NUMERICAL AND ANALYTICAL APPROACH FOR SAKIADIS RHEOLOGY OF GENERALIZED POLYMERIC MATERIAL WITH MAGNETIC FIELD AND HEAT SOURCE/SINK

by

Muhammad AWAIS*, Saeed Ehsan AWANb, AQSAc, Nimra MUQADDASSa, Saeed Ur REHMANb, and Muhammad Asif Zahoor RAJA b*

*Department of Mathematics, COMSATS University Islamabad, Attock Campus, Attock, Pakistan
bDepartment of Electrical and Computer Engineering, COMSATS University Islamabad, Attock Campus, Pakistan
cDepartment of Mathematics, Quaid-i-Azam University Islamabad, Pakistan

Original scientific paper
https://doi.org/10.2298/TSCI180426284A

In this analysis, Sakiadis rheology of the generalized polymeric material has been presented with magnetic field and heat source/sink. Convective heating process with thermal radiations have been incorporated. Mathematical modeling has been performed for the conversion of physical problem into set of non-linear equations. Suitable transformations have been employed in order to convert the derived PDE into set of non-linear ODE. Analytical as well as finite difference method based numerical solutions for the velocity and temperature profiles are computed. Graphical and numerical illustrations have been presented in order to analyze the behavior of involved physical quantities. Error analysis for the non-linear system has been presented in order to show the validity of the obtained results. Bar charts have been plotted to present the heat flux analysis. Tabular values of local Nusselt number are computed for the involved key parameters. Heat transfer rates against magnetic and porosity effects found to be decreased since magnetic field and porosity retard the molecular movement of the fluid particles. This controlling property of magnetic field and porosity effects have application in MHD power generation, electromagnetic casting of metals, MHD ion propulsion, etc. Moreover internal heat generation and absorption effects have opposite effects on the fluid temperature.

Key words: maximum ten generalized polymeric material, Oldroyd-B model, Sakiadis flow, heat source/sink, magnetic field

Introduction

Fluid-flow problem induced due to moving surfaces with heat transfer analysis under the application of MHD are one of the useful problems in fluid mechanics due to their relevance with engineering and industry, for-instance, in metal extrusion, wire coating, fiber spinning, glass blowing, manufacturing, sheeting stuff, i.e., paper, fiber and metallic sheets, and in the process of polymer extrusion in which the sheet experiences the stretching phenomenon in order to acquire the preferred thickness [1-5]. In these applications, the value of the final outcome strongly depends upon the cooling rate, so in such processes, the mechanism of cooling rate lead to gain the final product of desired features [6, 7]. Sakiadis
[8, 9] present the seminal work on the boundary-layer flows and successfully introduce to several engineering and industrial applications. Later on, researchers investigated in applied mathematics and physics domains have analyzed his ideas and utilized them effectively to provide the reliable solution of several new scientific problems, such as Zierep and Fetecau [10] investigate in Rayleigh-Stokes problem involving the Maxwell fluid. Jamil et al. [11] in fluidics problems based on unsteady helical fluid-flow. He considered the Oldroyd-B fluid model and presented the relaxation/retardation time properties, Tan and Masuoka [12] presented the stability analyses for the Maxwell fluid problem with porous medium in the presence of thermal heating, Nadeem et al. [13] provide the homotopy analysis based results for the boundary-layer flow in the region of the stagnation point towards a stretching sheet, Hayat et al. [14] computed the thermal radiation as well as Joule heating dynamics for the MHD flow involving the Oldroyd-B fluid in the scenarios of the thermophoresis phenomenon. Malik et al. [15] investigated the model based on hydromagnetic 3-D Maxwell fluid-flow problem, Hayat et al. [16] analyze the dynamics of mixed convective 3-D flow problem involving the upper-convective Maxwell fluid in the presence of magnetic field. Mehmoond et al. [17] presented numerical treatment for micropolar Casson fluid over a stretching sheet, Ramesh and Gireesha [18] investigated in nano-fluid-flow problem for heat generation on Maxwell fluid, Mehmood et al. [19] analyzed the Jeffery nanofluid impinging obliquely over a stretched plate, Kumar et al. [20] computed the effect of flow of Oldroyd B nano-fluid with thermal radiation, Rana et al. [21] provided the numerical treatment on non-Newtonian flow with non-linear thermal radiation problems, Awais et al. [22] study the Sakeidis flow of polymeric nanoliquids and Generally, many studies have been reported recently to analyze the physical behaviour of fluid mechanics problems, [23-27] and reference in them.

In this investigation we have extended the problem of fluid-flow over a moving surface into new directions. We have considered the heat transfer analysis for the Sakiadis flow for the rheology of an Oldroyd-B fluid. Mathematical modeling of the momentum equation reveals the occurrence of generalized magnetic field term. The fluid dynamics in a porous medium under the application of internal heat generation/absorption and thermal radiation effects are analyzed. Analytical and numerical treatment have been performed for the momentum and energy dynamics by exploiting the strength of homotopy analysis method [28-33] and numerical procedure of finite difference scheme. Error analysis for the velocity and temperature profiles are presented to show the validity of the obtained results. Numerical and graphical illustration in term of tables and plots are presented to study the effect of rheology by varying the involved physical quantities.

**Mathematical formulation**

Consider the rheology of an Oldroyd-B model (a subclass of rate type fluid model) over a wall. Sakiadis flow situation has been considered within a porous medium. Magnetic field of strength, $B_0$, is applied along a transverse direction in order to predict the MHD as shown in fig. 1. Convective heat process has been considered to study the thermal properties at the wall and within the system.

The mathematical equation (32) governing the flow with internal heat generation/absorption properties:
div\mathbf{V} = 0 \quad (1)

\rho \frac{D\mathbf{V}}{Dt} = -\nabla p + \text{div} \mathbf{S} \quad (2)

\left(1 + \dot{\lambda}_t \frac{D}{Dt}\right) \mathbf{S} = \mu \left(1 + \dot{\lambda}_r \frac{D}{Dt}\right) \mathbf{A} \quad (3)

\frac{Da_t}{Dt} - \frac{\partial a_t}{\partial t} = u \omega + u_r \omega_r = 0 \quad (4)

\rho c_p \frac{dT}{dt} = k \nu^2 \mathbf{T} + \mathbf{q} \quad (5)

here the \mathbf{V} is the velocity field, \rho – the fluid density, \mathbf{S} – the stress tensor, \mathbf{A}_1 – the Rivlin-Ericksen tensor, \dot{\lambda}_t – the relaxation time effect, \dot{\lambda}_r – the retardation time effect, \mu – the dynamic viscosity, and \frac{D}{Dt} – the covariant derivative. Simplifying eqs. (2)-(5):

\left( \nu \frac{\partial^2 u}{\partial y^2} + \lambda_1 \left( \frac{\partial^2 u}{\partial y^2} + \nu \frac{\partial^2 u}{\partial x \partial y} - \frac{\partial^2 \nu}{\partial x \partial y} \right) \right) - \left( \frac{\sigma B_x^2}{\rho} + \frac{\nu}{k} \right) \left( u + \lambda_i \frac{\partial u}{\partial y} \right) +

\nu \left[ \frac{\partial^2 u}{\partial y^2} + \lambda_2 \left( \frac{\partial^2 u}{\partial y^2} + \nu \frac{\partial^2 u}{\partial x \partial y} - \frac{\partial^2 \nu}{\partial x \partial y} \right) \right]

\left( \nu \frac{\partial^2 T}{\partial y^2} + \lambda_2 \left( \frac{\partial^2 T}{\partial y^2} + \nu \frac{\partial^2 T}{\partial x \partial y} - \frac{\partial^2 \nu}{\partial x \partial y} \right) \right)

\frac{u \partial T}{\partial x} + \nu \frac{\partial T}{\partial y} = \alpha m \frac{\partial^2 T}{\partial z^2} - \frac{1}{\rho c_p} \frac{\partial q_0}{\partial y} + \frac{Q_0}{\rho c_p} (T - T_\infty) \quad (7)

It is noted that for \dot{\lambda}_2 = 0, the results for Maxwell model can be deduced. Additionally, in case of \dot{\lambda}_1 = \dot{\lambda}_2 = 0, one has a Newtonian fluid model results.

The subjected wall properties [22]:

\begin{align*}
  &u = U, \quad v = 0, \quad -k \frac{\partial T}{\partial y} = h_f \left( T_f - T \right) \quad \text{at} \quad y = 0 \\
  &u \to 0, \quad v \to 0, \quad T \to T_\infty \quad \text{as} \quad y \to \infty
\end{align*}

(8)

where \sigma and \ T represent the electrical conductivity and temperature of the fluid, respectively. Furthermore, \mathbf{B}_0, K, C_p, \alpha_m, Q_0 are the magnetic field strength, porosity of medium, specific heat constant, thermal conductivity, and internal heat generation or absorption parameter, respectively, while the radiative thermal flux quantity \mathbf{q}_r is defined as \mathbf{q}_r = -(4\sigma^3/k^3)\partial^4 T/\partial y^4. Making use of the quantities:

\begin{align*}
  \eta &= \frac{U}{\nu x}, \quad u = U f^*, \quad \nu = \frac{1}{2} \sqrt{\frac{\nu U}{x} \left( f - \eta f' \right), \quad \theta(\eta) = \frac{T - T_\infty}{T_{\infty} - T_\infty}} \quad (9)
\end{align*}

in eqs. (5)-(8):

\begin{align*}
  f^* + \left( \frac{1}{2} \right) f^* \frac{D_z}{2} \left( 2 f f' + \eta f'^2 f^* + f^2 f'' - M^2 \left[ f' - D_e (f - \eta f') f^* \right] \right) - Kf^* + KD_e \left( f f^* - \eta f f' \right) + D_e \left[ 2 (\eta f f' - \eta f f'^2) f^* - f f' - f'' \right] &= 0 \quad (10)
  \\
  \theta^* + \Pr \left( \frac{1}{2} f^* f' + h s \theta \right) + \frac{4}{3} Rd \theta^* &= 0 \quad (11)
\end{align*}
along with the wall conditions:

\[ f(\eta) = 0, \quad f'(\eta) = 1, \quad \vartheta'(\eta) = -\gamma_1[1 - \vartheta(\eta)], \quad \text{at} \quad \eta = 0 \]
\[ f'(\eta) \to 0, \quad \vartheta(\eta) \to 0 \quad \text{as} \quad \eta \to \infty \quad (12) \]

Note that in previous equations \( D_e = \lambda_1 U/2x \) and \( D_s = \lambda_2 U/2x \) are representing the Deborah numbers, \( M = (\delta\beta^2/\rho U)^{1/2} \) – the magnetic parameter, \( K = v/kU \) – the porosity coefficient, \( Rd \) – the radiation factor \( (= 16\delta^3 T^5/3k'k) \), \( Pr = v/\alpha_w \) – the Prandtl number, \( h_s = Q/\rho C_p \) – the internal heat generation/absorption quantity. The quantity of physical interest are the thermal variation at wall \( Nu_x \) as given:

\[ Nu_x = \frac{xq_w}{k(T_f - T_c)} \quad (13) \]

in which \( q_w \) represents the wall heat flux:

\[ q_w = -k \left( \frac{\partial T}{\partial \eta} \right)_{\eta=0} + (q_w)_{\eta=0} \quad (14) \]

In dimensionless form, aforementioned equations can be written:

\[ Nu_x / Re^{1/2} = \left( 1 + \frac{4}{3} Rd \right) \vartheta(0) \quad (15) \]

**Solution techniques**

*Series solution*: Homotopy analysis method has been employed for solving eqs. (10)-(12). The initial guesses and linear operator for \( f \) and \( \vartheta \) are selected:

\[ f_0(\eta) = 1 - e^{-\eta}, \quad \vartheta_0(\eta) = \left( \frac{\gamma_1}{1 + \gamma_1} \right) e^{-\eta} \quad (16) \]

while the appropriate initial guesses

\[ f^* - f' = 0, \quad \vartheta^* - \vartheta = 0 \quad (17) \]

Associated zeroth order problems:

\[ (1 - p)L_f \left[ f(\eta; p) - f_0(\eta) \right] = ph_f N_f \left[ f(\eta; p) \right] \quad (18) \]
\[ (1 - p)L_\vartheta \left[ \vartheta(\eta; p) - \vartheta_0(\eta) \right] = ph_\vartheta N_\vartheta \left[ \vartheta(\eta; p), f(\eta; p) \right] \quad (19) \]

in which \( N_f \) and \( N_\vartheta \) are non-linear operators defined:

\[
\begin{align*}
N_f \left[ f(\eta, p) \right] &= \frac{\partial^3 f(\eta, p)}{\partial \eta^3} + \frac{1}{2} \left[ f(\eta, p) \frac{\partial^2 f(\eta, p)}{\partial \eta^2} \right] - K \frac{\partial f(\eta, p)}{\partial \eta} - \\
&\quad - \frac{De}{2} \left[ f(\eta, p) \frac{\partial f(\eta, p)}{\partial \eta} \frac{\partial^2 f(\eta, p)}{\partial \eta^2} + \right. \\
&\left. \quad + \eta \left[ \frac{\partial f(\eta, p)}{\partial \eta} \right]^2 \frac{\partial^2 f(\eta, p)}{\partial \eta^2} + \left[ f(\eta, p) \right]^2 \frac{\partial^3 f(\eta, p)}{\partial \eta^3} \right] 
\end{align*}
\]
Awais, M., et al.: Numerical and Analytical Approach for Sakiadis Rheology of...

THERMAL SCIENCE; Year 2020, Vol. 24, No. 2B, pp. 1183-1194

\begin{equation}
-M^2 \left\{ \frac{\partial^2 f(\eta, p)}{\partial \eta^2} - \text{De} \left[ f(\eta, p) - \eta \frac{\partial f(\eta, p)}{\partial \eta} \right] \frac{\partial^2 f(\eta, p)}{\partial \eta^2} \right\} + \text{KDe} \left[ f(\eta, p) \frac{\partial^2 f(\eta, p)}{\partial \eta^2} - \eta \frac{\partial f(\eta, p)}{\partial \eta} \right] + \text{Ds} \left[ \frac{2}{\eta} \frac{\partial f(\eta, p)}{\partial \eta} \frac{\partial^3 f(\eta, p)}{\partial \eta^3} + \eta \frac{\partial f(\eta, p)}{\partial \eta} \frac{\partial^4 f(\eta, p)}{\partial \eta^4} - \frac{\partial f(\eta, p)}{\partial \eta} \frac{\partial^2 f(\eta, p)}{\partial \eta^2} \right] \right\} (20)

\left[ \frac{\partial^2 \theta(\eta, p)}{\partial \eta^2} \right] = \frac{\partial^2 \theta(\eta, p)}{\partial \eta^2} + \text{Pr} \left[ \frac{f(\eta, p)}{2} \frac{\partial \theta(\eta, p)}{\partial \eta} + h \text{s} \theta(\eta, p) \right] + \frac{4}{3} \text{RD} \frac{\partial^2 \theta(\eta, p)}{\partial \eta^2} (21)

Using Taylor’s series for expansion of \( f(\eta, p) \) and \( \theta(\eta, p) \), and considering that the resulting series are convergent at \( p = 1.0 \):

\begin{equation}
f(\eta) = f_0(\eta) + \sum_{n=1}^\infty f_n(\eta) (22)
\end{equation}

\begin{equation}
\theta(\eta) = \theta_0(\eta) + \sum_{n=1}^\infty \theta_n(\eta) (23)
\end{equation}

where

\begin{equation}
f_n(\eta) = \left[ \frac{1}{m!} \frac{\partial^m f(\eta; p)}{\partial p^m} \right] \quad \theta_n(\eta) = \left[ \frac{1}{m!} \frac{\partial^m \theta(\eta; p)}{\partial p^m} \right]_{p=0} (23)
\end{equation}

The problems of \( m \)-th order given:

\begin{equation}
L_f \left[ f_m(\eta) - \chi_m f_{m-1}(\eta) \right] = h \text{R}_m^f(\eta) (24)
\end{equation}

\begin{equation}
L_\theta \left[ \theta_m(\eta) - \chi_m \theta_{m-1}(\eta) \right] = h \text{R}_m^\theta(\eta) (25)
\end{equation}

and the non-linear operators:

\begin{equation}
R_m^f(\eta) = f_{m+1}^* + \frac{1}{2} \sum_{k=0}^{m-1} \left[ f_{m-1-k} f_k^* \right] - \text{De} \sum_{k=0}^{m-1} f_{m-1-k} \sum_{l=0}^{k} \left[ f_{k-l} f_l^* \right] - \frac{\text{De}}{2} \sum_{k=0}^{m-1} f_{m-1-k} \sum_{l=0}^{k} \left[ f_{k-l} f_l^* \right] - M^2 \left[ f_{m-1-k} f_k^* \right] - M^2 \text{De} \sum_{k=0}^{m-1} \left[ f_{m-1-k} f_k^* \right] - M^2 \text{De} \sum_{k=0}^{m-1} \left[ f_{m-1-k} f_k^* \right] + \text{KDe} \sum_{k=0}^{m-1} \left[ f_{m-1-k} f_k^* - \eta f_{m-1-k} f_k^* \right] + 2 \text{Ds} \sum_{k=0}^{m-1} \left[ \eta f_{m-1-k} f_k^* + \eta f_{m-1-k} f_k^* - f_{m-1-k} f_k^* \right] - K f_{m-1-k} \sum_{k=0}^{m-1} \left[ f_{m-1-k} f_k^* + f_{m-1-k} f_k^* \right] (26)
\end{equation}
\[ R_m^0(\eta) = \frac{4}{3} R d \theta_m^* + \text{Pr} h s \theta_m^* + \text{Pr} \left( \sum_{k=0}^{m-1} \frac{1}{2} \theta_{m-1-k}^* f_k \right) \]  
\[ \chi_m = \begin{cases} 
0, & m \leq 1 \\
1, & m > 1 
\end{cases} \]  

**Numerical solution**

System model represented by eqs. (10)-(12) are discretized using the forward, backward and central difference formula based on 5 point stencils \[34-36\].

For velocity profile \( f(\eta) \), the discretization formulas:

\[ f'(\eta) = \frac{-25 f(\eta + 0h) + 48 f(\eta + 1h) - 36 f(\eta + 2h) + 16 f(\eta + 3h) - 3 f(\eta + 4h)}{12 h} \]  
\[ f''(\eta) = \frac{35 f(\eta + 0h) - 104 f(\eta + 1h) + 114 f(\eta + 2h) - 56 f(\eta + 3h) + 11 f(\eta + 4h)}{12 h^2} \]  
\[ f'''(\eta) = \frac{-5 f(\eta + 0h) + 18 f(\eta + 1h) - 24 f(\eta + 2h) + 14 f(\eta + 3h) - 3 f(\eta + 4h)}{2 h^3} \]

Accordingly, the discretization formula for \( \theta(\eta) \) are constructed similarly. With the help of discretization formula, the system eqs. (10)-(12) is transformed into system of non-linear algebraic equations with are tackled numerically up to the tolerance level of \(10^{-6}\).

**Error analysis**

The set of eqs. (10) and (11) along with wall conditions (12) are coupled and highly non-linear. Therefore, error analysis has been performed in order to get the validated results. We have prepared figs. 2 and 3 which show the error in velocity and temperature profiles. These plots show that error in the computations are very much negligible.

![Figure 2. Error in f](image)

![Figure 3. Error in \( \theta \)](image)

**Rheological results**

It is noted that system of non-linear eqs. (10)-(12) contains several physical and rheological quantities involving Deborah numbers, magnetic parameter, internal heat generation/absorption quantity, wall convection parameter, etc. Therefore, we have prepared
figs. 4-12 and tab. 1 showing the behavior of the involved parameters on the velocity and temperature profiles. Figures 4 and 5 presents the heat transfer rate for different values of magnetic parameter and porosity parameter. Front bar shows the results of propane whereas back bar presents the results of ethylene glycol. It is observed that heat transfer rate decreases in both case when the magnetic parameter and the porosity parameter are increased. Figures 6 and 7 are prepared to show the effects of Deborah numbers (De and Ds) on the flow field. It is observed that velocity profile and its associated boundary-layer thickness decreases as values of De gets higher but for the case of Ds velocity profile declines. Small values of Deborah numbers (De, Ds << 1) signifies the flowing behavior while their large values (De, Ds >> 1) corresponds to solid-like behavior. Moreover, opposite trend of the velocity profile is noted for the positive values of De and Ds. Figure 8 portrays the effects of magnetic field on the velocity profile. We have seen that there is inverse relation between magnetic parameter and fluid’s velocity. Figure 9 provides the temperature profiles for different magnitudes of magnetic parameter. It is noticed that temperature and thermal boundary-layer thickness improves for larger magnetic parameter. In fact, magnetic parameter relies on Lorentz force. As magnetic force increases, stronger the Lorentz force is and that create development in temperature and its boundary-layer thickness. In fig. 10 influence of internal heat generation/absorption parameter, \( hs \), on temperature profile is displayed. Note that \( hs < 0 \) corresponds to the heat absorption phenomena while \( hs > 0 \) represents the heat generation situation. It is observed that the temperature and its associated boundary-layer is decreasing.
function of heat absorption coefficient whereas an increase in temperature is noticed for the case of heat generation. Variation in temperature profile for different values of Biot number, \( \gamma_1 \), are sketched in fig. 11. Here temperature and thermal boundary-layer thickness show an increasing behavior for large values of \( \gamma_1 \). Figure 12 portrays the 3-D flow configuration of the considered analysis. This plot clearly shows that maximum variation is near the moving wall where decays slowly and tend to uniform free stream. Tables 1 and 2 are prepared to present the numerical magnitudes of local skin friction and local Nusselt numbers against several rheological parameters.
Conclusions

In present analysis, we examined the dynamics of Sakiadis flow of Oldroyd-B fluid over a permeable wall. Some final outcomes for present study are made on the basics of graphical results are listed as follows.

Table 1. Numerical values of skin friction against several physical quantities

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Numerical solutions</th>
</tr>
</thead>
<tbody>
<tr>
<td>De</td>
<td>$h_s$</td>
</tr>
<tr>
<td>0.0</td>
<td>0.5</td>
</tr>
<tr>
<td>0.5</td>
<td>0.5</td>
</tr>
<tr>
<td>1.0</td>
<td>0.5</td>
</tr>
<tr>
<td>1.5</td>
<td>0.5</td>
</tr>
<tr>
<td>0.5</td>
<td>-1.5</td>
</tr>
<tr>
<td>0.5</td>
<td>-1</td>
</tr>
<tr>
<td>0.5</td>
<td>-0.5</td>
</tr>
<tr>
<td>0.5</td>
<td>0</td>
</tr>
<tr>
<td>0.5</td>
<td>0.5</td>
</tr>
<tr>
<td>0.5</td>
<td>1.0</td>
</tr>
<tr>
<td>0.5</td>
<td>1.5</td>
</tr>
<tr>
<td>0.5</td>
<td>0.5</td>
</tr>
<tr>
<td>0.5</td>
<td>0.5</td>
</tr>
<tr>
<td>0.5</td>
<td>0.5</td>
</tr>
<tr>
<td>0.5</td>
<td>0.5</td>
</tr>
<tr>
<td>0.5</td>
<td>0.5</td>
</tr>
<tr>
<td>0.5</td>
<td>0.5</td>
</tr>
<tr>
<td>0.5</td>
<td>0.5</td>
</tr>
<tr>
<td>0.5</td>
<td>0.5</td>
</tr>
<tr>
<td>0.5</td>
<td>0.5</td>
</tr>
<tr>
<td>0.5</td>
<td>0.5</td>
</tr>
<tr>
<td>0.5</td>
<td>0.5</td>
</tr>
<tr>
<td>0.5</td>
<td>0.5</td>
</tr>
<tr>
<td>0.5</td>
<td>0.5</td>
</tr>
<tr>
<td>0.5</td>
<td>0.5</td>
</tr>
<tr>
<td>0.5</td>
<td>0.5</td>
</tr>
<tr>
<td>0.5</td>
<td>0.5</td>
</tr>
<tr>
<td>0.5</td>
<td>0.5</td>
</tr>
<tr>
<td>0.5</td>
<td>0.5</td>
</tr>
<tr>
<td>0.5</td>
<td>0.5</td>
</tr>
</tbody>
</table>
Velocity and momentum boundary-layers decrease for larger values of De but both shows enhancement with rising values of Ds.
Magnetic field reduces the velocity of fluid.
The temperature profile improves by increasing magnetic field.

Table 2. Numerical values of wall temperature gradient against several physical quantities

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Numerical solutions</th>
</tr>
</thead>
<tbody>
<tr>
<td>De</td>
<td>hs</td>
</tr>
<tr>
<td>0.0</td>
<td>0.5</td>
</tr>
<tr>
<td>0.5</td>
<td>0.5</td>
</tr>
<tr>
<td>1.0</td>
<td>0.5</td>
</tr>
<tr>
<td>1.5</td>
<td>0.5</td>
</tr>
<tr>
<td>0.5</td>
<td>-1.5</td>
</tr>
<tr>
<td>0.5</td>
<td>-1</td>
</tr>
<tr>
<td>0.5</td>
<td>-0.5</td>
</tr>
<tr>
<td>0.5</td>
<td>0</td>
</tr>
<tr>
<td>0.5</td>
<td>0.5</td>
</tr>
<tr>
<td>0.5</td>
<td>1.0</td>
</tr>
<tr>
<td>0.5</td>
<td>1.5</td>
</tr>
<tr>
<td>0.5</td>
<td>0.5</td>
</tr>
<tr>
<td>0.5</td>
<td>0.5</td>
</tr>
<tr>
<td>0.5</td>
<td>0.5</td>
</tr>
<tr>
<td>0.5</td>
<td>0.5</td>
</tr>
<tr>
<td>0.5</td>
<td>0.5</td>
</tr>
<tr>
<td>0.5</td>
<td>0.5</td>
</tr>
<tr>
<td>0.5</td>
<td>0.5</td>
</tr>
<tr>
<td>0.5</td>
<td>0.5</td>
</tr>
<tr>
<td>0.5</td>
<td>0.5</td>
</tr>
<tr>
<td>0.5</td>
<td>0.5</td>
</tr>
<tr>
<td>0.5</td>
<td>0.5</td>
</tr>
<tr>
<td>0.5</td>
<td>0.5</td>
</tr>
<tr>
<td>0.5</td>
<td>0.5</td>
</tr>
<tr>
<td>0.5</td>
<td>0.5</td>
</tr>
<tr>
<td>0.5</td>
<td>0.5</td>
</tr>
<tr>
<td>0.5</td>
<td>0.5</td>
</tr>
<tr>
<td>0.5</td>
<td>0.5</td>
</tr>
<tr>
<td>0.5</td>
<td>0.5</td>
</tr>
<tr>
<td>0.5</td>
<td>0.5</td>
</tr>
<tr>
<td>0.5</td>
<td>0.5</td>
</tr>
</tbody>
</table>
• Opposite behaviors of heat generation and absorption effects is observed over temperature profile.
• Large values of Biot number causes increase in temperature.

In future, it looks promising to explore the potential of stochastic numerical computing methodologies [37-41] based on artificial intelligence procedures to analyze the dynamics of Sakiadis flow of Oldroyd-B fluid over a permeable wall model.

References