# A HEAT TRANSFER MODEL FOR A NOVEL THERMAL MANIKIN

## by

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Thermal manikin is a functional instrument used to investigate the interaction between human body and its environment. A heat transfer model for a novel thermal manikin is established and verified experimentally, the results are of great importance to establish an international standard for manikins.

Key words: heat transfer model, thermal manikin, verification experiment

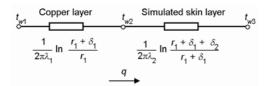
## Introduction

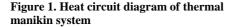
Thermal manikin is an effective and functional instrument used to study the interaction of surface heat and moisture transfer from human body, and it embodies many human features (i. e. capable of generating heat and perspiration) [1]. Since the first thermal manikin was introduced in the early 1940s, more and more manikins have been made and used widely [2]. As thermal manikins have evolved from a one-segment model to various models with more than 30 individually heated segments, the measuring accuracy based on thermal manikin has been improved significantly [3]. However, research on heat exchange on thermal manikin itself is rare and preliminary, which affects the development of international standards related with manikins. Present thermal manikin is always covered with hard metal materials, whose heat transfer is so rapid that manikin's surface temperature always changes greatly with environmental temperature, which affects manikin's stability and garment's measuring accuracy. To overcome the shortcomings, Donghua University developed a novel thermal manikin, whose typical characteristic is its soft skin covering on the outer surface of copper layer, which is a kind of thermoplastic elastomer materials and has good physical properties similar to human skin. In this paper the heat transfer study on this novel thermal manikin is performed, and the heat transfer model is established. Verification experiments indicate that the model has a higher accuracy.

## Heat transfer model

The sections of thermal manikin, such as arm, leg, trunk, and so on, could be considered as cylinder. So thermal manikin system's heat transfer is analyzed based on the theory of infinite long cylinder [4]. The heat circuit diagram of thermal manikin system is shown in fig. 1.

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The boundary conditions are:

The thermal manikin system consists of three layers, which are copper layer, simulated skin layer, and air layer. The temperature field of this system is axisymmetric, so using cylindrical coordinates is more convenient. The heat transfer differential equation is:

$$\frac{\mathrm{d}}{\mathrm{d}r}\left(r\,\frac{\mathrm{d}t}{\mathrm{d}r}\right) = 0\tag{1}$$

$$r = r_1, \qquad t \Big|_{r = r_1} = t_{w1}$$
 (2)

$$-\lambda_2 \left. \frac{\mathrm{d}t}{\mathrm{d}r} \right|_{r=r_1+\delta_1+\delta_2} = 2\pi (r_1+\delta_1+\delta_2)a(t_{w3}-t_f) + 2\pi (r_1+\delta_1+\delta_2)\varepsilon\sigma_b(T_{w3}^4-T_f^4)$$
(3)

where  $r_1$  [m] is the inner radius of long cylinder,  $\delta_1$  [m] – the thickness of copper layer,  $\delta_2$  [m] – the thickness of simulated skin layer,  $t_{w1}$  [°C] – the inner surface temperature of copper layer,  $t_{w2}$  [°C] – the interface temperature between copper layer and simulated skin layer (we suppose that the copper layer has a good contact with simulated skin layer, so the temperature of all points on the interface are the same),  $t_{w3}$  [°C] – the outer surface temperature of simulated skin layer,  $T_{w3}$  [K] – the Kelvin temperature of  $t_{w3}$ ,  $t_f$  [°C] – the temperature of air layer,  $T_f$  [K] – the Kelvin temperature of  $t_f$ ,  $\lambda_1$  [Wm<sup>-1</sup>°C<sup>-1</sup>] – the thermal conductivity of copper layer,  $\lambda_2$  [Wm<sup>-1</sup>°C<sup>-1</sup>] – the thermal conductivity of simulated skin layer, a [Wm<sup>-1</sup>°C<sup>-1</sup>] – the convective heat transfer coefficient between simulated skin layer and air layer,  $\varepsilon$  – the blackness of simulated skin layer, and  $\sigma_b$  – the radiation constant of blackbody,  $\sigma_b = 5.67 \cdot 10^{-8}$  W/m<sup>2</sup>K<sup>4</sup>.

 $r = r_1 + \delta_1 + \delta_2$ 

Integrating eq. (1), we obtain the general solution:

$$t = c_1 \ln r + c_2 \tag{4}$$

where  $c_1$  and  $c_2$  are constants. We can see that the temperature distribution follows logarithmic curve.

Solving eqs. (1), (2), and (3), we can get the heat flux and temperature distribution of copper layer, simulated skin layer and air layer. The heat transfer of these three layers is analyzed as follows.

## Copper layer

From copper layer's inner surface to outer surface, the heat exchange quantity per cylinder length is:

$$q_1 = -2\pi r \lambda_1 \frac{\mathrm{d}t}{\mathrm{d}r} \tag{5}$$

Separating the variables and making integral, we obtain:

$$q_{1} = \frac{t_{w1} - t_{w2}}{\frac{1}{2\pi\lambda_{1}} \ln \frac{r_{1} + \delta_{1}}{r_{1}}}$$
(6)

#### Simulated skin layer

From simulated skin layer's inner surface to outer surface, the heat exchange quantity per cylinder length is:

$$q_2 = -2\pi\lambda_2 \frac{\mathrm{d}t}{\mathrm{d}r} = -2\pi\lambda_0 (1+bt) \frac{\mathrm{d}t}{\mathrm{d}r} \tag{7}$$

Separating the variables and making integral, we obtain:

$$q_{2} = \frac{t_{w2} - t_{w3}}{\frac{1}{2\pi\lambda_{m}} \ln \frac{r_{1} + \delta_{1} + \delta_{2}}{r_{1} + \delta_{1}}}$$
(8)

where  $\lambda_m = \lambda_0 [1 + b/2(t_{w2} + t_{w3})].$ 

Air layer

From simulated skin layer's outer surface to air layer, the heat exchange quantity per cylinder length is:

$$q_3 = 2\pi (r_1 + \delta_1 + \delta_2) a(t_{w3} - t_f) + 2\pi (r_1 + \delta_1 + \delta_2) \varepsilon \sigma_b (T_{w3}^4 - T_f^4)$$
(9)

According to the first law of thermodynamics, we obtain the heat balance equation:

$$q = \frac{t_{w1} - t_{w2}}{\frac{1}{2\pi\lambda_1} \ln \frac{r_1 + \delta_1}{r_1}} = \frac{t_{w2} - t_{w3}}{\frac{1}{2\pi\lambda_m} \ln \frac{r_1 + \delta_1 + \delta_2}{r_1 + \delta_1}} =$$
$$= 2\pi(r_1 + \delta_1 + \delta_2)a(t_{w3} - t_f) + 2\pi(r_1 + \delta_1 + \delta_2)\varepsilon\sigma_b(T_{w3}^4 - T_f^4)$$
(10)

where q [W] is the power consumed by thermal manikin's sections.

## **Experimental verification**

To verify the accuracy of above heat transfer model, the verification experiments were performed in climate chamber by unclothed thermal manikin. The environmental temperature of climate chamber ( $t_f$ ) was set at 18 °C, 21 °C, and 24 °C, respectively. Thermal manikin's inner surface temperature ( $t_{w1}$ ) was set at 28 °C, 31 °C, 33 °C, 36 °C, 39 °C, and 42 °C, respectively. After thermal manikin came to a steady state, the power *q* consumed by each section was measured and this value was considered as experimental value. The experimental value was compared with modeling value. We just take the thigh section as an example, the comparative diagram is

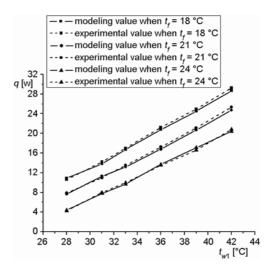


Figure 2. Comparative diagram of modeling value and experimental value (thigh section)

shown in fig. 2. We can see that the modeling value is fitting well with the experimental value. By calculating all the sections of thermal manikin, the maximum relative deviation between modeling value and experimental value is 3.11%, which approves above heat transfer model's higher accuracy.

## Conclusions

This paper analyzes the heat transfer of a novel thermal manikin with soft simulated skin. According to heat transfer theory, the heat transfer of thermal manikin system's three layers was analyzed respectively. Then the heat transfer differential equation and heat balance equation were obtained. Finally the verification experiments were performed in climate chamber by unclothed thermal manikin. Results show that the modeling value is fitting well with the experimental value, and the maximum relative deviation is 3.11%, which approves heat transfer model's higher accuracy.

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