THE COMBINED EFFECT OF NANOFLUID AND REFLECTIVE MIRRORS ON THE PERFORMANCE OF PV/Thermal Solar Collector

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A photovoltaic thermal (PV/T) solar collector is a system which is capable of producing both electricity and thermal energy; however, this technology still needs more studies. In this paper, a mathematical model was presented to study the performance of a PV/Thermal collector by using the upper and lower reflectors with the presence of glass cover. Water and nanofluids (Al\textsubscript{2}O\textsubscript{3}-H\textsubscript{2}O) were used as cooling medium. A computer program was proposed to calculate the amount of solar radiation reflected on the reflected mirrors and then absorbed by the hybrid collector and study the effect of Nano-fluid on the performance of the system. Solar radiation absorbed by the collector can be increased using the upper and lower reflectors to 1138 W/m\textsuperscript{2} while it can reach 950 W/m\textsuperscript{2} with the upper reflector and 746 W/m\textsuperscript{2} with the lower reflector. It was noticed that when using reflective mirrors, the outlet water temperature increased by 21.7\%. Meanwhile, the outlet water temperature increased by 0.44\% when nanofluid was used as a cooling medium. The average of daily thermal efficiency as a result of using two reflectors without nanofluid was 62.1\%, while the thermal efficiency was 59.735\% without using any reflector, meaning a positive effect of using reflectors on the thermal efficiency. The electrical efficiency reduced with the existence of the reflective mirrors, whereas the daily average of the total electrical efficiency without the reflective mirror and using the nanofluid was (14.6\%), while with a reflective mirror and using nanofluid, the daily average was (13.67\%). Key words: PV/Thermal collector, Nanofluid, reflective mirrors, performance.

1. Introduction

The use of solar energy to generate electricity is one of the most important applications at the present time as these cells convert solar energy into a constant current[1]. However, the disadvantage of these cells is the high temperature during work, especially in hot sunny climates as in the Middle East which is characterized by a hot climate for most days of the year. The high temperature of cells causes a decrease in their efficiency. For this reason, researchers have tried to improve the performance of solar cells by withdrawing the heat generated in them and making use of them for
heating and other industrial purposes[2]. Hybrid solar collectors (PV/Thermal collector) supply electricity and hot water or hot air at the same time. They integrate the two systems together; solar cells and heaters[3]. This system is mainly designed to increase the electrical efficiency of solar cells by drawing heat from these cells.

Kostic et al.[3,4] studied the effect of using aluminum mirrors on the performance of hybrid solar collectors. The produced thermal and electrical energies increased considerably when using the reflectors in an ideal method with the ideal angle calculated to be 66°. Tabet et al.[6] studied the effect of using a plane reflector to improve the performance of photovoltaic thermal air collector in Algeria. A mathematical model was presented to show the effect of the reflector. The study showed that there was an improvement in the performance of the collector when using this reflector.

Naik and Palatel[5] used a single mirror mounted on the top of the hybrid solar collector and at angles ranging from 85-100° in the Indian city of Kolkata, which enjoys a tropical climate. Baccoli et al.[6] analyzed the mathematical model of a flat solar collector connected to an external inverter at the bottom edge of the collector. The mathematical model was developed and used to estimate the solar radiation passing through a transparent cover of the collector with and without a reflector. Bahaidarah et al.[7] presented an experimental and analytical study of the effect of the mirrors placed at an angle on the performance of a hybrid solar collector. Belhadj et al.[8] studied the effect of the angle of two reflective plates to increase the intensity of solar radiation on solar cells. Chowdhury [9] analyzed a concentrated hybrid photovoltaic-thermal collector. The goal of this design was to increase the total efficiency of the hybrid collector. The overall efficiency of the collector was about 80%. Rosli et al.[10] studied the thermal efficiency of a polymer collector with unglazed photovoltaic thermal (PVT) system. The thermal efficiency of the system was 47%. Soltani et al.[11] improved the photovoltaic efficiency of the PV/T collector by using the nanofluid technique. Five different cooling methods were used practically, namely natural convection, forced air cooling, water cooling, SiO$_2$/water nanofluid cooling, and Fe$_3$O$_4$/water nanofluid cooling. The results indicated that the water nanofluid cooling by using SiO$_2$ materials, which were found to have the highest power and optimum efficiency, showed 54.29% and 3.35% improvement respectively, compared to the natural cooling method.

A mathematical model was performed by Mustafa et al.[12] to evaluate the performance of PV/Thermal nanofluid system. The goal of this article is to study theoretically a new design of the PV/T system which includes stainless steel rectangular tube. Nanofluid provides a higher performance, where the electrical and thermal efficiencies of this system obtained approximately 14.38% and 71.71% at the mass flow rate of 0.174 kg/s and 650 W/m$^2$ solar radiation. Colangelo et al.[13] presented a new design of PV/Thermal collector, this new design of hybrid system was analyzed using commercial software for thermal simulations, two models have been investigated: vertical configuration and horizontal configuration, considering a flow rate of 0.1 liter/min and of 0.5 liter/min of fluid, with a tilt of 30 deg. An analytical study has been carried out by Tripathi et al.[14] to study the performance of three cases for PV/T collector at constant flow rate. This study showed that the N-convectional compound parabolic concentrator collector connected in series is chosen superior than other cases.

Hussein et al.[15] utilized the nanoparticle type (Zn-H$_2$O) to improve the performance of the hybrid PV/T collector. The results showed that using the nanofluid led to improved electrical and thermal efficiency of the collector. Ghadiri et al.[16] used nanofluid type (Fe$_3$O$_4$ - water) with
concentrations ranging from 1% - 3% to improve the performance of the hybrid solar collector and found an increase in the efficiency of the hybrid collector (3%). Kim et al. [17] studied the effect of using glass cover on the performance of the hybrid solar collector used to heat the water and found that it improved thermal efficiency by 14% while the electrical efficiency decreased by 1.4%. Glass is an undesirable option when the priority is to produce electric power. Al-Shamani et al. [18] used nanofluid such as TiO$_2$/water, SiO$_2$/water, and SiC/water as a coolant in the photovoltaic thermal collector that contains serpentine shaped absorber design with rectangular cross-section. The results showed that the PV/Thermal collector with SiC nanofluid had the highest combined thermal performance of 81.73% and electrical efficiency of 13.52%. Sardarabadi et al. [19] studied the effect of using metal-oxides/water as nanofluids in the PV/Thermal collector. This study showed that the overall exergy efficiencies for the cases of PVT/water, PVT/TiO$_2$, PVT/Al$_2$O$_3$, and PVT/ZnO are enhanced by 12.34%, 15.93%, 18.27% and 15.45%, respectively, compared to that of the solar cell with no collector. Potenza et al. [20] studied the performance of parabolic trough collector (PTC), with transparent receiver tube, based on gas-phase nanofluid. Two coaxial tubes, with vacuum in the inner space were used as receiver pipe. Colangelo et al. [21] used numerical software to investigate the effect of nanofluid on the performance of the solar thermal collector. The study showed that there was an improvement in the performance of the collector when using the nano technology. The researchers found that when using Nano fluid, an increase in the thermal efficiency of the system has been achieved by (7.45%). Chemisana et al. [22] using a Fresnel lens to enhance the performance of the PV/Thermal collector for building – façade integration. This study showed that the electric power generated by this system is about 4.5-4.7 time higher than in the classical PV/T collector. Also, the thermal power ratio takes a value raging from 1.9 to 2.8 depending on the weather conditions.

By reviewing the literature related to the study of the performance of PV/Thermal solar collectors, no study was found combining the effects of reflective mirrors and nanofluid on the performance of these systems. Therefore, this study will focus on the study of variables affecting the performance of the systems with reflective mirrors and nanofluid to achieve a clear understanding of their effects and improve the performance of the hybrid PV/T collector.

2. Mathematical Models

The design of the hybrid solar collector used in this study consists of one glass cover, the solar cell, heat exchanger coated with the aluminum sheets on the back side of the solar cell, upper reflector connected to the upper side of the hybrid collector and the lower reflector connected to the lower side of the hybrid collector. The PV/Thermal collector with the reflective mirrors system is shown in Fig. (1). The collector type is serpentine as shown in Fig. (2).

2-1 Solar radiation calculations:

The isotropic diffuse model was derived by Liu and Jordan used to estimate the rate of solar radiation[10]. The total radiation ($S_{\text{total}}$) on the tilted PV/thermal collector included five components: the direct radiation ($I_b$), diffuse radiation ($I_d$), solar radiation reflected from the ground ($I_g$), radiation reflected ($I_{up-ref}$) from upper reflector to the surface of PV panel with tilted plane angle ($\alpha_1$) and the radiation reflected ($I_{lo-ref}$) from the bottom mirror to the solar cell with tilted plane angle ($\alpha_2$) as shown in Fig. (1). Therefore the total absorbed solar radiation on the tilted surface is the sum of five terms as:
The radiation components are calculated from the following equations[23]:

\[ I_b = I_{\text{total}} \sin(\alpha + \beta)(\tau \alpha)_b \]  \hspace{1cm} (2)

\[ I_d = I_{\text{diffuse}} ((1 + \cos\beta)/2)(\tau \alpha)_d \]  \hspace{1cm} (3)

\[ I_g = \rho_g I_{\text{total}} \left( (1 - \cos\beta)/2 \right)(\tau \alpha)_g \]  \hspace{1cm} (4)
\( \rho_e \) is the ground reflectance (equal to 0.4)[24]. The reflected radiation from upper reflector \( I_{up-ref} \) with tilted mirror angle \( \alpha_1 \) and reflected radiation from lower reflector \( I_{lo-ref} \) with tilted mirror angle \( \alpha_2 \) are defined as:

\[
I_{up-ref} = \rho A_1 \cdot I_{total} \cdot \sin(\tau) \cdot \sin(\alpha + \alpha_1) \cdot (\tau \alpha)_b , \quad \tau = \alpha + 2\alpha_1 - \beta \quad (5)
\]

\[
I_{lo-ref} = \rho A_1 \cdot I_{total} \cdot \sin(x) \cdot \sin(\alpha - \alpha_2) \cdot (\tau \alpha)_b , \quad x = \beta + 2\alpha_2 - \alpha \quad (6)
\]

The angles \((x)\) and \((\tau)\) are explained in Fig. 1. The total solar radiation \((I_{total})\), diffused radiation \((I_{diffuse})\), solar altitude angle \((\alpha)\) and transmittance–absorptance product \((\tau \alpha)\) were calculated according to the procedure as discussed in[23].

2-2 Thermo-physical Properties of Nano-fluid (\(AL_2O_3-H_2O\)):

Pure water is selected as the base-fluid with temperature dependent properties as shown in Table (1)[24]. \(AL_2O_3\) was used as nanoparticles in this study; the properties of \(AL_2O_3\) used for the modelling are summarized from references[25]. Thermo-physical properties of the working fluid \((AL_2O_3-H_2O \text{ Nano-fluid})\) are changed due to influence of the nanoparticles. These properties can be found from standard tables or equations.

**Table (1) Variation of water properties with the temperature**

<table>
<thead>
<tr>
<th>Property</th>
<th>Formula</th>
</tr>
</thead>
<tbody>
<tr>
<td>Density (kg/m³)</td>
<td>( \rho_w = 1000 - 0.0178(T-277)^{1.7} )</td>
</tr>
<tr>
<td>Viscosity (kg/m.s)</td>
<td>( \mu_w = 1.788 \times 10^{-3} \exp(-1.704 \cdot (1448.5/T + 521926.58/T^2)) )</td>
</tr>
<tr>
<td>Thermal conductivity (W/m.K)</td>
<td>( K_w = -8.01 \times 10^6 \cdot T^{-273} + 1.94 \times 10^{-3} \cdot (T-273) + 0.536 )</td>
</tr>
<tr>
<td>Specific heat (J/kg.K)</td>
<td>( c_w = 4.1855 \times 10^3 \cdot [0.966185 + 0.0002874 \cdot (T-173)/100]^{5.26} )</td>
</tr>
</tbody>
</table>

The properties of Nano-fluids can be estimated by using the following equations:

\[
\rho_{eff} = \rho_w (1 - \phi) + \rho_n \phi \quad (7)
\]

Where, \( \rho_{eff} \) is the nanofluid density, \( \rho_l \) and \( \rho_n \) are the water and \(AL_2O_3\) densities.

\( \phi \) is the nanofluid volume fraction calculated as[26]:

\[
\phi = \frac{m_n / \rho_n}{m_n / \rho_n + m_w / \rho_w} \quad (8)
\]

Where, \( m_n \) and \( m_w \) are the mass of \(AL_2O_3\) and water, respectively.

The heat capacity of Nano-fluid \((C_{eff})\) is calculated from[21]:

\[
C_{eff} = \frac{\phi \rho_n c_n + (1 - \phi) \rho_w c_w}{\rho_{eff}} \quad (9)
\]

where the \( c_n \) and \( c_w \) are the heat capacity of \(AL_2O_3\) and water, respectively.

The viscosity of Nano-fluid is given by [15]:

\[
\mu_{eff} = \frac{\mu_w}{(1 - \phi)^{2.5}} \quad (10)
\]

The Maxwell equation is used to evaluate the thermal conductivity of Nano-fluid \((K_{eff})\) as[25]:
\[ K_{\text{eff}} = \frac{K_u + 2K_w + 2h(K_u - K_w)}{K_u + 2K_w - h(K_u - K_w)} K_w \]  
\[ \text{where } K_u \text{ and } K_w \text{ are the thermal conductivity of } Al_2O_3 \text{ and water, respectively.} \]
The Prandtl number can be calculated from the following equation[27]:
\[ Pr_{\text{eff}} = \frac{\mu_{\text{eff}} C_{\text{eff}}}{K_{\text{eff}}} \]  

2-3 Thermal modeling of the system:

To model the PV/Thermal collector, a number of simplified assumptions are as follows[23]:

1. The flow in the system is incompressible, laminar, and uniform.
2. Performance is a semi-steady state.
3. Heat flow through a cover is one dimensional and temperature drop through a cover was negligible. Also, there is one-dimensional heat flow through back insulation.
4. The sky can be considered as a blackbody for long-wavelength radiation at an equivalent sky temperature.
5. Temperature gradients around tubes can be neglected. The temperature gradients in the direction of flow and between the tubes can be treated independently.
6. Loss through front and back are to the same ambient temperature.
7. Dust and dirt on the collector are negligible.
8. Shading of the collector absorber plate is negligible.
9. Nanofluid is assumed as a single phase fluid.

Mainly, the energy input to the PV/Thermal solar collector is in the form of solar radiation from the sun and the thermal fluid flowing inside the heat exchanger from the inlet. The energy from the system is due to the heat loss by convection and thermal fluid outflow from the collector. The total thermal energy gain by PV/T collector is expressed as[28]:
\[ \bar{Q}_a = A_F \bar{F}_R \left[ \bar{S} - U_{\text{loss}} (T_{f,in} - T_a) \right] \]  

Where, \( \bar{F}_R \) is called the modified collector heat removal factor and calculated for the serpentine arrangement of PV/Thermal collector from the following equation[23]:
\[ \bar{F}_R = F_1 F_2 F_3 \left[ \frac{2F_4}{F_6 \exp \left[ -\sqrt{1 - F_2^2} / F_3 \right] + F_5} - 1 \right] \]  
\[ F_4 = \left( \frac{1 - F_2^2}{F_2^2} \right)^{0.5}, \quad F_5 = \frac{1}{F_2} + F_4 - 1, \quad F_6 = I - \frac{1}{F_2} + F_4 \]
\[ \kappa = \frac{\delta U_{\text{loss}}^{1/2}}{\sinh \left[ (W - D) (U_{\text{loss}} / K_{\delta})^{1/2} \right]}, \quad \gamma = -2 \cosh \left[ (W - D) \left( U_{\text{loss}} / K_{\delta} \right)^{1/2} \right], \quad \frac{DU_L}{\kappa} = \frac{1}{C_b} + \frac{1}{\pi Dh_f} \]

Where, \( \delta \) is the thickness of the solar cell, \( k \) is the thermal conductivity of the material, and \( h_{f,i} \) is the convection heat transfer coefficient inside the tube and calculated for the nanofluid from the following relations [15]:
where

\[
h_{r,i} = \frac{K_{rel}}{D} \left[ 4.36 + \frac{0.086 \left( \frac{Re_{eff} Pr_{ref} D}{L} \right)^{0.83}}{1 + Pr_{eff} \left( \frac{Re_{eff} D}{L} \right)^{0.83}} \right]^{0.33}
\]

\[
Re_{eff} = \frac{4m}{\pi D \mu_{eff}}
\]

\( W \) is the distance between the tubes, \( D \) is the tube diameter, \( C_b \) the bond conductance, and \( L \) is the length of the tube.

The portion of solar radiation incident on the solar cell is converted into electricity, therefore the modified solar radiation can be calculated from the following equation[29]:

\[
\bar{S} = S_{total} \left[ 1 - \eta_{PV} \right]
\]

(15)

Where \( \eta_{PV} \) is the instantaneous electrical efficiency of the PV cells at their operating temperature and it be calculated from the following equation[30]:

\[
\eta_{PV} = \eta_{ref} \left[ l - B(T_{PV} - T_{ref}) \right]
\]

(16)

Where \( \eta_{ref} \) is the standard cell efficiency at reference temperature (\( T_{ref} = 25 \) °C).

The modification heat loss coefficient can be calculated from the following equation:

\[
\bar{U}_{loss} = U_{loss} - \frac{S}{\alpha_{pv}} \eta_{i} B
\]

(17)

The outlet temperature can be calculated from the following equation:

\[
T_{out} = \frac{\bar{Q}_{v}}{\dot{m}C_{eff}} + T_{fin}
\]

(18)

The total thermal energy gain by PV/T collector in terms of the mean solar cell temperature can be expressed as [23]:

\[
\bar{Q}_{v} = A \left[ \bar{S} - \bar{U}_{loss} (T_{PV,m} - T_{v}) \right]
\]

(19)

The mean solar cell temperature can be solved by equating equations (13) and (19) to get:

\[
T_{PV,m} = \frac{\bar{Q}_{v} / A}{\bar{F}_{r} \bar{U}_{loss}} \left( l - \bar{F}_{r} \right) + T_{fin}
\]

(20)

The heat loss coefficient \( U_{loss} \) is the summation of three components [31]:

\[
U_{loss} = U_{top} + U_{back} + U_{edge}
\]

(21)

The top loss coefficient is given by [32]:

\[
U_{t} = \left[ \frac{l}{h_{w} + h_{gs}} \right]^{t}
\]

(22)

\( h_{w} \) = wind heat transfer coefficient and calculated by [23]:

\[
h_{w} = 5.7 + 3.8V_{w}
\]

(23)

\( V_{w} \) = wind velocity (m/s)
$h_{rgs}$ = the radiation heat transfer coefficient between the glass cover and the sky obtained as follows[13]:

$$h_{rgs} = \varepsilon_g \alpha (T_g^2 + T_s^2)(T_g + T_s)$$  \hspace{1cm} (24)

Where, $T_g$ = mean glass temperature (°C), $\varepsilon_g$ = glass emittance, and $T_s$ = sky temperature and calculated from the following equation [33]:

$$T_s = 0.0558T_{at}^{1.5}$$  \hspace{1cm} (25)

The heat transfer from the edges can be neglected while the back heat transfer coefficient ($U_b$) can be evaluated by considering conduction and convection from the bottom of the hybrid collector as:

$$U_b = \frac{L_b}{k_b} \left[ 1 + \frac{1}{h_w} \right]^{-1}$$  \hspace{1cm} (26)

Where, $L_b$ and $k_b$, are the thickness and thermal conductivity of the insulation (Glass wool).

The electrical power can be calculated from the following equation[34]:

$$Q_{ele} = \frac{A_S \eta_{PV}}{\alpha_{PV}} \left[ I - \frac{\eta_{ref} \beta}{\eta_{PV}} \left( F_R (T_{f,in} - T_s) + \frac{\bar{S}}{U_{loss}} (1 - F_R) \right) \right]$$  \hspace{1cm} (27)

The thermal efficiency of the system can be calculated using the following equation[35]:

$$\eta_{th} = \frac{Q_s}{I_{total} \cdot A_c}$$  \hspace{1cm} (28)

Also, the electrical efficiency of the PV/Thermal hybrid collector evaluated from the relation[36]:

$$\eta_{ele} = \frac{Q_{ele}}{I_{total} \cdot A_c}$$  \hspace{1cm} (29)

The overall efficiency of the hybrid air collector is the summation of thermal and electrical efficiencies as:

$$\eta_{overall} = \eta_{ele} + \eta_{th}$$  \hspace{1cm} (30)

The MATLAB program was used to solve the above equations to obtain the theoretical results and compare these results with the experimental data.

4. Results and discussions:

This article presents the results of a study done to assess the combined effect of nanofluid and reflective mirrors on the performance of hybrid solar collector under Iraqi climate conditions. The system was set towards the south to benefit from a large extent of sun radiation. The collector tilted plane angle ($\beta$) was 45°. The angle of the upper and lower reflectors was 5° and 35°, respectively. Table 2 shows weather conditions during test (29th March) of Kirkuk city (35.46°N and 44.39°E) in Iraq. The system was put towards the south to benefit from a large extent of sun radiation. The collector tilted plane angle ($\beta$) was 45°.
Table (2) The weather condition for the test day.

<table>
<thead>
<tr>
<th>Time (Hour)</th>
<th>$T_{\text{ambient}}$ (°C)</th>
<th>Wind velocity (m/sec)</th>
<th>Solar radiation (W/m$^2$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>8</td>
<td>23.9</td>
<td>0.1</td>
<td>434.66</td>
</tr>
<tr>
<td>9</td>
<td>21.5</td>
<td>0.2</td>
<td>533.0</td>
</tr>
<tr>
<td>10</td>
<td>22.8</td>
<td>0.3</td>
<td>597.43</td>
</tr>
<tr>
<td>11</td>
<td>23.6</td>
<td>0.1</td>
<td>626.95</td>
</tr>
<tr>
<td>12</td>
<td>24.3</td>
<td>0.1</td>
<td>615.08</td>
</tr>
<tr>
<td>13</td>
<td>24.4</td>
<td>0.4</td>
<td>565.61</td>
</tr>
<tr>
<td>14</td>
<td>25.6</td>
<td>0.3</td>
<td>481.56</td>
</tr>
<tr>
<td>15</td>
<td>25.9</td>
<td>0.9</td>
<td>366.81</td>
</tr>
<tr>
<td>16</td>
<td>24.6</td>
<td>0.5</td>
<td>208.66</td>
</tr>
</tbody>
</table>

4.1 Absorbed solar radiation

Fig. (3) shows the variation of total absorbed solar radiation in the PV/T collector calculated from equation (1). The value of solar radiation increased with time and reached its maximum value of 558 W/m$^2$ at 12 noon for this particular day without using any reflective mirrors. The maximum value was 1139 W/m$^2$, approximately 51% of the system when using the upper and lower reflective mirrors on the same day. Meanwhile the maximum value of the total absorbed solar radiation with the presence of the upper or lower reflector alone was 951 W/m$^2$ and 747 W/m$^2$, respectively. These results are consistent with the results of [10]. This amount of absorbed solar radiation was then used as an input variable for the performance calculations.

Figure 3. Variation of Solar radiation with reflectors and without reflectors

4.2 Temperature of PV panel:

Fig.(4) shows the comparison between the PV panel temperatures for different operating conditions at 1% Nano-fluid mass fraction. The results showed that the panel surface temperature produced the same behavior of the absorbed solar radiation. The temperature of solar cell surface increased in the first hours of testing till midday and then decreased as the intensity of solar radiation
decreased till sunset[7][11]. The highest temperature of the cell surface using the nanofluid and two reflectors together was 63.67 °C whereas the conventional PV/Thermal collector (with nanofluid and without reflectors) was 44.3°C at midday, which means that thermal performance increased in the case of using the reflectors and nanofluid. The existence of reflectors and nanofluid as a cooling material leads to the increasing in the rates of different temperatures in PV/T collector corresponding to the behavior of conventional solar collectors [37][9].

4.3 Temperature of outlet water:

Fig.( 5 ) displays the comparison of the water outlet temperature for the eight model previously discussed. It was noticed that the outlet water temperatures were increasing throughout the period between 9 a.m. and 1 p.m., which indicates that the useful energy ( \( \overline{Q}_{u} \) ) was higher than that carried out by the load water. After 1 p.m., these temperatures started decreasing because the value of useful energy became lower than the energy carried out by the load water. The outlet temperature reached the maximum value of (50.021 °C) for the system (two reflectors and 1% Nano-fluid mass fraction), whereas in the case of the conventional PV/Thermal collector (without nanofluid and reflectors), the temperature was 39 °C at 1 p.m. The reason behind the rise in the temperature of the solar cell was the existence of the reflectors. These results accorded with the published literature [5][25][14].

**Figure 4. Variation of solar cell temperature for different operating conditions**

4.4 Thermal and electrical efficiencies:

The variation of useful transferred energy follows closely the variation of solar intensity. Fig.( 6 ) shows that there was a high increase in the thermal efficiency during the first hours of the operating period 8-10 a.m. for all cases. This is because of the large increase in the net energy absorbed due to the presence of mirrors, coupled with relatively small heat losses from the collector to the ambient atmosphere because of the low temperature of the cell surface which reduces the thermal losses . The instantaneous efficiency also reached its maximum value of 66.57 % at 9 a.m. for the hybrid collector
without a reflector and then decreased. This trend is due to the increasing heat losses with the time of the day accompanied with decreasing net energy absorbed in the afternoon hours; the time at which the maximum instantaneous efficiency occurrence was found to be different for dissimilar conditions. It was also observed that on the second half of the day (after 2 p.m.), there was a noticeable increase in the instantaneous efficiency resulting from an increase in the useful energy transferred. The hybrid collector with two reflectors and without using the Nano-fluid was found to be more efficient than other systems. It was also noticed that the using of nanofluid reduced the daily thermal efficiency for different cases[38].

![Figure 5. Variation of outlet water temperature for different operating condition](image)

![Figure 6. Variation of thermal efficiency ($\eta_{th}$) with time for different cases (1% concentration)](image)
The existence of the reflective mirrors increased the thermal efficiency due to the rise of solar radiation that occurred on the surface of the solar cell. Hence, this choice is deemed favorable for getting the highest energy and also agreeable with the results of published articles[3]. The average of daily thermal efficiency as a result of using two reflectors without Nano-fluid was 62.1% , while the thermal efficiency without using any reflector was 59.735 %. This indicates a positive effect of using reflectors on the thermal efficiency[7]. Fig. (7) shows the electrical efficiency following the solar radiation except near noon because the increase of the solar panel temperature caused the decrease in the electrical efficiency for all cases. It was observed from the figure that the system using the Al₂O₃/water cooling without reflectors had the highest efficiency with the maximum value of daily electrical efficiency was 14.6 %. It can be seen that the electrical efficiency was reduced with the existence of the reflective mirrors, whereas the daily average of the total electrical efficiency without the reflective mirror and using the nanofluid was 14.6%, while with a reflective mirror and using nanofluid, the daily average was 13.67%. This is related to the reflective mirror which increases the solar radiation that leads to the increase of the solar cell temperature and means a reduction in its efficiency. It was also noticed that the increase in electrical efficiency in the first morning hours was due to the decrease in the temperature of solar cell, then started to decline gradually at noon due to the increase in the temperature of the solar cell and after that started to rise slightly in the afternoon, and then began to reduce due to the decline the solar radiation quantity reaching the solar cell. This agreed with the experimental results from the previous studies[11][39]. It was also noted that the total efficiency values of most of the designs were semi-equal. It was also noted that the overall efficiency increased in the presence of the reflective mirror and decreased with the used of Al₂O₃/water as a cooling media[40].

**Figure 7. Variation of electrical efficiency with time for different cases (1% concentration)**

5. Conclusions:

In the present article, the common effect of reflective mirror and nanofluid on the performance of a PV/Thermal water collector was discovered. From the finding of the previous sections, the following results are obtained:
1- The existence of reflectors and nanofluid as cooling materials leads to the increase in the rates of different temperatures in PV/T collector corresponding to the behavior of conventional solar collectors.
2- The outlet water temperature increased by 21.7%, while the outlet water temperature increased by 0.44% when nanofluid was used as a cooling medium.
3- The usage of reflective mirrors was the main factor in the enhancement of the performance of the PV/Thermal collector compared to the use of Nano-fluid.
4- The system using the Al₂O₃/water cooling without reflectors had the highest electrical efficiency; the maximum value of daily electrical efficiency was 14.6%. It was also noticed that the using of nanofluid reduced the daily thermal efficiency for different cases.

Nomenclatures:

- collector surface area, [m²]
- coefficient of Photovoltaic cell, [β = 0.0045°C⁻¹]
- temperature coefficient of efficiency, [-]
- heat capacity of the nano material (Al₂O₃), [Jkg⁻¹°C⁻¹]
- heat capacity of the base fluid (water), [Jkg⁻¹°C⁻¹]
- heat capacity of Nano-fluid, [Jkg⁻¹°C⁻¹]
- current, [A]
- total absorbed radiation on the collector surface, [Wm⁻²]
- beam radiation on the collector surface, [Wm⁻²]
- diffuse solar radiation, [Wm⁻²]
- component of solar radiation reflected from upper reflector, [Wm⁻²]
- component of solar radiation reflected from lower reflector, [Wm⁻²]
- solar radiation reflected from the ground, [Wm⁻²]
- diffused radiation, [Wm⁻²]
- thermal conductivity of Nano-fluid, [Wm⁻¹K⁻¹]
- thermal conductivity of water, [Wm⁻¹K⁻¹]
- thermal conductivity of nanoparticale, [Wm⁻¹K⁻¹]
- mass flow rate, [kg⁻¹]
- Prandtl number (=μ_effC_eff/K_eff), [-]
- total thermal energy gain, [Wm⁻²]
- total absorbed solar radiation, [Wm⁻²]
- ambient air temperature, [°C]
- solar cell temperature, [°C]
- air temperature at the inlet, [°C]
- air temperature at the outlet, [°C]
- temperature of solar cell at standard condition, [T_o = 25 °C]

Greek symbols

- transmittance-absorptance product, [-]
- thermal absorbtance of cell, [-]
- solar altitude angle, [°]
- angle between upper reflector and horizontal plane, [°]
- angle between lower reflector and vertical plane, [°]
- collector tilted plane angle, [°]
\( \gamma_S \) - solar azimuth angle, [\( ^\circ \)]
\( \delta \) - declination angle of the sun, [\( ^\circ \)]
\( \varphi \) - latitude of the location of thermal collector, [\( ^\circ \)]
\( \rho_{A1} \) - reflectance from mirrors, [-]
\( \rho_g \) - ground reflectance, [-]
\( \phi \) - volume concentration of the nanoparticles
\( \mu_w \) - water viscosity, [kgm\(^{-1}\)C\(^{-1}\)]
\( \mu_{eff} \) - nanofluid viscosity, [kgm\(^{-1}\)C\(^{-1}\)]
\( \rho_w \) - density of the water, [kgm\(^{-3}\)]
\( \rho_n \) - density of the nanoparticle, [kgm\(^{-3}\)]
\( \rho_{eff} \) - density of the nanofluid, [kgm\(^{-3}\)]
\( \eta_{PV} \) - instantaneous electrical efficiency, [-]
\( \eta_{ele} \) - electrical efficiency, [-]
\( \eta_{th} \) - thermal efficiency, [-]

6. References:


