STUDY OF THE PHENOMENON OF THE INTERACTION BETWEEN SESSILE DROPS DURING EVAPORATION

by

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This research work represents an experimental study of the interaction between water drops deposited on a substrate at ambient temperature. To examine this phenomenon, the evaporation of a single drop deposited on a substrate was first investigated. Then, several drops were deposited alongside on the same substrate under the same conditions. The central drop dynamic behavior was also examined and compared with that of a single drop. This comparison shows the effect of the interaction between the neighboring drops, which delayed the evaporation of these drops and particularly the central droplet, on evaporation. In fact, three configurations were studied by changing the initial distance, d, between the drops (d = 0.2 mm, d = 7 mm, and d = 15 mm). The obtained results reveal that the interaction phenomenon becomes less important by increasing the distance between the drops. This is important for optimizing many industrial applications, such as spray drying, fuel injection in combustion engines, and other applications.
Key words: *deposited drop, evaporation, liquid-gas interface and interaction, relative humidity*

Introduction

Evaporation of a drop deposited on a substrate is considered as a complex phenomenon during which several processes, such as the Marangoni effect, mass and thermal transfers, interact. This phenomenon was widely dealt with in many research works because of its intensive application in various fields as spray drying, DNA mapping [1, 2], inkjet printing [3, 4], combustion engineering [5-7], electronic cooling [8], cooling system [9], *etc.*

For instance, authors, in [10, 11], studied the evaporation of a sessile drop. They proved that the substrate thermophysical properties can significantly affect the evaporation rate.

Besides, Lopes *et al.* [12] examined the influence of the substrate thermal properties (glass and silicone) on the evaporation time of the water droplets. They showed that evaporation, in the case of silicon, is faster than that in the case of a glass substrate due to its high thermal conductivity.

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Numerous studies were also carried out on the evaporation modes of a sessile drop [13-15]. They revealed the existence of three behavioral modes of the sessile drop evaporation. The first mode is characterized by the reduction of the contact angle and the anchoring of the contact line (constant contact line mode). However, the second mode is characterized by the decrease of the contact line and the stabilization of the contact angle (constant contact angle mode). Whereas the third mode, called stick-slip mode [16], is characterized by minimizing the angle contact and the contact line simultaneously. The last mode was observed during the evaporation of different liquids [17-19] especially with the presence of nanoparticles [20, 21].

Moreover, several works demonstrated that, at the liquid-gas interface, the surface tension varies as a function of temperature. This variation involves the Marongonia forces investigated by many authors.

Lu *et al.* [22] examined the Marangoni effect on temperature evolution *vs.* time at the liquid-vapor interface and at the upper surface of the substrate.

Yan *et al.* [23] proved that the role of Marangonie is more evident for the large values of the initial contact angle.

Ouenzerfi *et al.* [24] presented an experimental study on the inversion of the Marangoni effect of a drop of binary mixture (97% water – 3% butanol) under a horizontal temperature gradient. They showed that a binary drop (97% water – 3% butanol) tends to move to warmer areas.

Pin *et al.* [25] used an acoustic method to track the alcohol concentration at the bottom of a droplet of binary solution during the evaporation process.

However, conducting a numerical simulation of droplet evaporation is not an easy task, mainly because of the coupling of heat and mass transfer processes with the evolution of the free surface. To avoid the tracing of the free interface, some previous numerical simulation studies [26, 27] focused on the evaporation at certain contact angle and contact line (fixed droplet profile), while others simulated the droplet volume variation as a function of time by decoupling the interface evolution with an evaporation calculation [28-31].

In fact, the flow evaporated at the liquid-gas interface was the subject of several research works.

For example, Widjaja *et al.* [32] studied a profile of the flow evaporated at the liquid-gas interface, showing that the evaporation is more intense near the triple line.

Galvin [33] demonstrated that the concentration of saturated vapor above the liquid-gas interface depends on the droplet curvature.

To our knowledge, the literature taking place have focused on understanding the transfer phenomena of evaporation of a drop but in practice, applications involving several drops on the same substrate. The interaction between the drop does not extrapolate the results of a drop. The study of the evaporation of a drop surrounded by several drops is needed to examine the effect of the interaction between them: this is the subject of this work.

To show the effects of the presence of several drops, the work has a section dedicated to the evaporation of a drop and a second portion where the drop will be surrounded by six other neighboring drops.

Experimental process

The sapphire substrate was placed in a controlled room ($14 \times 12.4 \times 7.5$ cm^3) with temperature $T_{amb} = 21$ °C and humidity $H = 50\%$, fig. 1. The water drop having initial temperature $T_0 = 20$ °C and 0.7 µl volume was deposited on the sapphire substrate using a pro-

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grammable syringe (KdScientific legato 100), resulting in a deposit drop diameter of about 1.5 mm.

Obviously, there was no air movement inside the room whose upper part was equipped with an infrared transparent sapphire window to allow measuring the temperature at the drop surface using the infrared camera (FLIR X6580SC, 640×512 pixels, 15 μm detector pitch). The room was also equipped with a hole for the syringe passage.

Figure 1. Schema of the experimental set-up

A Kruss-shape analyzer was employed to measure the drop contact angle, its volume, its diameter and its height during evaporation. A side view CCD camera (Allied Vision Technologies, 780×580 pixels) was utilized to record the process of the drop evaporation.

Experimental results

Description of the evaporation of a single drop of water on a substrate

In this part, we will study the single drop sessile on a sapphire substrate.

Figures 2 and 3 show the variations of the volume, the contact angle, and the drop diameter over time, respectively.
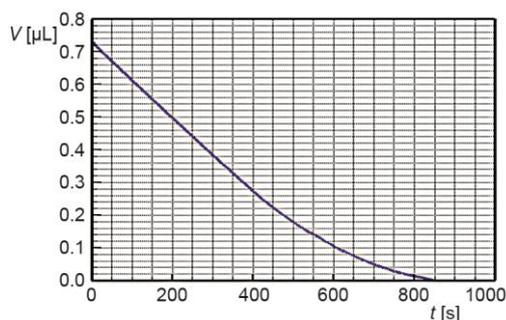

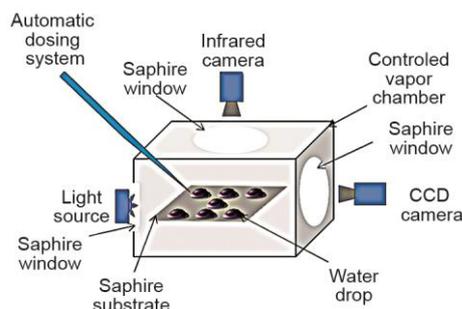**Figure 2. Variations in the volume of drop as function of time at $T_{amb} = 21$ °C and $H = 50\%$**

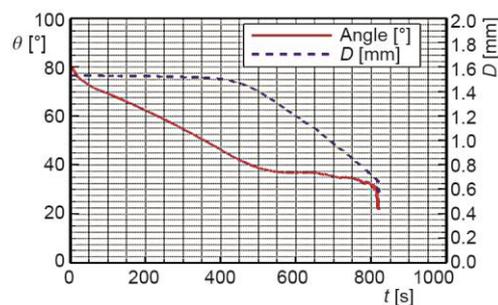**Figure 3. Variations in the contact angle and diameter of drop as function of time at $T_{amb} = 21$ °C and $H = 50\%$**

In fact, the drop volume decreased over time. The drop, evaporating on the sapphire, had a constant diameter for almost half of the drop life, while the contact angle minimized linearly over time. Two evaporation stages were observed:

Stage 1 – during this stage, the drop evaporated according to a constant contact line mode. After about 450 seconds, the diameter began to diminish linearly, while the contact angle remained constant for a period $\Delta t = 350$ s.

Stage 2 – the drop evaporated in a constant contact angle mode.

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Stage 3 – during this stage, the drop deposited on the substrate exhibited a different behavior in which the diameter and the contact angle were reduced simultaneously until the drop disappeared totally, which represents the stick slip mode.
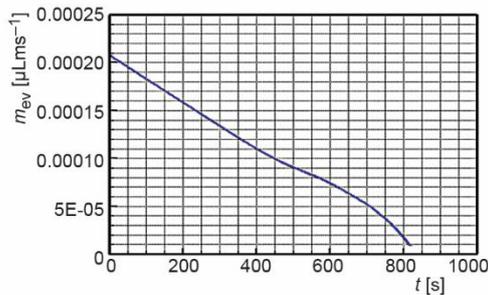

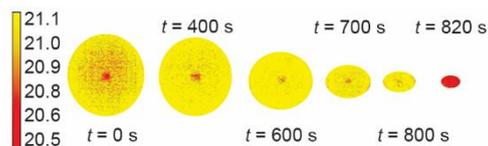**Figure 4. Evolution of the evaporated density over time; $T_{amb} = 21$ °C and $H = 50\%$**

Figure 5. Snapshots from infrared video camera of evaporation process of water drop until the total disappearance of drop: $T_{amb} = 21$ °C and $H = 50\%$
(*for color image see journal web site*)

Figure 4 demonstrates the evolution of the evaporated density over time. Indeed, the evaporated density attained its maximum value at $t = 0$ seconds because the concentration gradient, c_{sat}, c_{amb}, was important at $t = 0$ seconds. Obviously, at the beginning of evaporation, the air, in the drop immediate vicinity, became wetter and temperature decreased at the liquid-gas interface. This behavior was due to the effect of the interface cooling by evaporation which led to a considerable decline in the concentration gradient c_{sat}, c_{amb}, and explained the decrease in the evaporated density over time.

The drop images taken at different times reveal of the drop evaporation, fig. 5. In this figure, we present the process of the water drop evaporation until its total disappearance. We notice, from the experiment, that the life of this water drop is was around 820 seconds.

At the beginning of evaporation, to become relatively constant, the liquid-gas interface temperature did not require long time. Then, it decreased relatively at the end of the evaporation due to the interface cooling by evaporation.

Study of the interaction between drops during evaporation

Because in most industrial applications of the evaporation of liquid drops the latter are close to each other, it is important to study the phenomenon of their interaction during the evaporation process by considering the symmetrical configuration of a central drop surrounded by others, Configuration (b). Thus, the aim of our investigation is to study the effect of the interaction between the neighboring drops on the evaporation of the central drop. Using the syringe, we deposited these drops, separated at a relatively small distance ($d = 0.2$ mm ± 0.02 mm), on the substrate. Their evaporation is done under the same conditions as the configuration of a single drop, Configuration (a).

Description of the phenomenon

The disposition of drops is described in fig. 6(a): 4 drops at the extremity (E_1, E_2, E_3, E_4), 2 drops at the center (C_2, C_3), and 1 central drop C_1.

In fig. 6(b), we present a series of images taken by an infrared camera. These images show the evolution of the drops size as a function of time. They also demonstrate that the evaporation of the drops at the extremities (E_1, E_2) was faster, compared to that of the drops at the center (C_2 and C_3), particularly the central drop.

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At $t = 3$, the corresponding photo reveals that the diameter of the drops remained constant, which does not necessarily mean the absence of evaporation that can also take place in constant contact line mode.

At $t = 1200$, a reduction in both the drop diameter and size occurred at the extremities (E_1, E_2, E_3, E_4) which have already reached the constant contact angle mode (Stade 2) demonstrated fig. 3. However, the minimization of the diameter of the drops at the center (C2, C3), particularly the central drop, C1, was not remarkably observed but that does not necessarily mean the absence of evaporation. The evaporation can take place in a constant contact line mode (Stade 1). This highlights the interaction of the central drop with its neighbors. This result may be explained by changing local conditions in the vi-

Figure 6(a). The description of drops arrangement (*for color image see journal web site*)

cinity of the central drop C1. The relative humidity, in proximity close to the gas-liquid interface of the central drop, increased due to evaporation of neighboring drops, which saturated the air surrounding the central drop and therefore reduced the density evaporated at the gas-liquid interface of this drop. From the previously mentioned results, we may deduce that the evaporation of the central drop was delayed by that of the neighboring drops: The drops disappeared from the end towards the center (corresponding pictures at times $t = 1300$, $t = 1600$, and $t = 1700$ seconds).
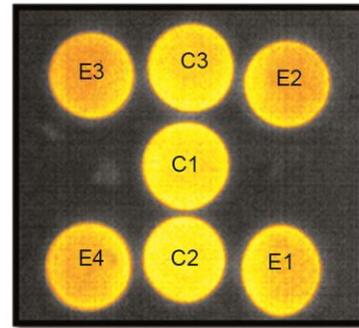
Figure 7 shows that the life of the central drop is pretty meadows 1760 seconds. Comparing the kinetics of evaporation of this drop to that of a single drop, fig. 5, we can conclude that the phenomenon of interaction increases the lifetime of the drop of 51%.
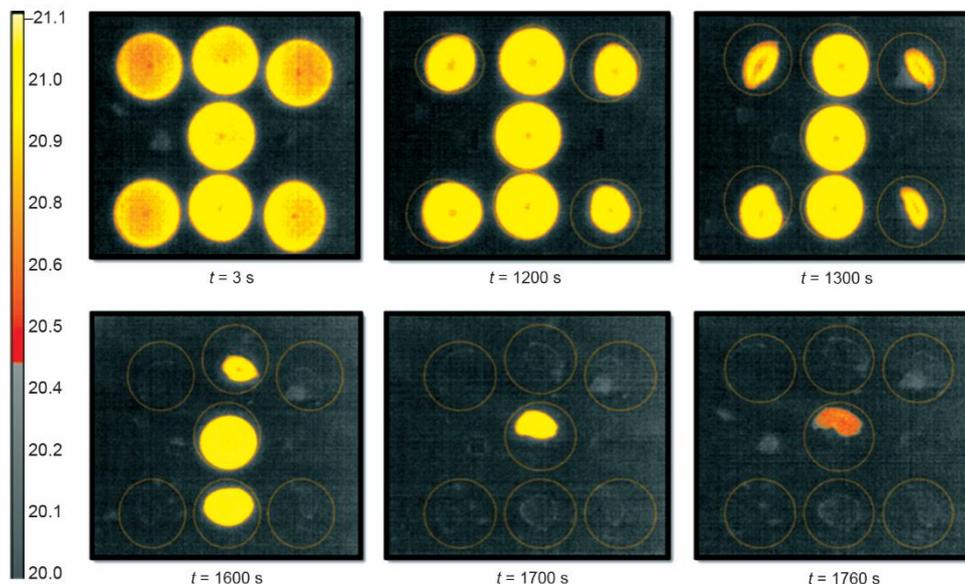

Figure 6(b). Snapshots of evaporation process over time: $T_{amb} = 21\,°C$ and $H = 50\%$ of the drops close to each other ($d = 0.2$ mm ± 0.02 mm) taken by infrared video camera (*for color image see journal web site*)
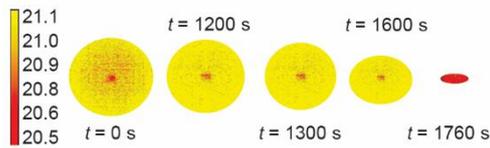
Figure 7. Snapshots of the evaporation process of water central drop until its total disappearance: $T_{amb} = 21\ °C$ and $H = 50\%$ taken by infrared video camera
(*for color image see journal web site*)

Effect of the interaction between drops on evaporation

In this section, we will study the influence of interaction on the evaporation process by comparing the two following configurations: Configuration (a): a single drop deposited on the substrate (single drop) and Configuration (b): a drop surrounded by 6 other drops.

Figure 8 illustrates the evolution of the drop volume over time for both configurations. We note that the volume of the single drop, Configuration (a), decreased more rapidly than that of the surrounded drop, Configuration (b).

The life time of the drop deposited on a substrate and surrounded by six other drops close to each other, Configuration (b), was twice more than that of the drop deposited separately on the substrate, Configuration (a). This result shows that the interaction between the drops resulted in the central drop evaporation, which confirms the result observed in fig. 6.

We can conclude that, if the drop is surrounded by other neighbors, the volume will be reduced by 55%, for 850 seconds, compared to the case of an isolated drop

Figures 9 and 10 show the variations in the drop diameter and contact angle over time for both Configurations (a) and (b). From these figures, we notice that both the central drop, Configuration (b), and the single drop, Configuration (a), evaporated according to the same evaporation mode.
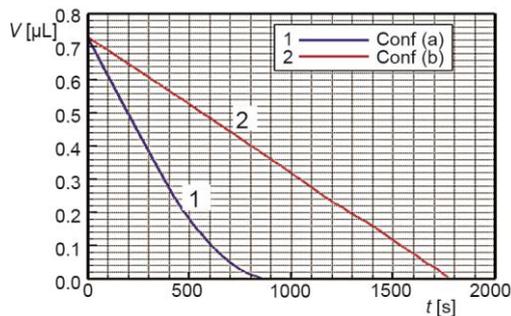

Figure 8. Variations in the drop volume as function of time for both configurations; Configuration (a) – a single drop and Configuration (b) – a drop surrounded by other drops: $T_{amb} = 21\ °C$ and $H = 50\%$
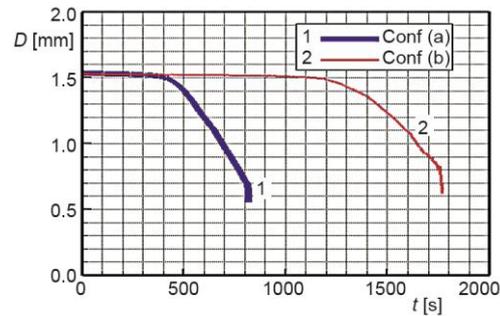

Figure 9. Variations in the drop diameter as function of time for both configurations; Configuration (a) – a single drop and Configuration (b) – a drop surrounded by other drops: $T_{amb} = 21\ °C$ and $H = 50\%$

Figure 11 depicts the evolution of the evaporated drop density over time for both Configurations (a) and (b) and shows the effect of the phenomenon of interaction on evaporation.

The corresponding curve for the Configuration (a) – (single drop), takes a maximum value at $t = 0$ seconds. Then, it decreases over time, against the values of the density shown in Configuration (b) – (gout surrounded), are void at the beginning of evaporation and then increases over time.

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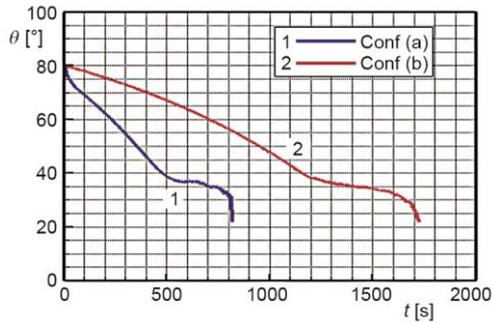
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Figure 10. Variations in the drop contact angle as function of time for both configurations; Configuration (a) – a single drop and Configuration (b) – a drop surrounded by other drops: $T_{amb} = 21$ °C and $H = 50\%$
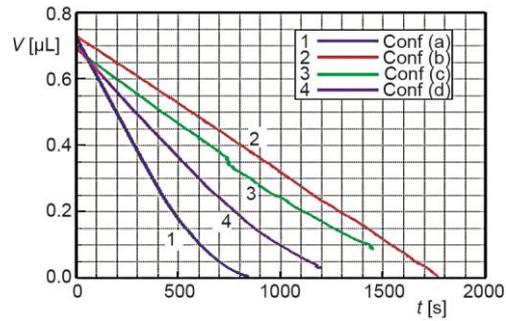

Figure 11. Evolution of the evaporated density over time for both configurations; Configuration (a) – a single drop and Configuration (b) – a drop surrounded by other drops: $T_{amb} = 21$ °C and $H = 50\%$

In fact, at the beginning of evaporation, the central drop evaporated density was relatively negligible and drops were still very close to each other, which delayed the central drop evaporation. Obviously, it was not the same case for a single drop where evaporation was triggered at $t = 0$ seconds. Then, the evaporated density began to increase with the decrease of the neighboring drops influence. This can be explained mainly by the fact that the neighboring drops increased humidity at the air liquid interface of the central drop. Thus, the complete disappearance of the neighboring drops decreased the humidity nearby the central drop, which accelerated considerably its evaporation.

To examine the influence of the distance between the different drops on the kinetics of the central drop evaporation, we plotted the curves presented in fig. 12 which demonstrates the evolution of the central drop volume for three configurations: $d = 0.2$ mm, $d = 7$ mm, and $d = 15$ mm (d is the distance between two successive drops). From this figure, it is noted that the volume of central drop decreased considerably by rising the distance, d, between the drops.

Figure 12. Variations in the drop volume as function of time for the four studied configurations: Configuration (a) – a single drop, Configuration (b) – $d = 0.2$ mm, Configuration (c) – $d = 7$ mm and Configuration (e) – $d = 15$ mm at $T_{amb} = 21$ °C and $H = 50\%$

Indeed, the increase of the distance d between the drops induces:
− the increase in the volume of air surrounding the central drop and
− the decrease of humidity around the liquid-gas interface of the central drop.

Therefore, this evaluation shows that the interaction phenomenon between the drops was reduced by increasing the distance, d.

Summary of the results

The obtained results are summarized in tab. 1 in which we compare the findings of a single drop, Configuration (a), with those of a surrounded drop in terms of the drop life time and volume. We considered the three configurations: Configuration (b), Configuration (c),
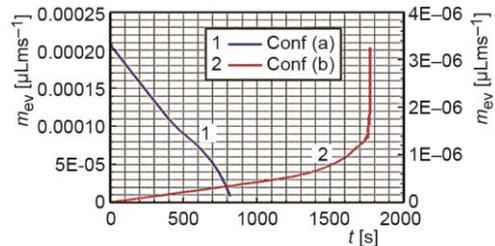
and Configuration (e) by changing the distance between the drops. From this table, we can conclude that the volume of the surrounded drop was reduced, in 850 seconds, by 55%, in configuration Configuration (b), by 43% in configuration Configuration (c), and by 23% in configuration Configuration (e), compared to the case of a single drop. These results prove that the interaction phenomenon between the drops became less important by increasing the distance between the drops.

Table 1. Summary table

	Single drop $V_0 = 0.7$ μl: Configuration (a)	Drop surrounded by other drops, $V_0 = 0.7$ μl		
		Configuration (b): $d = 0.2$ mm	Configuration (c): $d = 7$ mm	Configuration (e): $d = 15$ mm
The life expectancy of the drop [s]	850	1770	1650	1250
V_{rest} ($t = 850$ seconds) [μl]	0	0.383	0.302	0.161
$\dfrac{\Delta V (850 \text{ seconds})}{V_0}$ [%]	100	45	56	77

where V_o presents the initial volume of drop, $V_o = 0.7$ μl, V_{rest} ($t = 850$ s) – the volume remaining at the instant $t = 850$ s, ΔV (850 s) [μl] corresponds to the evaporated liquid during $\Delta t = 850$ s, [$\Delta V(850$ s)]/V_0 – the percentage of the evaporated liquid during $\Delta t = 850$ s, and the comparison time, $t = 850$ s is that of the total evaporation of the single drop.

Conclusion

In this research work, we highlighted the importance of the neighborhood effect on the evaporation of a water drop. From this study, we can conclude the following.
- For drops which are very close to each other ($d = 0.2$ mm), the total evaporation can be minimized by 55% compared to that of an isolated drop. This reduction is mainly due to the increase of humidity near the drops.
- To decrease the effect of proximity on evaporation, the distance, d, between the drops must be increased.
- The variation of the distance between the neighboring drops allowed controlling the evaporation kinetics in cases where standard control parameters, such as humidity or substrate temperature, were out of control.
- This finding is important to optimize many industrial applications, such as spray drying, fuel injection in combustion engines, *etc*.

Nomenclature

c – molar concentration, [molm^{-3}]
D – diameter, [mm]
d – distance between two successive drops, [mm]
H – relative humidity
m_{ev} – evaporated density, [μlm^{-1}s^{-1}]
T – temperature, [C]
t – time, [s]
V – volume [μl]

Greek symbol

θ – contact angle

Subscripts

0 – initial
amb – environmental condition
rest – remaining
sat – saturated

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