $t$ . The optimum  $T_{sup}$  does not change with  $t$  in this specific case. The dependence of  $COP_{EX}$  at thinner insulations diminishes with  $T_{sup}$  exceeding  $T_{supopt}$ .

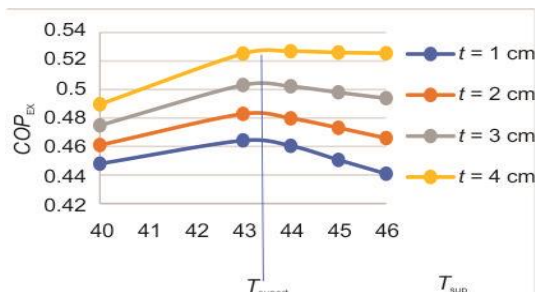


Figure 13. Change of  $COP_{EX}$  with  $T_{sup}$  and  $t$

## Discussion

This paper has dealt with the exergy-based optimum design and operation scheme of district energy systems, deemed to be necessary to be based on a holistic view, covering all phases starting from the renewable energies at their source, then including the energy conversion and storage plant feeding the district energy network, and finally the buildings in the district. For low temperature applications, which enable

us to harvest low-exergy renewables and waste thermal energy, all which remained almost unexploited so far, it has been pointed out that a careful and precise exergy balance between each step of the district supply and the demand points is essential. A holistic model was developed with an objective function of maximizing the exergy-based COP, namely  $COP_{EX}$  for the entire system. The REMM was utilized in deriving the essential relationships for defining and connecting the  $COP_{EX}$  value with exergy destructions and  $CO_2$  emissions, such that while  $COP_{EX}$  is maximized, the carbon footprint is minimized in terms of minimizing the exergy imbalances between all steps of district heating. The model is also valid for district cooling systems. In deriving LowEx buildings, the optimum insulation thickness was also included in the maximization process of  $COP_{EX}$ . Results showed that maximum  $COP_{EX}$  does not depend much on the district supply temperature. This relaxes the constraints on determining the optimum district supply temperature and the maximum permitted distance,  $L_{max}$  between the plant and the city.

## Conclusions

The 5G district energy systems are a promising asset against climatic urgency but at the same time, more prone to climatic hazards [38]. According to the IPCC Report, the global average surface temperature increases exponentially [39]. Low-exergy districts and exergy-matching buildings, all holistically designed and controlled with the second law increase the overall REMM efficiency,  $\psi_R$ , reduce  $GWP$  and  $ODP$  to such an extent that natural decarbonization may take over [40]. Therefore low-exergy district energy systems, when coupled with LowEx buildings, seem to have a big potential for decarbonization, provided that such attempts are accompanied by the following auxiliary recommendations.

- In a district energy system, customers may receive and return heat or cold at different temperatures. Therefore, development and use of exergy meters and thermal pulse meters will be prudent [4].
- Electric motor efficiencies higher than 0.90 (> IE4) and high-efficiency pumps [41].
- Solar PVT panels covering almost all solar spectrum [42-44].
- Switching to direct-current power supply. Wind and solar power are originally direct-current and then inverted to AC, and then converted to direct-current again in many uses like computers.
- Exergy budgeting for all components of district energy, including thermal energy storage.
- High efficiency wind turbines like direct-drive systems should be considered [45].
- The optimum number of building floors in urban development is important in such a manner that pumping exergy is related to  $L_{\max}$ , thus to the average number of building floors [46].
- Although each renewable source has their energy atlases [47], their different unit exergy make it difficult to overlay them to calculate their composite exergy supply potential. Therefore exergy-composite atlases are needed.
- Supplementary temperature-peaking systems, like fossil fuel-fired boilers, must be analyzed with their embodiments, CO<sub>2</sub> and ODI responsibilities, and exergy rationality.

## Nomenclature

$b$	– coefficient of thermal load dependence on building insulation thickness [–]	$N_{HP}$	– number of identical heat pumps in tandem [–]
$ALT$	– residence time in the atmosphere [year]	$NetE_{xsup}$	– difference between supply power exergy and total pumping exergy[kW]
$c$	– CO <sub>2</sub> content of the fuel [kgCO <sub>2</sub> /kWh], eq. (27)	$ODI$	– composite ozone-depletion index, eq. (1)
$\bar{c}_f$	– CO <sub>2</sub> content of the fuel mix in a given energy sector [–]	$\bar{p}$	– unit cost of a renewable energy system [kW]
$c$	– heating capacity of the equipment [kW/K <sup>-(1/n)</sup> ], eq. (7)	$q, r$	– constants of the linearized heat pump COP, eq.( 9)
$C$	– coefficient of the pumping power exergy demand, eq. (4)	$Q$	– thermal energy [kWh]
$C_p$	– specific heat [kJkg <sup>-1</sup> K <sup>-1</sup> ]	$\dot{Q}_D, \dot{Q}_{sup}$	– thermal power of the district energy system at the plant exit [kW]
$C_{HP}$	– life cycle cost of heat pump oversizing [€/kWh]	$\dot{Q}'_D, \dot{Q}'_{sup}$	– thermal power of the district energy system at the district entrance [kW]
$C_{eq}$	– life cycle cost of equipment oversizing [€/kWh]	$\dot{Q}_o$	– original building thermal load before insulation [kW]
$C_1$	– heat pump temperature coefficient at design conditions [K]	$S$	– net operational savings [€]
$C_2$	– equipment temperature coefficient at design conditions [K]	$T$	– temperature [K]
$\Delta CO_2$	– avoidable CO <sub>2</sub> emission [kgCO <sub>2</sub> /kWh]	$T_{DR}$	– average district loop return temperature in the main return pipe [K]
$COP_{EX}$	– exergy-based coefficient of performance [–]	$T_{DS}$	– average district loop supply temperature in the main supply pipe [K]
$D$	– pipe inside diameter [m]	$T_{sup2}$	– district main piping supply temperature after temperature-peaking [K]
$E_x$	– exergy [kW]	$x$	– split between the thermal supply and electrical supply to the grid [–]
$g_c$	– acceleration of gravitation =9.81 [m/sec <sup>2</sup> ]		
$I_n$	– solar energy intensity normal to the collector surface plane [W/m <sup>2</sup> ]		
$\Sigma L$	– total trip distance of the supply and return main piping [m]		
$L$	– straight distance between the central plant and the district center [m]		
$L_{\max}$	– allowable straight distance between the plant and the district [m], [km]		

### Greek symbols

$\rho$	– mass density [kg/m <sup>3</sup> ]
$\Psi_R$	– overall exergy management efficiency [–]
$\Delta P$	– pressure drop [Pa]
$\Delta T$	– supply and return temperature difference [K]

*Subscripts or superscripts*

a	– air (indoor)
e	– electricity
D	– district
DR	– district return side in the main district pipe
DS	– district supply side in the main district pipe
dem	– demand
des	– destroyed (exergy)
f	– Carnot cycle-equivalent source temperature-related
g	– ground (geothermal)
H	– heat
HP	– heat pump
i	– index for a branch in a multiple exergy-flow system
ins	– thermal insulation
k	– number of different renewable energy systems in the plant
m	– embodied
min	– minimum
max	– maximum (allowable)
opt	– optimum
p	– pump (pump station)
pb	– pay-back related variable
res, ret	– resource, return

solar	– solar energy system
sup	– supply
T	– power transmission-related
wind	– wind energy system
X, EX	– exergy
wt	– wind turbine
n	– equipment thermal output coefficient

*Acronyms*

ABS, ADS	– absorption and adsorption cooling
CHP	– combined heat and power
CSP	– concentrating solar power
DE, DH, DC	– district energy, heating, cooling
EBC	– energy in buildings and communities program
HP	– heat pump
IE4	– super-premium efficiency according to IEC/EN 60034-30-1:2014
IEA	– International Energy Agency
IPCC	– intergovernmental panel on climate change
LowEx	– low exergy (building, source, or district)
PV	– solar photovoltaic
PVT	– solar photovoltaic-thermal
100REXC	– hundred-percent renewable exergy city
RHC	– renewable heating and cooling
TPI	– Turkish Patent Institute

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