INFLUENCE OF HEAT IN-LEAK, LONGITUDINAL CONDUCTION AND PROPERTY VARIATIONS ON THE PERFORMANCE OF CRYOGENIC PLATE-FIN HEAT EXCHANGERS

by

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For helium liquefaction/refrigeration systems, conventional design theory always fails in cryogenic applications and heat exchangers operating at low temperatures are usually sensitive to longitudinal heat conduction, heat in-leak from surroundings and variable fluid properties. Governing equations based on distributed parameter methods are developed to evaluate performance deterioration caused by these effects. The model synthetically considering these loss mechanisms is validated against experimental data and design results obtained by commercial software Aspen MUSE. Sample multi-stream heat exchangers are further studied to discuss quantitative effects of these heat losses. In accordance with previous researches, the comprehensive effects of various losses are analyzed qualitatively in order to reveal their influences and investigate on the strategies of improving the heat transfer performance. The numerical method is useful in the design procedure of cryogenic heat exchangers and can be adopted to predict heat transfer and pressure drop performance under the actual low temperature environment.

Key words: heat exchanger, longitudinal conduction, heat in-leak, helium liquefier, helium refrigerator

Introduction

Counter-flow plate-fin heat exchangers (PFHE) are commonly utilized in cryogenic applications due to their high effectiveness and compact size. In helium liquefaction/refrigeration systems, PFHE are always used to further cool the coming hot and high pressure helium gas by recuperating most sensible heat from the low pressure vapor. However, for the cryogenic applications, various parameters such as longitudinal heat conduction, heat-in-leak from surroundings and property variations of fluid need to be considered carefully, which are often neglected in the conventional design procedure of heat exchangers. Lumped parameter models, as the basic design theory, i.e. the effectiveness-number of heat transfer units (ε-NTU) method, the logarithmic mean temperature difference method and so on, are based on the assumptions of steady-state, negligible heat transfer from ambient, no longitudinal heat conduction, constant heat capacity rate, constant individual, and overall heat transfer coefficients [1, 2]. When the magnitude of these secondary parameters is too large to be neglected, these closed form solutions would not be precise enough.
During the last several decades, these effects have been studied by many researchers based on various different assumptions. For the performance deterioration caused by longitudinal heat conduction, which would flatten the temperature distributions in the wall and thus reduce the effectiveness, Kays and London [1] provided graphical results for the balanced and imbalanced counter-flow heat exchangers. More comprehensive, systematic analytical results assuming constant properties and adiabatic end conditions were proposed by Kroeger [3]. For the conditions of the heat exchanger cold end directly connected to the evaporator in Joule-Thomson refrigerators, Narayanan and Venkataraman [4] discussed the parasitic heat loss through the wall at the cold end. Hansen et al., [5] investigated the effects of longitudinal conduction and found that there exists an optimal metal conductivity for the geometry considered in the design of heat exchangers incorporated with J-T expansion process. Krishna et al., [6] studied the effect of longitudinal wall conduction on the performance of three-fluid cryogenic heat exchangers. Saberimoghaddam and Abadi [7] found that the higher tube wall thermal conductivity would not bring about a bigger temperature measurement error at tube outlet, while the wall thermal conductivity led to longitudinal conduction in the tube wall.

In addition, a significant amount of heat in-leak from ambient could be crucial in determining the heat exchanger performance. Chowdhury and Sarangi [8] analyzed a heat exchanger exposed to a parasitic heat transfer that is driven by a temperature difference between a fixed ambient temperature and the local fluid temperature. Gupta and Atrey [9] published the experimental results and numerical modeling considering the heat in-leak from surroundings and longitudinal conduction through the wall. Based on this model, the characterizations of various losses were discussed by Aminuddin and Zubair [10] assuming adiabatic and non-adiabatic end conditions. Different from the assumptions of external heat transfer linearly proportional to the temperature difference between ambient and fluid, Nellis [11] considered radiative heat transfer as the dominant parasitic in a typical cryogenic heat exchanger. The commercial software, Aspen MUSE™ [12], has been successfully used to evaluate the performance of PFHE. It can effectively take into accounts the losses due to longitudinal conduction and actual fluid physical properties, but the heat in-leak is empirically represented as a rough input from any source.

In order to study these combined effects, many numerical models have been developed. A systematic review of the evolution and challenges in mathematical models of cryogenic heat exchangers was presented by Pacio and Dorao [13]. The differential equations derived by Kroeger [3] under conditions of constant properties could be used to study the effects of longitudinal conduction for balanced and imbalanced flow qualitatively and systematically. Atrey [9] and Gupta et al., [14] extended the model to cover heat in-leak from surroundings. The numerical model presented by Nellis and Gupta et al., [11] considering the effects of property variations, metal conductivity, parasitic heat load, and heat transfer coefficients was useful in the design of a two-stream heat exchangers. To take care of transverse heat conduction for multi-stream heat exchangers, Goyal et al., [15] presented a detailed numerical model with discretizing energy balance equations additionally for fin elements.

In this study, the model early proposed is modified at the methodology of analysis and modeling, which can not only reveal the cryogenic loss mechanisms qualitatively, but also analyze the quantitative effects of these losses occurring in multi-stream heat exchangers under the actual cryogenic environment. Based on the model, the predictions are validated against experimental results presented previously. To further examine the flexibility of this model and overcome the insufficiencies of the commercial software, the results about two integrated common cases with special reference to helium liquefaction/refrigeration systems are made comparisons with the predictions. The numerical model could be useful for designers to properly
forecast the performance deterioration under conditions of considering arbitrary variations of number of transfer units, heat capacity ratios, fluid properties, metal conductivities, parasitic heat loads, heat transfer and frictional resistance coefficients along the length of heat exchangers. Compared with studies reported in previous literatures, qualitative analyses of performance influences caused by longitudinal heat conduction, heat in-leak and property variations are also performed for different number of transfer units and heat capacity rate ratios.

**Numerical model**

In this section, governing equations for a counter-flow heat exchanger with external heat transfer to the cold fluid are derived based on the conservation of energy in a control volume and expressed in dimensionless form by commonly used parameters. The computational grid consisting of the necessary nodes and elements is illustrated in fig.1. Considering the effects of longitudinal conduction tend to be concentrated at the ends, an exponentially distributed grid characterized by higher concentration of nodes near the edges is applied. The heat exchanger is divided into \( n \) sections. Each section consists of three elements: hot fluid side, cold fluid side and wall boundary. With the following assumptions:

- Steady-state conditions exist throughout the heat exchanger.
- In any cross-section for every passage, the fluid temperature and pressure perpendicular to the flow direction remain unchanged.
- The metal matrix temperature inside the core is constant along the width of the heat exchanger.
- The fluid in every passage is distributed uniformly.

The governing equations in the \( i \)-th section are:

**Hot fluid:**

\[
\frac{U_{\omega,i} + U_{\omega,i}}{2} A'_{\omega,i} \Delta x \left( \frac{T_{\omega,i} + T_{\omega,i}^* - T_{\omega,i}}{2} \right) + U_{\omega,i} A_{\omega,i} \left( T_{\omega,i} - \frac{T_{\omega,i} + T_{\omega,i}^*}{2} \right) = \frac{C_{\omega,i} + C_{\omega,i}^*}{2} (T_{\omega,i} - T_{\omega,i}^*)
\]

**Wall:**

\[
\frac{U_{\omega,i} + U_{\omega,i}}{2} A'_{\omega,i} \Delta x \left( \frac{T_{\omega,i} + T_{\omega,i}^* - T_{\omega,i}}{2} \right) + U_{\omega,i} A_{\omega,i} \left( T_{\omega,i} - \frac{T_{\omega,i} + T_{\omega,i}^*}{2} \right) + \frac{(k_{\omega,i} + k_{\omega,i}) A_{\omega,i}}{\Delta x_{\omega,i}} \left( T_{\omega,i} - T_{\omega,i}^* \right) + \frac{k_{\omega,i} A_{\omega,i}}{\Delta x_{\omega,i}} \left( T_{\omega,i} - T_{\omega,i}^* \right)
\]

**Cold fluid:**

\[
\frac{U_{\omega,i} + U_{\omega,i}}{2} A'_{\omega,i} \Delta x \left( \frac{T_{\omega,i} + T_{\omega,i}^*}{2} \right) + U_{\omega,i} A_{\omega,i} \left( T_{\omega,i} - \frac{T_{\omega,i} + T_{\omega,i}^*}{2} \right) = \frac{C_{\omega,i} + C_{\omega,i}^*}{2} (T_{\omega,i} - T_{\omega,i}^*)
\]

The energy equations can be analyzed non-dimensionally:

**Hot fluid:**

\[
\left( \frac{U_{\omega,i} + U_{\omega,i}}{2} \Delta x_{\omega,i} \right) ntu_{\omega,i}^* + \left( \frac{\theta_{\omega,i} + \theta_{\omega,i}^*}{2} - \theta_{\omega,i} \right) + 2 \alpha_{\omega,i} NTU \left( R - \frac{\theta_{\omega,i} + \theta_{\omega,i}^*}{2} \right) + 1 = \frac{\mu_{\omega,i} + \mu_{\omega,i}^*}{\mu_{\omega,i}} (\theta_{\omega,i} - \theta_{\omega,i}^*)
\]
given typical heat capacity rate ratios for reference in various cryogenic processes. As part of the high pressure stream is routed through the expander, Aminuddin and Zubair [9] suggested the value as 0.003 in general operation conditions. Barron [16] reported the value equal to 0.01 in the design of air liquefaction systems. Hausen [17] suggested the value as 0.003 in general operation conditions and 0.0001 in most cryogenic applications when the NTU is between 10 and 100. For the cryogenic heat exchanger with high vacuum and multi-layer insulation, the radiation parasitic is always used as an empirical factor. Barron [10] has given typical heat capacity rate ratio(s) for reference in various cryogenic processes.

The energy balance equations are made non-dimensional in order to improve the computational efficiency and reveal the inherent relationship between these physical quantities. Additionally, for multi-stream PFHE with more than two passages, analogous equations can be followed by the suffix, h, c, and w, respectively.

The longitudinal conduction parameter, \( \lambda_i \), is defined as a ratio of longitudinal wall heat conduction per unit temperature difference to the heat capacity rate of the fluid per unit length. Closed form expressions for calculating heat exchanger ineffectiveness, \( 1 - \epsilon_i \), have been derived by Kroeger [3] for a wide range of NTU, \( C_i/C_w \) and \( \lambda_i \). However, because of simplifications of these complex equations for imbalanced flow, the capacity rate ratio, \( C_i/C_w \) is restricted in the range 0.8 ≤ \( C_i/C_w \) ≤ 1.25 to be acceptable for most engineering computations. For some kinds of cryogenic systems such as Claude and Brayton, imbalanced flow often occurs in heat exchangers as part of the high pressure stream is routed through the expander. Aminuddin and Zubair [10] has given typical heat capacity rate ratios for reference in various cryogenic processes.
Assuming adiabatic ends for the wall, the boundary conditions specifying inlet temperatures for hot and cold fluid are expressed:

$$\theta_{in} = 1, \quad \theta_{out} = \theta_{in}$$  \hspace{1cm} (11) \\
$$\theta_{in} = 0, \quad \theta_{out} = \theta_{in} + 1$$ \hspace{1cm} (12)

Effectiveness, $\varepsilon$, defined as a ratio of the actual heat transfer rate based on the hot fluid to the maximum possible heat transfer rate, has been widely used as a measure of thermal performance of heat exchangers:

$$\varepsilon = \frac{C_p (T_{in} - T_{out})}{C_p (T_{in} - T_{max})}$$  \hspace{1cm} (13)

To consider directly the reduction in the effectiveness due to heat in-leak and longitudinal conduction, degradation factor, $\tau$, is adopted:

$$\tau = \frac{\Delta \varepsilon}{\varepsilon} = \frac{\varepsilon_{in,1} - \varepsilon_{in,2}}{\varepsilon_{in,1}}$$ \hspace{1cm} (14)

The core pressure drop in the $i^{th}$ section mainly including two components, the frictional pressure drop and the pressure drop due to the momentum rate change, can be expressed as [2]:

$$\Delta P_i = \frac{G^2}{2 \rho_i} \left[ \frac{4f}{D_h} \Delta x \left( \frac{1}{\rho_i} \right)_m + 2 \left( \frac{1}{\rho_{in}} - \frac{1}{\rho_{out}} \right) \right]$$ \hspace{1cm} (15)

**Results and discussion**

**Comparison with available experimental results**

The proposed model can also be utilized to analyze the other heat exchangers with different structures. For instance, considering heat in-leak only takes place on the cold fluid side and there exists only two streams, the accuracy of this model can be briefly examined by comparing with experimental results from coiled tube in tube heat exchangers [9]. Figure 2 illustrates the comparison between the experimental results and numerical predictions, assuming adiabatic end conditions and equal per side number of transfer units, $ntu = ntu$. It can be observed that the temperature distribution along the length of hot fluid shows a good match with the actual condition, while temperature predictions near the entrance of cold fluid are slightly lower than the actual values. As suggested by the author, the general, empirically obtained heat in-leak parameter, $\alpha$, which may be a variable along the length rather than a constant, tends to cause the error. Therefore, the differential heat in-leak parameters, $\alpha_i$, across the outside surface should be considered carefully depending on the specific circumstances.

**Examination of numerical model**

The generalized numerical model could be used to predict the performance of any multi-channel and multi-stream heat exchangers. The schematic view of the multi-channel PFHE is shown in fig. 3 and the dimensions of the core and fins for model validation are given in tab. 1. The side bar width, separating plate thickness and cap sheet thickness are set as 25, 1, and 6 mm, respectively. Two cases with the selected operation parameters from a helium refrigerator, as
shown in tab. 2, are used to analyze the flexibility and robustness of this model. The Case-1 is set as a two stream heat exchanger to study the effects due to the dramatic physical changes of helium below 20 K. The Case-2 is a three stream heat exchanger with 6 layers for the hot stream and 2, 3 layers for the other cold streams, respectively. The outer surfaces of heat exchangers are covered with multi-layer insulation to keep a low emissivity, 0.0045, and exposed to radiation from the thermal shield at 77 K.

Thermalphysical properties of helium are obtained using HEPAK [18]. The thermal conductivity of Aluminum (AL3003) at low temperature is acquired via the empirical correlation from NIST [19]. The general accepted correlations presented by Manglik and Bergles [20] are adopted to predict heat transfer and pressure drop performance. For offset strip fins, extended surfaces are used to increase the total rate of heat transfer. The above high-dimensional non-linear equations are iteratively solved by MATLAB and the calculation procedure is illustrated in fig. 4.

To examine the accuracy of numerical prediction results, commercial software Aspen MUSE [12] are further applied to make comparisons. In the software, the heat leak is used to represent a heat empirical input from any source, therefore, it can't be acquired automatically and accurately. To take heat in-leak into consideration as well, 0.01 % of the total heat transfer recommended by the engineering experience are input for two cases. The comparisons of the outlet temperature and pressure drop are illustrated in tab. 3. It can be seen that the results calculated by Aspen MUSE agree well with the numerical predictions under similar conditions. Figure 5 illustrates the lateral temperature profile at inlet, mid and outlet axial positions for eleven layers and ten separating walls as described in Case 2. There exists a non-linear temperature distribution at different axial positions to guarantee conduction heat transfer through the separating wall between the hot and cold fluids.

Table 1. Details of the heat exchanger core and fins

<table>
<thead>
<tr>
<th>Stream number</th>
<th>Case 1</th>
<th>Case 2</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>B</td>
<td>A</td>
</tr>
<tr>
<td>B</td>
<td>C</td>
<td>B</td>
</tr>
</tbody>
</table>

Figure 3. Schematic view of a multi-channel PFHE core

Table 2. Operation conditions for case studies

<table>
<thead>
<tr>
<th>Case number</th>
<th>Stream number</th>
<th>Working fluid</th>
<th>Mass flow rate [gs]</th>
<th>Inlet temperature [K]</th>
<th>Inlet pressure [kPa]</th>
<th>Number of layers</th>
<th>Layer pattern</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>A</td>
<td>Helium</td>
<td>18</td>
<td>20</td>
<td>200</td>
<td>3</td>
<td>A-B-A-B-A</td>
</tr>
<tr>
<td></td>
<td>B</td>
<td>Helium</td>
<td>18</td>
<td>4.7</td>
<td>120</td>
<td>2</td>
<td></td>
</tr>
<tr>
<td>2</td>
<td>A</td>
<td>Helium</td>
<td>30</td>
<td>80</td>
<td>1920</td>
<td>5</td>
<td>A-C-A-B-A-C</td>
</tr>
<tr>
<td></td>
<td>B</td>
<td>Helium</td>
<td>8</td>
<td>13</td>
<td>420</td>
<td>2</td>
<td>-A-B-A-C-A</td>
</tr>
<tr>
<td></td>
<td>C</td>
<td>Helium</td>
<td>24</td>
<td>13</td>
<td>128</td>
<td>3</td>
<td></td>
</tr>
</tbody>
</table>
Effect of property variations

For comparison, effectiveness curves in case-1 solved with actual local thermal-physical property variations and constant property parameters covering density, viscosity, specific heat and conductivity at the mean temperature are shown in fig. 6. The increase of the core length, representing better heat transfer effect, causes a corresponding increase in the deviation between the results of two methods. It can be also seen from this figure, degradation curve declines due to weak influences of longitudinal conduction with the increase of the core length and limited effects of heat in-leak at the very low external emissivity.

The influence curve of metal conductivity on the required heat exchanger core length under the condition of $\varepsilon = 0.8$ for Case 1 is shown in fig. 7. It can be seen that increasing metal conductivity couples with falling core length at the very low metal conductivity. Because the core length needs to be increased to make up the weak heat transfer ability to satisfy performance requirements. However, with metal conductivity gradually increasing, the core length remains almost unchanged due to the effect of longitudinal conduction begins to dominate and reduces heat transfer augmentation caused by the enhancement of metal thermal conductivity.

<table>
<thead>
<tr>
<th>Case number</th>
<th>Stream number</th>
<th>Outlet temperature [K]</th>
<th>Pressure drop [bar]</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>Aspen MUSE</td>
<td>Numerical predictions</td>
</tr>
<tr>
<td>1</td>
<td>A</td>
<td>8.79</td>
<td>9.21</td>
</tr>
<tr>
<td></td>
<td>B</td>
<td>15.45</td>
<td>15.01</td>
</tr>
<tr>
<td>2</td>
<td>A</td>
<td>18.05</td>
<td>18.94</td>
</tr>
<tr>
<td></td>
<td>B</td>
<td>74.02</td>
<td>74.12</td>
</tr>
<tr>
<td></td>
<td>C</td>
<td>73.19</td>
<td>71.66</td>
</tr>
</tbody>
</table>

Figure 4. Flow chart for the calculation procedure
Effect of longitudinal conduction parameter, $\lambda$

Figure 8 illustrates the effect of $\lambda$ on $\tau$ as a function of NTU under the condition of $ntu_1 = ntu_2$, $\alpha = 0$, and $R = 0$ for balanced flow and imbalanced flow. For the case of adiabatic end conditions and no external heat transfer, the sensible heat exchange is identical for the hot and cold fluids. Although effectiveness increases with NTU due to available additional surface area, degradation curves based on $\lambda$ represent different trends for different flows. On the whole, the performance of the heat exchanger deteriorates with the increase of $\lambda$ as the conduction effect enhances. For balanced flow, $C/C_0 = 1$, degradation curves approach asymptotic maximums at high NTU. In contrast, for unbalanced flow, $C/C_0 = 0.8 (1.25)$ degradation factors always reach the maximum at $NTU = 10$ approximately, which is close to the common design value of cryogenic heat exchangers. It is worth noting, essentially similar trends are shown in degradation curves for $C/C_0 = 0.8$ and $C/C_0 = 1.25$ due to the equal ratio of minimum to maximum heat capacity rates.

Effect of heat capacity rate ratio, $C_C/C_h$ and heat in-leak parameter, $\alpha$

Two typical cases with the temperature ranging from 300 K to 80 K ($R = 0$) and a larger temperature difference between ambient and streams, from 80 K to 20 K ($R = 3.67$) are analyzed. Fig. 9 shows the distribution curves about the effect of $C/C_0$ on $\tau$ due to $\lambda$ and $\alpha$ in a comprehensive manner. Further deterioration can be obviously observed for major operating conditions at $C/C_0 = 1$ as the temperature gradient across the length of the wall reaches the maximum. In particular, for $\alpha = 0.003$ and $\lambda = 0.001$, the degradation curve shows an ascending trend with the increase of $C/C_0$. This is because, $\alpha$, relative to $\lambda$, is sufficient enough to dominate the worsening effect of heat transfer for imbalanced flow. When $C/C_0$ increases, higher $C_C$ implies lower temperature for cold stream. With the assumption of only cold stream in the model exposed to external parasitic, heat in-leak enhances due to incremental temperature difference between ambient and cold stream.
Figure 10 illustrates degradation curves with NTU for different $\alpha$ and $C_1/C_0$ for $\lambda = 0$, $R = 0$. With the increase of $\alpha$, the heat transfer performance is further deteriorated by the aggravation of poor insulation. It can be also observed that deterioration decreases at low NTU, as the corresponding external surface area under a fixed $\alpha$ value becomes small.

In contrast, the heat exchanger is evaluated with a larger temperature difference between ambient and streams ($R = 3.67$) as illustrated in fig. 11. It shows the same trend at very low NTU while the previous law about more severe deterioration occurred in balanced flow no longer applies. It is worth noting that the figure do not include higher NTU. Because cold fluid effectiveness is likely to exceed 100% above approximately NTU = 6, as insufficient insulation may cause cold fluid to be heated warmer than the inlet hot fluid. Figure 12 shows an example for NTU = 20, $\alpha = 0.01$, $C_1/C_0 = 1$, $\lambda = 0$, and $R = 3.67$. Internal temperature cross can be observed due to the domination of external heat transfer.
The numerical model taking into account of various loss mechanisms including longitudinal heat conduction, heat in-leak from surroundings and property variations for counter-flow heat exchangers is developed in dimensionless form. This model can be successfully applied to calculate heat transfer and pressure drop performance of multi-stream PFHE and evaluate deterioration caused by these losses comprehensively for cryogenic application. For comparisons with the results from Aspen MUSE\textsuperscript{14}, two integrated cases in regard to multi-channel and multi-stream heat exchangers are calculated. The results obtained by this model are in good agreement with the software. Distinguishing from the software, the model can also calculate heat in-leak, rather than inputting an empirical value by experience, and predict the local temperature along the length for every fluid and metal wall. It can be found through this model:

- Significant deviations may occur in the results calculated by actual local thermal-physical property variations and constant property parameters.
- For a specific case, there exists a conductivity value of available metal material at the low temperature, to satisfy performance requirements with the possible least heat exchanger length.
- Performance deterioration enhances with significant $\alpha$ and $\lambda$ for cryogenic applications. In addition to operation at very low NTU, the degradation always reaches the maximum for balanced flow.
- For some extreme cases with poor insulation, temperature cross would appear due to external heat transfer from surroundings dominating the system.
- The numerical model could be used in the design of cryogenic counter-flow heat exchangers and able to calculate under the actual operation conditions to evaluate heat transfer and pressure drop performance.

### Nomenclature

**Greek symbols**

- $\alpha$ - heat in-leak parameter defined in
- $\gamma$ - numerical parameter representing the grid concentration factor, [–]
- $\varepsilon$ - effectiveness defined in eq. (13)
- $\varepsilon_e$ - effective emissivity, [–]
- $\eta_f$ - fin efficiency, [–]
- $\theta$ - dimensionless temperature defined in eq. (7)
- $\lambda$ - longitudinal conduction parameter defined in eq. (7)
- $\mu, \nu$ - capacity ratio defined in eq. (8)
- $\rho$ - density, [kgm$^{-3}$]
- $\sigma$ - stefan-boltzmann constant, [= 5.67e-8 Wm$^{-2}$K$^{-4}$]
- $\tau$ - degradation factor defined in eq. (14)

**Subscripts**

- ambient
- cold and hot fluid
- inlet and outlet
- mean value
- minimum
- separating wall

### References


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